

Due Friday, 3/31:

12.4 p. 508 #35-42

12.5 p. 513 #22-38

12.6 p. 518 #11-15

Ch 12 Review pp. 523-524 #9-16; p. 525 #45-50; p. 526 #55-61

QUIZ - FRIDAY

Chapter 12: Circles

Def: A **circle** is the set of all points in a plane that are at a given distance from a given point in the plane.

Def: Circles are **concentric** iff they lie in the same plane and have the same center.

Def: A **radius** of a circle is a line segment that connects the center of the circle to any point on it.
The radius of a circle is the length of one of these line segments.

Corollary: All radii of a circle are equal.

Def: A **chord** of a circle is a line segment that connects two points of the circle.

Theorem 56: If a line through the center of a circle is perpendicular to a chord, it also bisects the chord.

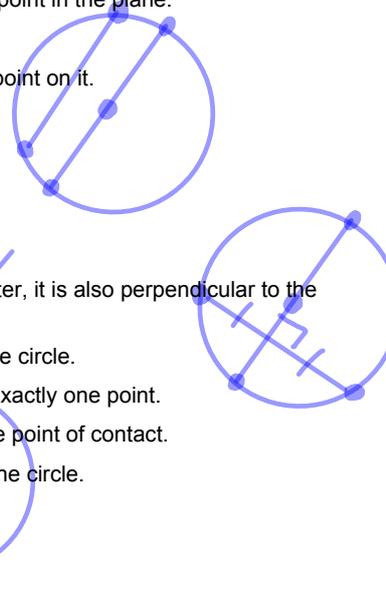
Theorem 57: If a line through the center of a circle bisects a chord that is not a diameter, it is also perpendicular to the chord.

Theorem 58: The perpendicular bisector of a chord of a circle contains the center of the circle.

Def: A **tangent** to a circle is a line in the plane of the circle that intersects the circle in exactly one point.

Theorem 59: If a line is tangent to a circle, it is perpendicular to the radius drawn to the point of contact.

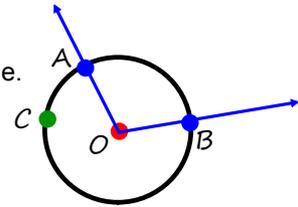
Theorem 60: If a line is perpendicular to a radius at its outer endpoint, it is tangent to the circle.



Def: A **central angle** of a circle is an angle whose vertex is the center of the circle.

Def: A **reflex angle** is an angle whose measure is more than 180°

Def: The **degree measure** of an arc is the measure of its central angle.



$\angle AOB$ is a central angle

\widehat{AB} is the minor arc

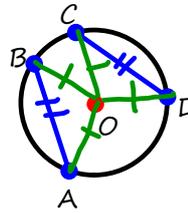
\widehat{ACB} is the major arc

Postulate 10: The Arc Addition Postulate

If C is on \widehat{AB} , then $m\widehat{AC} + m\widehat{CB} = m\widehat{ACB}$

Theorem 61: In a circle, equal chords have equal arcs.

Theorem 62: In a circle, equal arcs have equal chords.

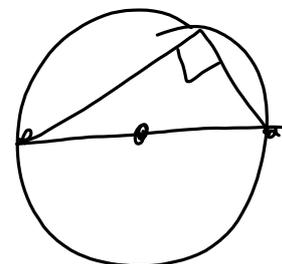
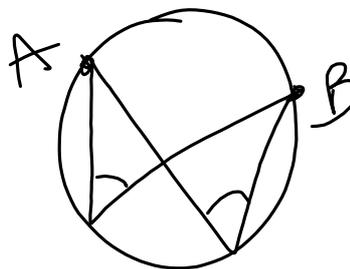
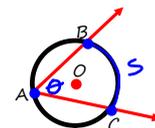


Def: An **inscribed angle** is an angle whose vertex is on a circle, with each of the angle's sides intersecting the circle in another point.

Theorem 63: An inscribed angle is equal in measure to half its intercepted arc.

Corollary 1 to Theorem 63: Inscribed angles that intercept the same arc are equal.

Corollary 2 to Theorem 63: An angle inscribed in a semicircle is a right angle.

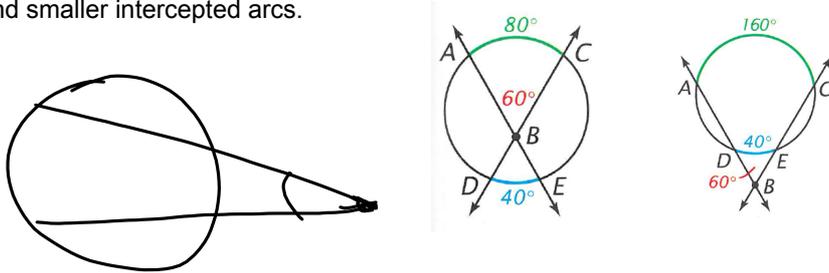


Def: A **secant** is a line that intersects a circle in two points.

Def: A **secant angle** is an angle whose sides are contained in two secants of a circle so that each side intersects the circle in at least one point other than the angle's vertex.

Theorem 64: A secant angle whose vertex is inside a circle is equal in measure to half the sum of the arcs intercepted by it and its vertical angle.

Theorem 65: A secant angle whose vertex is outside a circle is equal in measure to half the difference of its larger and smaller intercepted arcs.



