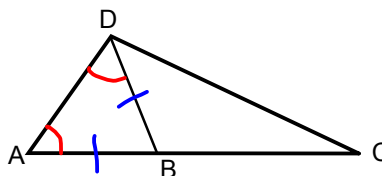


48.

Given: A-B-C; $\angle ADB = \angle DAB$

Prove: $AC > DB$



Proof:

Statements:

1. A-B-C; $\angle ADB = \angle DAB$
2. $AB + BC = AC$
3. $AB = DB$
4. $DB + BC = AC$
5. either $A < B < C$ or $A > B > C$
6. $B \neq C$
7. $BC > 0$
8. $DB + BC > DB$
9. $AC > DB$

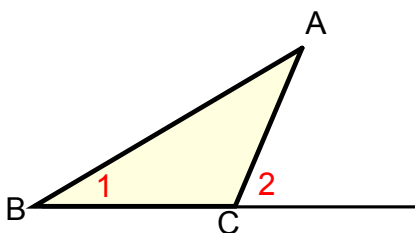
Reasons:

- Given
- Betweenness of Points Theorem
- If two angles in a Δ are =, the sides opposite them are equal
- substitution
- A-B-C (Betweenness of Points Definition)
- either $B < C$ or $B > C$ so $B \neq C$
- Ruler postulate
- Addition
- Substitution

5.2 - The Exterior Angle Theorem

Def: An **exterior angle** of a triangle is an angle that forms a linear pair with an angle of the triangle.

In ΔABC , exterior $\angle 2$ forms a linear pair with $\angle ACB$. The other two angles of the triangle, $\angle 1$ ($\angle B$) and $\angle A$ are called **remote interior angles** with respect to $\angle 2$.



Theorem 12: The Exterior Angle Theorem

An Exterior angle of a triangle is greater than either remote interior angle.

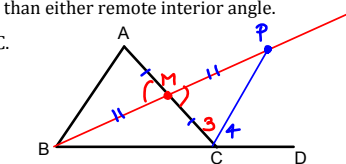
Given: $\angle ACD$ is an exterior angle of $\triangle ABC$.

Prove: $\angle ACD > \angle A$ and $\angle ACD > \angle B$

Proof:

Statements

1. $\angle ACD$ is an exterior angle of $\triangle ABC$
2. Let M be the midpoint of AC
3. $AM = MC$
4. Draw line BM
5. Choose P on line BM so that $MB = MP$
6. Draw CP
7. $\angle AMB = \angle CMP$
8. $\triangle AMB \cong \triangle CMP$
9. $\angle A = \angle 3$
10. $\angle ACD = \angle 3 + \angle 4$
11. $\angle ACD > \angle 3$
12. $\angle ACD > \angle A$



Reasons

- Given
- segment bisector is unique
(by compass construction)
- segment bisector divides a line segment into two equal segments
- two points define a line
- compass construction to copy line segment
- 2 points define a line
- vertical \angle 's are equal
- SAS congruence
- corresponding parts of congruent \triangle 's are equal
- Betweenness of Rays Theorem
- Whole greater than part
- substitution

HW #1 (submitted Friday, 11/7)

- Read Ch 1 & Ch 2
- [Ch 1 Review Problems pp. 36-38](#)
- Start working on Geometry badge on [Khan Academy](#)

HW #2 (submitted Friday, 11/14)

- Read Ch 3 & Ch 4
- [Ch 2 Review Problems pp. 71-74](#)
- [Ch 3 Review Problems pp. 124-128](#)
- Khan Academy exercises:
 - "Introduction to Euclidean geometry"
 - "Angles and intersecting lines"

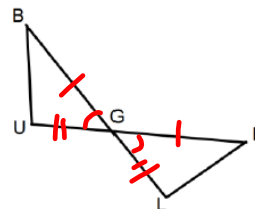
HW #3 (due Friday, 11/21)

- Read Ch 4 & Ch 5
- [Ch 4 Review Problems pp.176-180](#)
- Khan Academy exercises: "[Congruence](#)"

