

Theorem 17: Equal corresponding angles mean that lines are parallel.

Corollary 1: Equal alternate interior angles mean that lines are parallel.

Corollary 2: Supplementary interior angles on the same side of a transversal mean that lines are parallel.

Corollary 3: In a plane, two lines perpendicular to a third line are parallel.

The Parallel Postulate – Through a point not on a line, there is exactly one line parallel to the given line.

Theorem 18: In a plane, two lines parallel to a third line are parallel to each other.

Theorem 19: Parallel lines form equal corresponding angles.

Corollary 1: Parallel lines form equal alternate interior angles.

Corollary 2: Parallel lines form supplementary interior angles on the same side of a transversal.

Corollary 3: In a plane, a line perpendicular to one of two parallel lines is also perpendicular to the other.

Theorem 20: The Triangle Sum Theorem – The sum of the angles of a triangle is 180° .

Corollary 1: If two angles of one triangle are equal to two angles of another triangle, the third angles are equal.

Corollary 2: The acute angles of a right triangle are complementary.

Corollary 3: Each angle of an equilateral triangle is 60° .

Theorem 21: An exterior angle of a triangle is equal to the sum of the remote interior angles.

Theorem 22: The AAS Theorem – If two angles and the side opposite one of them in one triangle are equal to the corresponding parts of another triangle, the triangles are congruent.

Theorem 23: The HL Theorem – If the hypotenuse and a leg of one right triangle are equal to the corresponding parts of another right triangle, the triangles are congruent.

ASA, SAS, SSS

~~SSA=ASS~~

Def: A **diagonal** of a polygon is a line segment that connects any two nonconsecutive vertices.

Theorem 24: **The sum of the angles of a quadrilateral is 360° .**

Def: A **rectangle** is a quadrilateral each of whose angles is a right angle.

Corollary to Theorem 24: **A quadrilateral is equiangular iff it is a rectangle.**

In general, if a polygon has n sides, in terms of n ,

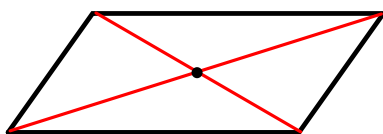
- $n-3$ diagonals can be drawn from one vertex
- these diagonals form $n-2$ triangles
- the sum of the angles of an n -gon is $(n-2)*180^\circ$
- If the n -gon is equiangular, each angle measures $(n-2)*180^\circ/n$

Def: A **parallelogram** is a quadrilateral whose opposite sides are parallel.

A figure has point symmetry if it looks exactly the same when it is rotated about a point.

Def: Two points are **symmetric with respect to a point** iff it is the midpoint of the line segment joining them.

Parallelograms have point symmetry about the point in which their diagonals intersect.



Theorem 25: The opposite sides and angles of a parallelogram are equal.

Theorem 26: The diagonals of a parallelogram bisect each other.

Theorem 27: A quadrilateral is a parallelogram if its opposite sides are equal.

Theorem 28: A quadrilateral is a parallelogram if its opposite angles are equal.

Theorem 28: A quadrilateral is a parallelogram if its opposite angles are equal.

Given: $\angle A = \angle C$
 $\angle B = \angle D$

Prove: ABCD is a parallelogram

Proof

Statements

1. $\angle A = \angle C, \angle B = \angle D$

2. $\angle A + \angle B + \angle C + \angle D = 360^\circ$

3. $\angle A + \angle B + \angle A + \angle B = 360^\circ$
 $2\angle A + 2\angle B = 360^\circ$

4. $\angle A + \angle B = 180^\circ$

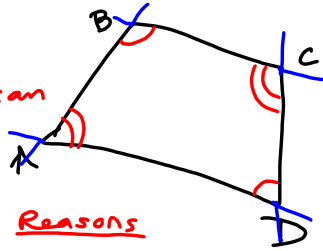
5. $\angle A$ & $\angle B$ are supplementary

6. $\angle C$ & $\angle B$ are supplementary

7. $BC \parallel AD$

$BA \parallel CD$

8. ABCD is a parallelogram



Reasons

Given

Quadrilateral Sum Theorem

Substitution (& Simplification)

Division

Supplementary \angle 's sum to 180°

substitution (#1 & #5)

Supplementary \angle 's on the same side of a transversal means lines are parallel

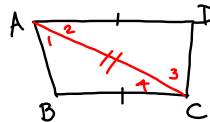
parallelogram is a quadrilateral whose opposite sides are parallel

Theorem 29: A quadrilateral is a parallelogram if two opposite sides are both parallel and equal.

Given: Quadrilateral ABCD

$AD \parallel BC$

$AD = BC$



Prove: ABCD is a parallelogram

Proof:

Statements

1. ABCD is a quadrilateral
 $AD \parallel BC$
 $AD = BC$

2. $\angle B$ and $\angle A$ are supplementary
 $\angle C$ and $\angle D$ are supplementary

3. $\angle A + \angle B + \angle C + \angle D = 360^\circ$

4. Draw diagonal AC

5. $\angle 2 = \angle 4$

6. $\angle A + \angle B = 180^\circ$

$\angle C + \angle D = 180^\circ$

7. $AC = AC$

8. $\triangle CAD \cong \triangle ACB$

9. $AB = CD$

10. ABCD is a parallelogram

Reasons

Given

Parallel lines yield supplementary interior angles on same side of transversal

Quadrilateral sum theorem

2 points define a line
 parallel lines yield equal opposite interior \angle 's

Supplementary \angle 's sum to 180°

reflexive

SAS congruence

Corresponding parts of congruent Δ 's are equal

Quadrilaterals w/ opposite sides equal are parallelograms

HW #1 (submitted Friday, 11/7)

- [Ch 1 Review Problems pp. 36-38](#)
- Start working on Geometry badge on [Khan Academy](#)

HW #2 (submitted Friday, 11/14)

- [Ch 2 Review Problems pp. 71-74](#)
- [Ch 3 Review Problems pp. 124-128](#)
- Khan Academy exercises: "[Introduction to Euclidean geometry](#)," "[Angles and intersecting lines](#)"

HW #3 (submitted Friday, 11/21)

- [Ch 4 Review Problems pp.176-180](#)
- Khan Academy exercises: "[Congruence](#)"

HW #4 (submitted Friday, 12/5)

- [Ch 5 Review Problems pp. 206-209](#)
- Work toward [mastery of practiced Khan Academy exercises](#) in "Introduction to Euclidean Geometry," "Angles and Intersecting Lines," and "Congruence"

HW #5 (submitted Monday, 12/15)

- [Ch 6 Review Problems pp. 250-254](#)

HW #6 (due ~~Friday, 12/19~~ *January*)

- [Ch 7 Review Problems pp. 292-295](#)

QUIZ #3 - NOW

TEST #2 - 2nd per - WED 12/18; 3rd per - THURS 12/19