

- Ch 4 Review Problems pp.176-180 #7-36, 48,51,52 due MONDAY 12/12
- Quiz Wednesday 12/14

- Ch 5 Review Problems pp. 206-209 #15-50
- Ch 6 Review Problems pp. 250-254 #9-19, 33-53

3.7 #44

Given: $\angle 1$ and $\angle 2$ are complementary;
 PB-PC-PD. *PC is between PB & PD*

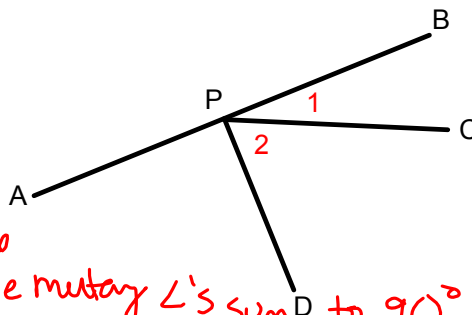
Prove: $AB \perp PD$.

Statements

1. $\angle 1$ and $\angle 2$ are complementary
2. $\angle 1 + \angle 2 = 90^\circ$
3. PB-PC-PD
4. $\angle BPD = \angle 1 + \angle 2$
5. $\angle BPD = 90^\circ$
6. $\angle BPD$ is a right angle
7. *$AB \perp PD$*

Reasons

Given
 complementary \angle 's sum to 90°
Given
 Betweenness of Rays Theorem
 Substitution (#2 & #4)
 right \angle 's measure 90°
 perpendicular lines meet @ right \angle 's

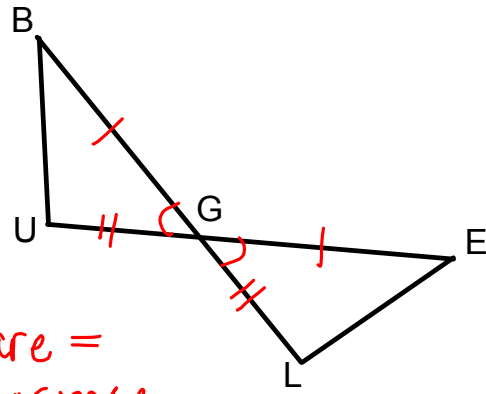


4.4 #31

Given: $\angle BGU$ and $\angle EGL$ are vertical angles;
 $BG=GE$ and $UG=GL$

Prove: $BU=LE$

1. $\angle BGU$ & $\angle EGL$ are vertical \angle 's
 $BG=GE, UG=GL$
2. $\angle BGU = \angle EGL$
3. $\triangle BGU \cong \triangle EGL$
4. $BU=LE$



Given
 Vertical \angle 's are =
 SAS congruence
 Corresponding parts of congruent
 \triangle 's are equal

5.1 – Properties of Inequality

a, b, c – real #'s

Algebraic Axioms:

The “Three Possibilities” Property: either $a > b$, $a = b$, or $a < b$

The Transitive Property: If $a > b$ and $b > c$, then $a > c$

The Addition Property: If $a > b$, then $a + c > b + c$

The Subtraction Property: If $a > b$, then $a - c > b - c$

The Multiplication Property: If $a > b$ and $c > 0$, then $ac > bc$

The Division Property: If $a > b$ and $c > 0$, then $a/c > b/c$

The Addition Theorem of Inequality: If $a > b$ and $c > d$, then $a + c > b + d$

Proof:

Statements

Reasons

1. $a > b$

Given

2. $a + c > b + c$

Addition Property (Axiom/Postulate) of Inequality

3. $c > d$

Given

4. $b + c > b + d$

Addition Property of Inequality

5. $a + c > b + d$

Transitive Property of Inequality

The "Whole Greater than Part" Theorem: If $a > 0$, $b > 0$, and $a + b = c$, then $c > a$ and $c > b$

Proof:

Statements

Reasons

1. $a > 0$ and $b > 0$

Given

$+b + b$ $+a + a$

2. $a + b > b$ and $a + b > a$

Addition Property of Inequality

3. $a + b = c$

Given

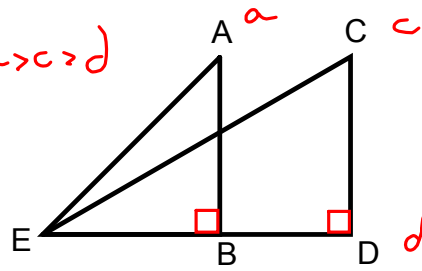
4. $c > b$ and $c > a$

Substitution (#3 into #2)

47.

