

Theorem 24: The sum of the angles of a quadrilateral is 360° .

Def: A **rectangle** is a quadrilateral each of whose angles is a right angle.

Corollary to Theorem 24: A quadrilateral is equiangular iff it is a rectangle.

Def: A **parallelogram** is a quadrilateral whose opposite sides are parallel.

Theorem 25: The opposite sides and angles of a parallelogram are equal.

Theorem 26: The diagonals of a parallelogram bisect each other.

Theorem 27: A quadrilateral is a parallelogram if its opposite sides are equal.

Theorem 28: A quadrilateral is a parallelogram if its opposite angles are equal.

Theorem 29: A quadrilateral is a parallelogram if two opposite sides are both parallel and equal.

Theorem 30: A quadrilateral is a parallelogram if its diagonals bisect each other.

Def: A **square** is a quadrilateral all of whose sides and angles are equal. Every square is a rhombus.

Def: A **rhombus** is a quadrilateral all of whose sides are equal.

Theorem 31: All rectangles are parallelograms.

Theorem 32: All rhombuses are parallelograms.

Theorem 33: The diagonals of a rectangle are equal.

Theorem 34: The diagonals of a rhombus are perpendicular.

Def: A **regular polygon** is one that is equilateral and equiangular.

Def: A **trapezoid** is a quadrilateral that has exactly one pair of parallel sides. The parallel sides are called the **bases** of the trapezoid, and the non-parallel sides are called its **legs**. The pairs of angles that include each base are called **base angles**.

Def: An **isosceles trapezoid** is a trapezoid whose legs are equal.

Theorem 35: The base angles of an isosceles trapezoid are equal.

Theorem 36: The diagonals of an isosceles trapezoid are equal.

If a quadrilateral is a trapezoid, then its diagonals cannot bisect each other.

7.6 – The Midsegment Theorem

Def: A **midsegment** of a triangle is a line segment that connects the midpoints of two of its sides.

Theorem 37: The Midsegment Theorem –

A midsegment of a triangle is parallel to the third side and half as long.

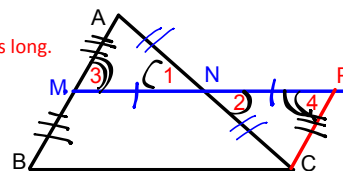
Given: MN is a midsegment of $\triangle ABC$.

Prove: $MN \parallel BC$ and $MN = \frac{1}{2}BC$.

Proof:

Statements

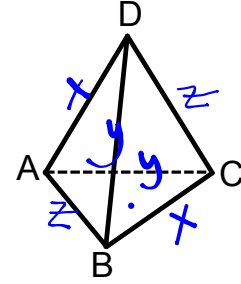
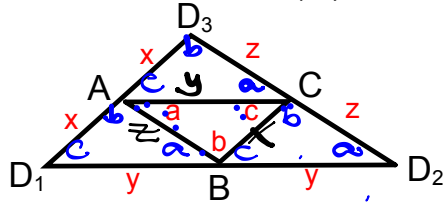
1. Draw line MN
2. Choose a point P so that $NP = MN$
3. $\angle 1 = \angle 2$
4. $AN = NC$
5. $\triangle AMN \cong \triangle CPN$
6. $MA = CP$
7. $BM = MA$
8. $BM = CP$
9. $\angle 3 = \angle 4$
10. $BA \parallel CP$
11. BCPM is a parallelogram
12. $MP \parallel BC$ and $MP = BC$
13. $MP = MN + NP$
14. $MP = MN + MN = 2MN$
15. $MN = \frac{1}{2}MP$
16. $MN = \frac{1}{2}BC$



Reasons

Two points define a line
 Ruler Postulate
 Vertical angles are equal
 N is midpoint of AC & divides it into 2 equal parts
 SAS congruence
 corresponding parts of congruent \triangle s are equal
 M is midpoint of AB & divides it into 2 equal parts
 substitution (#6 & #7)
 corresponding parts of congruent \triangle s are equal
 equal alternate interior \angle s mean lines are parallel
 a pair of opposite sides that is both equal & parallel yields a parallelogram
 A parallelogram has opposite sides equal & parallel
 Betweenness of points theorem
 substitution (#2 & #13)
 Division
 Substitution (#12 & #10)

An edition of Euclid's Elements published in London in 1570 featured little paper models attached to the pages that could be folded up to form three-dimensional figures. One pattern consisted of a triangle and its three midsegments. It could be folded to form a tetrahedron, which is a polyhedron with four triangular faces.



38. What must be true about the four triangles in each figure?

all are congruent by SSS

Two edges of a tetrahedron that do not intersect are called opposite edges; for example, AC and BD are opposite edges.

40. What do you notice about the opposite edges of the tetrahedron?

they have the same lengths

41. What is the sum of the three angles at each vertex of the tetrahedron?

a + b + c = 180°

8.1 – Transformations

Def: A **transformation** is a one-to-one correspondence between two sets of points.

