

4.2

19.  $\left[ \begin{array}{cc|c} 4 & 4 & 5 \\ 2 & -8 & -5 \end{array} \right] \xrightarrow{\text{interchange } R_1 \times R_2 \cdot \frac{1}{2}}$   $\left[ \begin{array}{cc|c} 1 & -4 & -5/2 \\ 4 & 4 & 5 \end{array} \right]$

$R_2 - 4R_1 \rightarrow \left[ \begin{array}{cc|c} 1 & -4 & -5/2 \\ 0 & 20 & 15 \end{array} \right] \rightarrow \left[ \begin{array}{cc|c} 1 & -4 & -5/2 \\ 0 & 1 & 3/4 \end{array} \right]$

$5 - 4(-5/2) \quad -5/2 + 4(3/4)$

$R_1 + 4R_2 \rightarrow \left[ \begin{array}{cc|c} 1 & 0 & 1/2 \\ 0 & 1 & 3/4 \end{array} \right] \quad \left( \begin{array}{c} 1/2 \\ 3/4 \end{array} \right)$

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$\left[ \begin{array}{cc|c} a & b & c \\ d & e & f \end{array} \right] \xrightarrow{R_1 \cdot \frac{1}{a}} \left[ \begin{array}{cc|c} 1 & b/a & c/a \\ d & e & f \end{array} \right]$

$R_2 - d \cdot R_1 \rightarrow \left[ \begin{array}{cc|c} 1 & b/a & c/a \\ 0 & e - \frac{db}{a} & f - \frac{dc}{a} \end{array} \right] \xrightarrow{R_2 \cdot \frac{1}{e - \frac{db}{a}}} \left[ \begin{array}{cc|c} 1 & b/a & c/a \\ 0 & 1 & \frac{f - \frac{dc}{a}}{e - \frac{db}{a}} \end{array} \right]$

$\left[ \begin{array}{cc|c} 1 & b/a & c/a \\ 0 & 1 & \frac{f - \frac{dc}{a}}{e - \frac{db}{a}} \end{array} \right] \xrightarrow{R_1 - \frac{b}{a}R_2} \left[ \begin{array}{cc|c} 1 & 0 & \frac{c}{a} - \frac{b}{a} \left( \frac{f - \frac{dc}{a}}{e - \frac{db}{a}} \right) \\ 0 & 1 & \frac{f - \frac{dc}{a}}{e - \frac{db}{a}} \end{array} \right]$

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$$\begin{array}{l}
 15. \begin{cases} 2y+z=7 \\ 2x-z=3 \end{cases} \\
 2. \quad (x-y=3) \\
 \\
 2x-2y=6 \\
 2x+2y=10 \\
 \hline
 4x=16 \\
 x=4 \\
 \\
 2y+z=7 \\
 2x-z=3 \\
 \hline
 2x+2y=10 \\
 \\
 4-y=3 \\
 -y=-1 \\
 y=1 \\
 2(1)+z=7 \\
 z=5 \\
 \\
 (4, 1, 5)
 \end{array}$$

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5.1 Exponential Expressions

$$X^n = \underbrace{X \cdot X \cdot \dots \cdot X}_{n \text{ times}}$$

$m, n, p \in \mathbb{Z}$

$$X^m X^n = X^{m+n} \qquad (X^m)^n = X^{mn}$$

$$\frac{X^m}{X^n} = X^{m-n} \qquad (X^m y^n)^p = (X^m)^p (y^n)^p = X^{mp} y^{np}$$

$$= \frac{1}{X^{n-m}}$$

$$\left(\frac{X^m}{y^n}\right)^p = \frac{X^{mp}}{y^{np}}, y \neq 0$$

$X^0 = 1, X \neq 0$

$$\frac{1}{X^n} = X^{-n}, \quad \frac{1}{X^{-n}} = X^n, X \neq 0$$

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Simplify

- one instance of each variable
- no negative exponents

$$4. (-2ab^4)(-3a^2b^4) = (-2)(-3)a^2b^4b^4 \\ = \boxed{6a^3b^8}$$

$$20. [(3x^2y^3)^2]^2 = [9x^4y^6]^2 = \boxed{81x^8y^{12}}$$

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$$66. \frac{6a^2b^3}{3ab^4} = \frac{3b}{3} \cdot \frac{a^{-2}}{a^1} \cdot \frac{b^3}{b^4}$$

$$\frac{x^m}{x^n} = \frac{x^{m-n}}{1} = \frac{1}{x^{n-m}} = \frac{12}{1} \cdot \frac{1}{a^{1-(-2)}} \cdot \frac{1}{b^{4-3}}$$

$$= \boxed{\frac{12}{a^3b}}$$

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72.  $\left(\frac{x^{-3}y^{-4}}{x^2y^1}\right)^{-2} = \left(\frac{1}{x^{-2-(-3)}y^{1-(-4)}}\right)^{-2}$

$= \left(\frac{1}{xy^5}\right)^{-2} = \frac{1}{x^{-2}y^{-10}} = \boxed{x^2y^{10}}$

$\frac{x^6y^8}{x^4y^2} = x^2y^6$        $\frac{1}{x^n} = x^{-n}$   
 $\frac{1}{x^{-n}} = x^n$

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80.  $\left(\frac{4^{-2}xy^{-3}}{x^{-3}y}\right)^3 \left(\frac{8^{-1}x^{-2}y}{x^7y^{-1}}\right)^{-2}$

$= \left(\frac{x^7}{16y^7}\right)^3 \left(\frac{y^2}{8x^6}\right)^{-2}$

$= \frac{x^{21}}{2^{12}y^{21}} \cdot \frac{y^{-4}}{2^{-6}x^{12}} = \frac{x^{24}}{2^6y^{16}} = \frac{x}{64y^{16}}$

5.1  
 #63-85  
 odd  
 quiz on rates  
 (p257)<sup>24</sup>

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