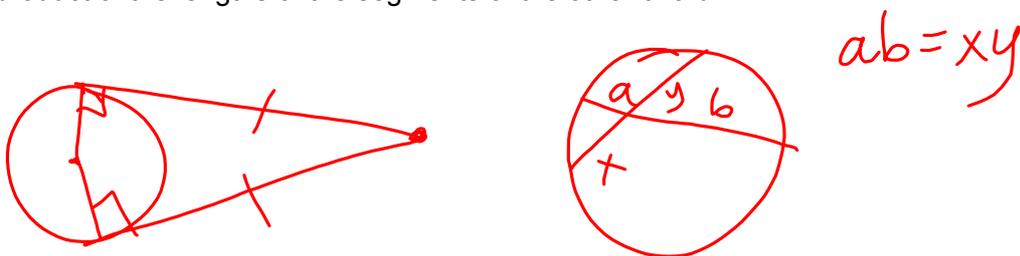
12.6 - Tangent Segments and Intersecting Chords

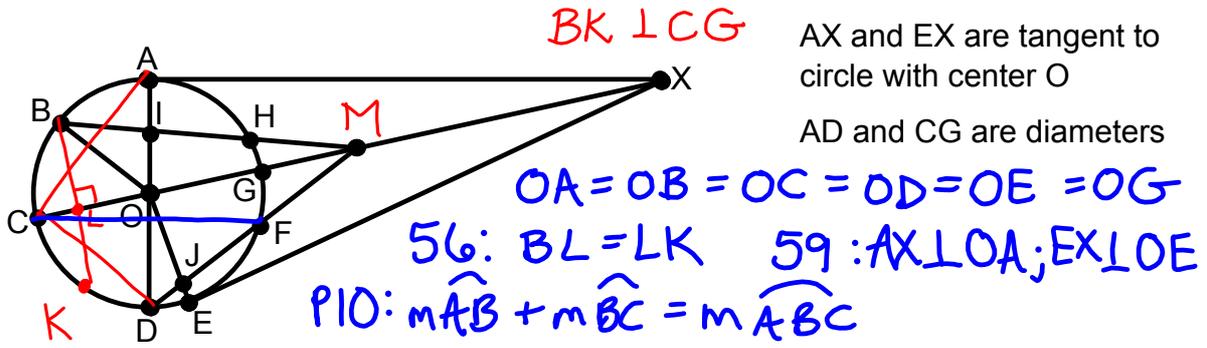
Def: If a line is tangent to a circle, then any segment of the line having the point of tangency as one of its endpoints is a **tangent segment** to the circle.

Theorem 66: The tangent segments to a circle from an external point are equal.

Theorem 67: The Intersecting Chords Theorem

If two chords intersect in a circle, the product of the lengths of the segments of one chord is equal to the product of the lengths of the segments of the other chord.





AX and EX are tangent to circle with center O
AD and CG are diameters

$OA = OB = OC = OD = OE = OG$

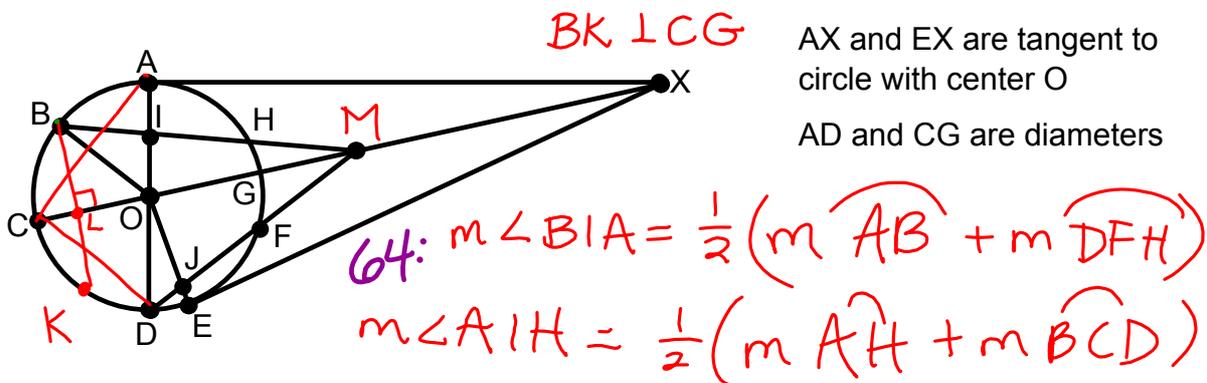
56: $BL = LK$ 59: $AX \perp OA; EX \perp OE$

P10: $m\widehat{AB} + m\widehat{BC} = m\widehat{ABC}$

61: $AD = CG \Rightarrow m\widehat{ACD} = m\widehat{CAG}$

63: $m\angle ADF = \frac{1}{2} m\widehat{AHF}$

cor 1: $m\angle ACF = m\angle ADF$ cor 2: $\angle ACD = 90^\circ$



AX and EX are tangent to circle with center O
AD and CG are diameters

$BK \perp CG$

64: $m\angle BIA = \frac{1}{2} (m\widehat{AB} + m\widehat{DFH})$

$m\angle AIH = \frac{1}{2} (m\widehat{AH} + m\widehat{BCD})$

65: $m\angle BMD = \frac{1}{2} (m\widehat{BCD} - m\widehat{HGF})$

66: $AX = EX$

67: $(BI)(IH) = (AI)(ID)$

Ch 13 - The Concurrence Theorems

13.1 - Triangles and Circles

Def: A polygon is **cyclic** iff there exists a circle that contains all of its vertices.

Theorem 68: Every Triangle is cyclic.

Def: A polygon is **inscribed in a circle** iff each vertex of the polygon lies on the circle. The circle is **circumscribed about the polygon**.

Corollary to Theorem 68: The perpendicular bisectors of the sides of a triangle are concurrent.

Construction 9: To circumscribe a circle about a triangle.