Given: $AB=CD$; $EA-EC-ED$
 Prove: $AED > CED$

iff $a < c < d$ or $a > c > d$



Proof:

Statements

Reasons

1. $EA-EC-ED$

Given

2. $AED = AEC + CED$

Betweenness of Rays Theorem

3. $AEC > 0$

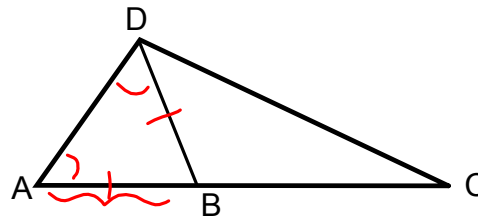
Betweenness of Rays Def'n & Protractor Postulate

4. $AED > CED$

Whole Greater than Part

48.

Given: $A-B-C$; $\angle ADB = \angle DAB$
 Prove: $AC > DB$



Proof:

Statements:

Reasons:

1. $A-B-C$, $\angle ADB = \angle DAB$

Given

2. $AB = DB$

If 2 \angle s in a Δ are $=$, the sides opposite them are $=$

3. $AB + BC = AC$

Betweenness of Points Theorem

4. $DB + BC = AC$

Substitution (#2 & 3)

5. $AC > DB$

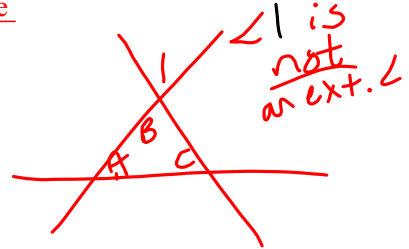
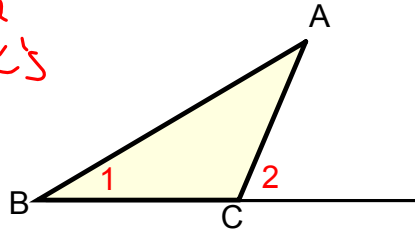
Whole Greater than Part

5.2 – The Exterior Angle Theorem

Def: An exterior angle of a triangle is an angle that forms a linear pair with an angle of the triangle.

In $\triangle ABC$, exterior $\angle 2$ forms a linear pair with $\angle ACB$.
 The other two angles of the triangle, $\angle 1$ ($\angle B$) and $\angle A$ are called remote interior angles with respect to $\angle 2$.

$\angle B$ & $\angle A$ are the remote interior \angle 's w.r.t. $\angle 2$



Theorem 12: The Exterior Angle Theorem

An Exterior angle of a triangle is greater than either remote interior angle.

Given: $\angle ACD$ is an exterior angle of $\triangle ABC$.
 Prove: $\angle ACD > \angle A$ and $\angle ACD > \angle B$

Proof:

Statements

1. $\angle ACD$ is an exterior angle of $\triangle ABC$
2. Let M be the midpoint of AC
3. $AM = MC$
4. Draw line BM
5. Choose P on line BM so that $MB = MP$
6. Draw CP
7. $\angle AMB = \angle CMP$
8. $\triangle AMB \cong \triangle CMP$
9. $\angle A = \angle 3$
10. $\angle ACD = \angle 3 + \angle 4$
11. $\angle ACD > \angle 3$
12. $\angle ACD > \angle A$

Reasons

Given
 Ruler postulate & uniqueness of midpoint
 Def. of midpoint / midpoint divides segments into 2 equal parts
 2 points define a line
 Ruler Postulate
 2 pts define a line
 vertical \angle 's are equal
 SAS congruence
 Corresponding parts of $\cong \Delta$'s are $=$
 Betweenness of Rays Theorem
 Whole greater than part
 Subst. (#9 & 11)

