

Review: multiply the polynomials.

$$(a-b)(a+b) = a^2 - b^2$$

$$(a+b)(a+b) = a^2 + 2ab + b^2$$

$$(a-b)(a-b) = a^2 - 2ab + b^2$$

$$(a+b)(a^2 - ab + b^2) = a^3 + b^3$$

$$(a-b)(a^2 + ab + b^2) = a^3 - b^3$$

$$a^3 + \cancel{a^2b} + \cancel{ab^2} - \cancel{a^2b} - \cancel{ab^2} - b^3$$

HW Questions?

5.5

$$33. \quad \underbrace{xy + 4y}_{y(x+4)} - \underbrace{2x - 8}_{-2(x+4)}$$

$$y(x+4) - 2(x+4)$$

$$(x+4)(y-2)$$

$$\begin{aligned}
 29. & \quad a(x-2) - b(2-x) \\
 & \quad \left(a(x-2) + b(x-2) \right) \\
 & \quad \rightarrow a(x-2) - 2b + xb \\
 & \quad a(x-2) + xb - 2b \\
 & \quad \quad + b(x-2)
 \end{aligned}$$

$$(x-2)(a+b)$$

$$\begin{aligned}
 25. & \quad y^{2n+2} + y^{n+2} - y^2 \\
 & \quad y^2(y^{2n} + y^n - 1) \\
 & \quad y^2 y^n
 \end{aligned}$$

5.5

factoring trinomials of the form

$$ax^2 + bx + c$$

when $a=1$, we look for factors
of c that sum to b

when $a \neq 1$, we will look for
factors of $c \cdot a$ that sum to b ,
rewrite bx as a sum of 2 terms,
and factor by grouping

$$80. \quad 6y^2 + 5y - 6$$

factors of $6(-6) = -36$ that sum to 5
 $(-4)(9)$

$$6y^2 - 4y + 9y - 6$$

$$2y(3y-2) + 3(3y-2)$$

$$(3y-2)(2y+3)$$

$$2yx + 3x \\ x(2y+3)$$

$$88. 4a^2 - a - 5$$

factors of $4(-5)$ that sum to -1

$$4a^2 + 4a - 5a - 5$$

$$4a(a+1) - 5(a+1)$$

$$(a+1)(4a-5)$$

$$100. 6x^2 + 41xy - 7y^2$$

$$6(-7) = -42 = 42(-1)$$

$$6x^2 + 42xy - xy - 7y^2$$

$$6x(x+7y) - y(x+7y)$$

$$(x+7y)(6x-y)$$

$$106. \quad 6 - 7x - 5x^2 = -1(5x^2 + 7x - 6)$$

$$6(-5) = -30 = (-10) \cdot 3 = -1(5x-3)(x+2)$$

$$6 - 10x + 3x - 5x^2$$

$$2(3 - 5x) + x(3 - 5x)$$

$$(3 - 5x)(2 + x)$$

$$114. \quad 8a^4 + 37ab^3 - 15a^2b^2$$

$$8(-15) = -2 \cdot 2 \cdot 2 \cdot 3 \cdot 5 = (2 \cdot 2 \cdot 2 \cdot 5)(-3)$$

$$= -120$$

$$= 10(-12)$$

$$= 40(-3)$$

$$= 60(-2)$$

$$\begin{array}{r} 12 \cdot 10 \\ 5 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \\ 6 \cdot 20 \\ 24 \cdot 5 \\ 40 \cdot 3 \end{array}$$

$$8a^4 + 40a^3b - 3a^2b^2 - 15a^2b^2$$

$$8a^3(a+5b) - 3a^2b(a+5b)$$

$$(a+5b)(8a^3 - 3a^2b)$$

$$(a+5b)(8a-3b) \cdot a^2$$

$$a^2(a+5b)(8a-3b)$$

$$122. \quad 2a^2b^4 + 9ab^3 - 18b^2$$

$$b^2(2a^2b^2 + 9ab - 18)$$

$$2(-18) = -36 = (12)(-3)$$

$$b^2(2a^2b^2 + 12ab - 3ab - 18)$$

$$b^2[2ab(ab+6) - 3(ab+6)]$$

$$b^2(ab+6)(2ab-3)$$

$$136. \quad X^{3n} + 10X^{2n} + 16X^n$$

$$X^n(X^{2n} + 10X^n + 16)$$

$$X^n(X^n + 8)(X^n + 2)$$

$$\rightarrow X^n(X^{2n} + 8X^n + 2X^n + 16)$$

$$X^n(X^n(X^n + 8) + 2(X^n + 8))$$

$$X^n(X^n + 8)(X^n + 2)$$

$$X^n(X^n + 8)(X^n + 2)$$

$$96. \quad 10x^2 - 29x + 10$$

$$10(10) = 100 = (-25)(-4)$$

$$10x^2 - 25x - 4x + 10$$

$$5x(2x-5) - 2(2x-5)$$

$$(2x-5)(5x-2)$$

$$98. \quad 4x^2 - 6x + 1$$

$$4(1) = 4$$

$$-4(-1)$$

$$(-2)(-2)$$

$$2 \cdot 2$$

not factorable!

5.5

79-

137 odd