- | | |
|-------|-------|
| 1. J | 14. F |
| 2. W | 15. R |
| 3. P | 16. D |
| 4. G | 17. N |
| 5. L | 18. X |
| 6. E | 19. M |
| 7. S | 20. Z |
| 8. H | 21. T |
| 9. Q | 22. B |
| 10. A | 23. I |
| 11. Y | 24. K |
| 12. O | 25. U |
| 13. V | 26. C |

Given: $\angle BGU$ and $\angle EGL$ are vertical angles;
 $BG=GE$;
 $UG=GL$.

Prove: $BU=LE$



Statements:

27. $BG=GE, UG=GL$

28. $\angle BGU$ & $\angle EGL$ are vertical \angle s

29. $\angle BGU = \angle EGL$

30. $\triangle UGB \cong \triangle LGE$

31. $BU=EL$

Reasons:

Given

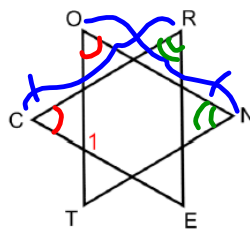
Given

vertical angles are equal

SAS Congruence

Corresponding parts of congruent Δ 's are equal

Given: $\angle C = \angle O$;
 $\angle R$ and $\angle N$ are supplements of $\angle 1$;
 $CR = ON$.



Prove: $\triangle CRE \cong \triangle ONT$.

Statements:

32. $\angle C = \angle O$; $CR = ON$

33. $\angle R$ & $\angle N$ are supplements of $\angle 1$

34. $\angle R + \angle 1 = 180^\circ$

35. $\angle N + \angle 1 = 180^\circ$

36. $\angle R + \angle 1 = \angle N + \angle 1$

37. $\angle R = \angle N$

38. $\triangle CRE \cong \triangle ONT$

Reasons:

Given

Given

Supplementary angles sum to 180°

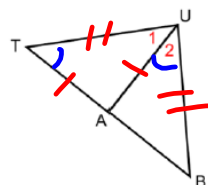
Supplementary angles sum to 180°

Substitution

Subtraction

ASA congruence

Given: $\angle T$ and $\angle 2$ are complements of $\angle 1$;
 $TA = AU$;
 $TU = UB$.



Prove: $AU = AB$.

Statements:

39. $TA = AU$; $TU = UB$

40. $\angle T$ & $\angle 2$ are complements of $\angle 1$

41. $\angle T + \angle 1 = 90^\circ$

42. $\angle 2 + \angle 1 = 90^\circ$

43. $\angle T + \angle 1 = \angle 2 + \angle 1$

44. $\angle T = \angle 2$

45. $\triangle ATU \cong \triangle AUB$

46. $AU = AB$

Reasons:

Given

Given

Complementary angles sum to 90°

Complementary angles sum to 90°

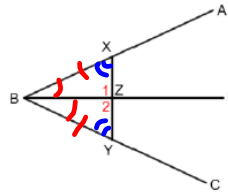
Substitution

Subtraction

SAS congruence

Corresponding parts of congruent triangles are equal.

Given: BP bisects $\angle ABC$;
 $BX=BY$;
 $\angle 1$ and $\angle 2$ form a linear pair.



Prove: $XY \perp BP$.

Statements:

47. $BX=BY$

48. $\angle BXY = \angle BYX$

49. BP bisects $\angle ABC$

50. $\angle CBP = \angle ABP$

51. $\triangle BXZ \cong \triangle BYZ$

52. $\angle 1 = \angle 2$

53. $\angle 1$ and $\angle 2$ form a linear pair

54. $XY \perp BP$

Reasons:

Given

If two sides of a triangle are equal, the ^{angles} opposite them are equal.

Given

angle bisectors divide an angle into 2 equal angles

ASA congruence

Corresponding parts of congruent Δ 's are =

Given

Two equal angles forming a linear pair have perpendicular sides