

- Ch 5 Review Problems pp. 206-209 #15-50 due FRIDAY 01/06
- TEST #2 - Wednesday 01/11
 - > mostly Ch 4-5
 - > some review of Ch 1-3
 - > Vocab from Ch 6 through Theorem 21

- Ch 6 Review Problems pp. 250-254 #9-19, 33-53

due Fri 01/13

Theorem 17: Equal corresponding angles mean that lines are parallel.

Corollary 1: Equal alternate interior angles mean that lines are parallel.

Corollary 2: Supplementary interior angles on the same side of a transversal mean that lines are parallel.

Corollary 3: In a plane, two lines perpendicular to a third line are parallel.

The Parallel Postulate – Through a point not on a line, there is exactly one line parallel to the given line.

Theorem 18: In a plane, two lines parallel to a third line are parallel to each other.

Theorem 19: Parallel lines form equal corresponding angles.

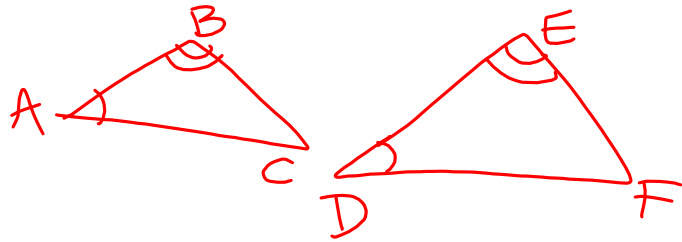
Corollary 1: Parallel lines form equal alternate interior angles.

Corollary 2: Parallel lines form supplementary interior angles on the same side of a transversal.

Corollary 3: In a plane, a line perpendicular to one of two parallel lines is also perpendicular to the other.

Theorem 20: The Angle Sum Theorem – The sum of the angles of a triangle is 180° .

Corollary 1: If two angles of one triangle are equal to two angles of another triangle, the third angles are equal.



Given: $\angle A = \angle D$
 $\angle B = \angle E$

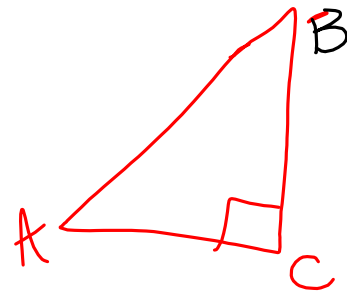
To Prove: $\angle C = \angle F$

Proof

1. $\angle A = \angle D, \angle B = \angle E$
2. $\angle A + \angle B + \angle C = 180^\circ$
 $\angle D + \angle E + \angle F = 180^\circ$
3. $\angle C = 180^\circ - \angle A - \angle B$
 $\angle F = 180^\circ - \angle D - \angle E$
4. $\angle C = 180^\circ - \angle D - \angle E$
5. $\angle C = \angle F$

Given
 Triangle sum Theorem
 subtraction property of equality
 substitution (#1 into #3)
 substitution (#4 into #3)

Corollary 2: The acute angles of a right triangle are complementary.



Given: $\triangle ABC$ is a right \triangle
 with right angle C

To Prove: $\angle A$ and $\angle B$ are complementary

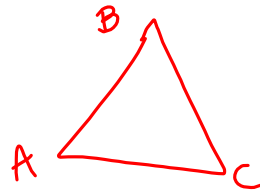
Proof:

1. $\triangle ABC$ is a right \triangle
 $\angle C$ is a right \angle
2. $\angle A + \angle B + \angle C = 180^\circ$
3. $\angle C = 90^\circ$
4. $\angle A + \angle B + 90^\circ = 180^\circ$
5. $\angle A + \angle B = 90^\circ$
6. $\angle A$ and $\angle B$ are complimentary

Given
 Triangle Sum Theorem
 Right \angle 's measure 90°
 substitution
 subtraction
 complimentary \angle 's sum to 90°

Corollary 3: Each angle of an equilateral triangle is 60° .

Given: $\triangle ABC$ is equilateral
 To Prove: $\angle A = \angle B = \angle C = 60^\circ$



Proof:

1. $\triangle ABC$ is equilateral
2. $\triangle ABC$ is equiangular
 $\angle A = \angle B = \angle C$
3. $\angle A + \angle B + \angle C = 180^\circ$
4. $\angle A + \angle A + \angle A = 180^\circ$
 $3\angle A = 180^\circ$
5. $\angle A = 60^\circ$
6. $\angle B = \angle C = 60^\circ$

Given
 Equilateral \triangle 's are equiangular
 Triangle Sum Theorem
 Substitution
 (& simplification)
 Division Property of
 Equality
 Substitution

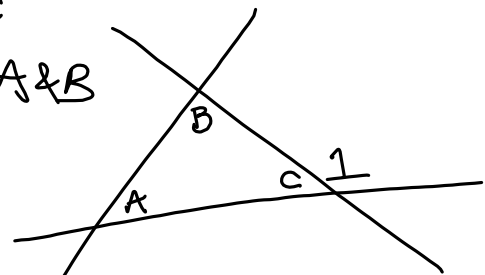
Theorem 21: An exterior angle of a triangle is equal to the sum of the remote interior angles.

