

Theorem 17: Equal corresponding angles mean that lines are parallel.

Corollary 1: Equal alternate interior angles mean that lines are parallel.

Corollary 2: Supplementary interior angles on the same side of a transversal mean that lines are parallel.

Corollary 3: In a plane, two lines perpendicular to a third line are parallel.

The Parallel Postulate – Through a point not on a line, there is exactly one line parallel to the given line.

Theorem 18: In a plane, two lines parallel to a third line are parallel to each other.

Theorem 19: Parallel lines form equal corresponding angles.

Corollary 1: Parallel lines form equal alternate interior angles.

Corollary 2: Parallel lines form supplementary interior angles on the same side of a transversal.

Corollary 3: In a plane, a line perpendicular to one of two parallel lines is also perpendicular to the other.

Theorem 20: The Triangle Sum Theorem – The sum of the angles of a triangle is 180° .

Corollary 1: If two angles of one triangle are equal to two angles of another triangle, the third angles are equal.

Corollary 2: The acute angles of a right triangle are complementary.

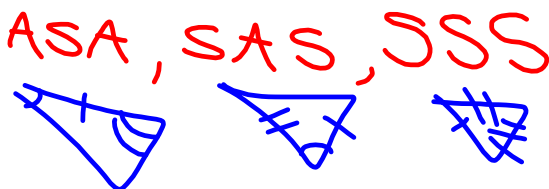
Corollary 3: Each angle of an equilateral triangle is 60° .

Theorem 21: An exterior angle of a triangle is equal to the sum of the remote interior angles.



Theorem 22: The AAS Theorem – If two angles and the side opposite one of them in one triangle are equal to the corresponding parts of another triangle, the triangles are congruent.

Theorem 23: The HL Theorem – If the hypotenuse and a leg of one right triangle are equal to the corresponding parts of another right triangle, the triangles are congruent.



Def: A **diagonal** of a polygon is a line segment that connects any two nonconsecutive vertices.

Theorem 24: **The sum of the angles of a quadrilateral is 360° .**

Def: A **rectangle** is a quadrilateral each of whose angles is a right angle.

Corollary to Theorem 24: **A quadrilateral is equiangular iff it is a rectangle.**

In general, if a polygon has n sides, in terms of n ,

- $n-3$ diagonals can be drawn from one vertex
- these diagonals form $n-2$ triangles
- the sum of the angles of an n -gon is $(n-2)*180^\circ$
- If the n -gon is equiangular, each angle measures $(n-2)*180^\circ/n$

Def: A **parallelogram** is a quadrilateral whose opposite sides are parallel.

A figure has point symmetry if it looks exactly the same when it is rotated about a point.

Def: Two points are **symmetric with respect to a point** iff it is the midpoint of the line segment joining them.

Parallelograms have point symmetry about the point in which their diagonals intersect.

Theorem 25: **The opposite sides and angles of a parallelogram are equal.**

Theorem 26: **The diagonals of a parallelogram bisect each other.**

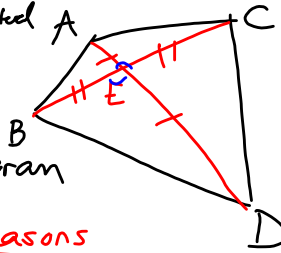
Theorem 27: **A quadrilateral is a parallelogram if its opposite sides are equal.**

Theorem 28: **A quadrilateral is a parallelogram if its opposite angles are equal.**

Theorem 29: **A quadrilateral is a parallelogram if two opposite sides are both parallel and equal.**

Theorem 30: A quadrilateral is a parallelogram if its diagonals bisect each other.

Given: ABCD is a quadrilateral
AD and BC bisect each other



Prove: ABCD is a parallelogram

Proof:

Statements

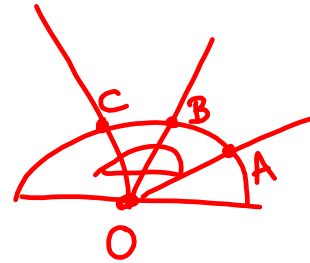
Reasons

- | | |
|---|--|
| 1. ABCD is a quadrilateral
AD & BC bisect each other | Given |
| 2. $\angle AEC = \angle BED$ | Vertical angles |
| 3. $BE = EC$ and $AE = ED$ | bisectors divide line segments into two equal parts |
| 4. $\triangle AEC \cong \triangle DEB$ | SAS congruence |
| 5. $\angle CAE = \angle BDE$ | corresponding parts of congruent triangles are equal |
| 6. $AC \parallel BD$ | equal alternate interior angles means lines are parallel |
| 7. $AC = BD$ | corresponding parts of congruent triangles are equal |
| 8. ABCD is a parallelogram | a quadrilateral is a parallelogram if two opposite sides are both parallel and equal |

Betweenness of Points

Def: $A-B-C$ iff $A < B < C$ or $A > B > C$

Theorem: $AB + BC = AC$



Betweenness of Rays

Def: $OA-OB-OC$ iff $A < B < C$ or $A > B > C$

Theorem: $\angle AOB + \angle BOC = \angle AOC$

[HW #1](#) (submitted Friday, 11/7)

- [Ch 1 Review Problems pp. 36-38](#)
- Start working on Geometry badge on [Khan Academy](#)

[HW #2](#) (submitted Friday, 11/14)

- [Ch 2 Review Problems pp. 71-74](#)
- [Ch 3 Review Problems pp. 124-128](#)
- Khan Academy exercises: "[Introduction to Euclidean geometry](#)," "[Angles and intersecting lines](#)"

[HW #3](#) (submitted Friday, 11/21)

- [Ch 4 Review Problems pp.176-180](#)
- Khan Academy exercises: "[Congruence](#)"

[HW #4](#) (submitted Friday, 12/5)

- [Ch 5 Review Problems pp. 206-209](#)
- Work toward [mastery of practiced Khan Academy exercises](#) in "Introduction to Euclidean Geometry," "Angles and Intersecting Lines," and "Congruence"

[HW #5](#) (submitted Monday, 12/15)

- [Ch 6 Review Problems pp. 250-254](#)

[HW #6](#) (due January)

- [Ch 7 Review Problems pp. 292-295](#)

TEST #2 - WEDNESDAY 12/18