A **translation** slides an object a certain distance without turning it. *(shift)*

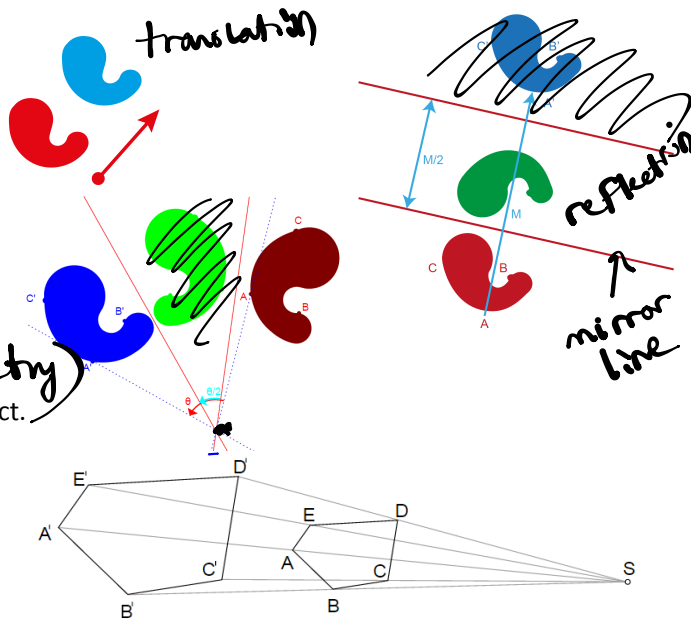
A **reflection** flips an object over a mirror line. *(line symmetry)*

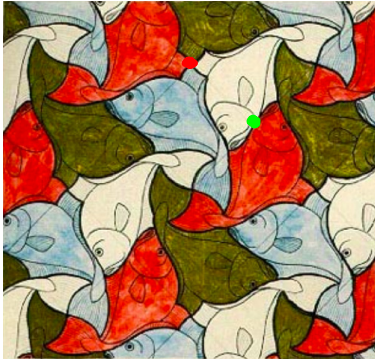
A **rotation** turns an object a certain number of degrees about a fixed point. *(point symmetry)*

A **dilation** enlarges or reduces the size of an object.

Def: an **isometry** is a transformation that preserves distance and angle measure.

Translations, reflections, and rotations are all examples of isometries, but dilations are not.





M.C. Escher. *Fish (No. 20)*

What type of translation seems to relate

1. Two fish of the same color?

translation

2. A pair of red and white fish?

rotation

3. A pair of blue and white fish?

rotation

Are there any pairs of fish in the figure for which one fish of the pair seems to be

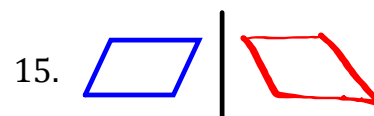
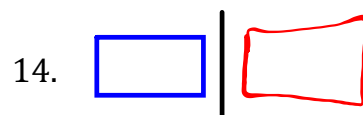
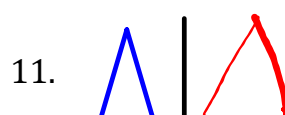
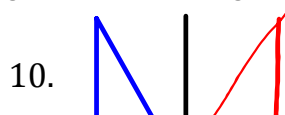
4. A dilation of the other?

nope!

5. A reflection of the other?

no

Complete the figures by including the reflection image of the object through the mirror line.



16. Which figures look the same as their mirror images?

9, 11, 14

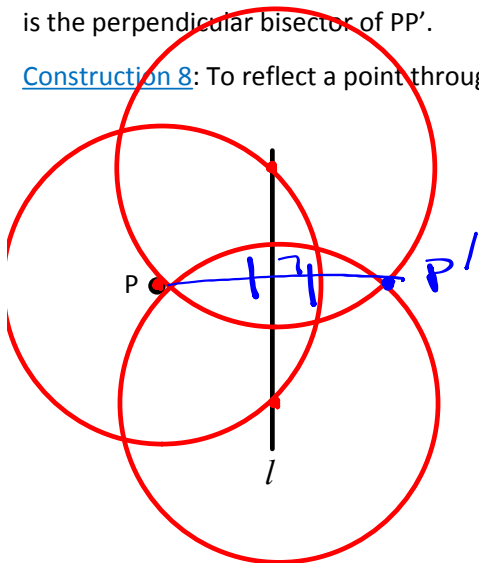
17. What is it about these figures that causes them and their mirror images to look the same?

each figure has mirror symmetry w/rt the figure with respect to a vertical line

8.2 – Reflections

Def: The **reflection** of point P through line l is P itself if P lies on l . Otherwise, it is the point P' such that l is the perpendicular bisector of PP' .

Construction 8: To reflect a point through a line.



HW #1 (submitted Friday, 11/7) - Ch 1 Review Problems pp. 36-38

HW #2 (submitted Friday, 11/14) - Ch 2 Review Problems pp. 71-74, Ch 3 Review Problems pp. 124-128

HW #3 (submitted Friday, 11/21) - Ch 4 Review Problems pp. 176-180

HW #4 (submitted Friday, 12/5) - Ch 5 Review Problems pp. 206-209

HW #5 (submitted Monday, 12/15) - Ch 6 Review Problems pp. 250-254

HW #6 (due Friday, 01/09)

- Ch 7 Review Problems pp. 292-295
- Khan Academy exercises: **anything that has been recommended by me!** ("Introduction to Euclidean geometry," "Angles and intersecting lines," "Congruence," etc.)
- Start working on Ch 8 Review Problems (pp. 325-329)

Quiz #4 - Friday, 01/09!