Given: $\angle 1$ is an exterior angle of $\triangle ABC$ w/ remote interior \angle 's A & B

To Prove: $\angle 1 = \angle A + \angle B$

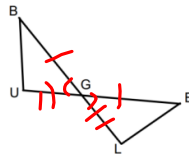
PROOF:

1. $\angle 1$ is an exterior angle of $\triangle ABC$
2. $\angle 1$ and $\angle C$ form a linear pair
3. $\angle 1$ and $\angle C$ are supplementary
4. $\angle 1 + \angle C = 180^\circ$
5. $\angle A + \angle B + \angle C = 180^\circ$
6. $\angle 1 + \angle C = \angle A + \angle B + \angle C$
7. $\angle 1 = \angle A + \angle B$



Given
 Def. of exterior angle
 \angle 's in a linear pair are suppl.
 Suppl. \angle 's sum to 180° .
 Triangle Sum Theorem
 Substitution
 Subtraction

Given: $\angle BGU$ and $\angle EGL$ are vertical angles;
 $BG=GE$;
 $UG=GL$.



Prove: $BU=LE$

Statements:

27. $BG=GE, UG=GL$

28. $\angle BGU$ & $\angle EGL$ are vertical \angle 's

29. $\angle BGU = \angle EGL$

30. $\triangle BGU \cong \triangle EGL$

31. $BU=EL$

Reasons:

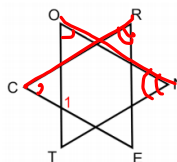
Given

Given
 vertical \angle 's are equal

SAS Congruence

corcesponding parts of congruent \triangle 's are equal

Given: $\angle C = \angle O$;
 $\angle R$ and $\angle N$ are supplements of $\angle 1$;
 $CR = ON$.



Prove: $\triangle CRE \cong \triangle ONT$.

Statements:

32. $\angle C = \angle O; CR = ON$

33. $\angle R$ & $\angle N$ are supplements of $\angle 1$

34. $\angle R + \angle 1 = 180^\circ$

35. $\angle N + \angle 1 = 180^\circ$

36. $\angle R + \angle 1 = \angle N + \angle 1$

37. $\angle R = \angle N$

38. $\triangle CRE \cong \triangle ONT$

Reasons:

given

Given

Supplementary angles sum to 180°

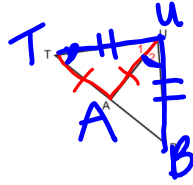
Supplementary angles sum to 180°

Substitution

subtraction by $\angle 1$

ASA congruence

Given: $\angle T$ and $\angle 2$ are complements of $\angle 1$;
 $TA=AU$;
 $TU=UB$.



Prove: $AU=AB$.

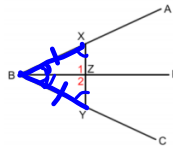
Statements:

- 39. $TA=AU$; $TU=UB$
- 40. $\angle T$ & $\angle 2$ are complements of $\angle 1$
- 41. $\angle T + \angle 1 = 90^\circ$
- 42. $\angle 2 + \angle 1 = 90^\circ$
- 43. $\angle T + \angle 1 = \angle 2 + \angle 1$
- 44. $\angle T = \angle 2$
- 45. $\triangle ATU \cong \triangle AUB$
- 46. $AU = AB$

Reasons:

- Given
- Given
- Complementary angles sum to 90°
- Complementary angles sum to 90°
- Substitution
- Subtraction
- SAS
- Corresponding parts of congruent triangles are equal.

Given: BP bisects $\angle ABC$;
 $BX=BY$;
 $\angle 1$ and $\angle 2$ form a linear pair.



Prove: $XY \perp BP$.

Statements:

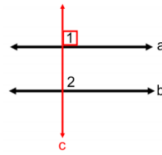
- 47. $BX=BY$
- 48. $\angle BXZ = \angle BYZ$
- 49. BP bisects $\angle ABC$
- 50. $\angle CBP = \angle ABP$
- 51. $\triangle BXZ \cong \triangle BYZ$
- 52. $\angle 1 = \angle 2$
- 53. $\angle 1$ and $\angle 2$ form a linear pair
- 54. $XY \perp BP$

Reasons:

- Given
- If two sides of a triangle are equal, the angles opposite them are equal.
- Given
- angle bisector divides an angle into 2 equal parts
- ASA congruence
- Corresponding parts of congruent \triangle 's are equal
- Given
- If \angle 's in a linear pair are equal, then their sides are perpendicular.

Theorem: In a plane, a line perpendicular to one of two parallel lines is also perpendicular to the other.

Given: $c \perp a$ and $a \parallel b$
 Prove: $c \perp b$



Statements

$c \perp a$

31. $\angle 1$ is a right angle
 $\angle 1 = 90^\circ$

32. $a \parallel b$
 $\angle 1 = \angle 2$

34. $\angle 2 = 90^\circ$

35. $\angle 2$ is a right angle

36. $c \perp b$

Reasons

Given

perpendicular lines form right \angle 's

Right angles measure 90°

Given

Parallel lines form equal corresponding angles

substitution

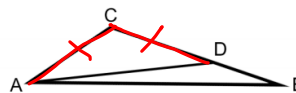
right \angle 's are equal

perpendicular lines meet @ right \angle 's

Theorem: If two sides of a triangle are unequal, the angles opposite them are unequal in the same order.

Given: $\triangle ABC$ with $BC > AC$

42. Prove: $\angle BAC > \angle B$



Statements

$\triangle ABC$ with $BC > AC$

Choose D on CB so that $CD = CA$

43. Draw AD
 $\angle CAD = \angle CDA$

45. $\angle CAB = \angle CAD + \angle DAB$

46. $\angle CAB > \angle CAD$

$\angle CAB > \angle CDA$

47. $\angle CDA > \angle B$

48. $\angle CAB > \angle B$

Reasons

Given

Ruler Postulate

2 points define a line

If two sides of a triangle are equal, the angles opposite them are equal.

Betweenness of Rays Theorem

Whole greater than part

Substitution

ext. \angle is greater than either remote int. \angle

Transitive