

Quiz Solutions:

$$1. 7x^3 + 8x^2 - 6x - 7$$

$$2. 7x^3 + 2x^2 - 2x + 1$$

$$3. -15x^4 + 22x^3 + 12x^2 - 16x$$

$$4. Q: 3x - 5; R: 9$$

$$5. f(-2) = -4$$

5.6

Special Factoring

$$a^2 - b^2 = (a+b)(a-b)$$

$$a^2 + 2ab + b^2 = (a+b)(a+b) = (a+b)^2$$

$$a^2 - 2ab + b^2 = (a-b)(a-b) = (a-b)^2$$

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

$$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$

$$\frac{5.6}{12} \cdot a^2 b^2 - 25$$

$$(ab)^2 - 5^2$$

$$(ab - 5)(ab + 5)$$

$$42. 64a^3 + 27$$

$$(4a)^3 + 3^3$$

$$(4a + 3)(16a^2 - 12a + 9)$$

$$(4a)^2 - (4a)(3) + 3^2$$

$$\begin{array}{l} x^3 + y^3 \\ x = 4a; y = 3 \\ (x+y)(x^2 - xy + y^2) \end{array}$$

$$16. 4x^2y^2 + 12xy + 9$$

$$a^2 + 2ab + b^2 = (a+b)^2$$

$$(2xy)^2 + 2(2xy)(3) + 3^2 = (2xy + 3)^2$$

$$22. b^2 - 18b + 81$$

$$= (b - 9)^2$$

$$48. 1 - 125b^3$$

$$1^3 - (5b)^3$$

$$(1 - 5b)(1^2 + (1)(5b) + (5b)^2)$$

$$(1 - 5b)(1 + 5b + 25b^2)$$

$$(a - b)(a^2 + ab + b^2)$$

$$54. 27x^3 - 8y^3 = (3x)^3 - (2y)^3$$

$$(3x - 2y)(9x^2 + 6xy + 4y^2)$$

$$58. a^3 + (a+b)^3$$

$$(a + a+b)(a^2 - a(a+b) + (a+b)^2)$$

$$(2a+b)(\cancel{a^2} - \cancel{a^2} - ab + a^2 + 2ab + b^2)$$

$$(2a+b)(a^2 + ab + b^2)$$

$$60. X^{3n} + Y^{3n}$$

$$(X^n)^3 + (Y^n)^3$$

$$(X^n + Y^n)(X^{2n} - X^n Y^n + Y^{2n})$$

$$86. 3x^4 - 81x = 3x(x^3 - 27)$$

$$3x(x-3)(x^2 + 3x + 9)$$

$$102. \underline{4x^3 + 8x^2} - \underline{9x - 18}$$

$$4x^2(x+2) - 9(x+2)$$

$$(x+2)(4x^2 - 9)$$

$$(x+2)(2x+3)(2x-3)$$

$$108. 8x^4 - 40x^3 + 50x^2$$

$$2x^2(4x^2 - 20x + 25)$$

$$(2x)^2 - 2(2x)(5) + 5^2 = (2x-5)^2$$

$$2x^2(2x-5)^2$$

$$120. 24a^2b^2 - 14ab^3 - 90b^4$$

$$2b^2(12a^2 - 7ab - 45b^2)$$

$$2b^2(12a^2 - 27ab + 20ab - 45b^2) \quad 12(-45)$$

$$2b^2[3a(4a-9b) + 5b(4a-9b)] \quad \begin{matrix} 3 \cdot 4 \cdot 9 \cdot 5 \\ 3 \cdot 2 \cdot 2 \cdot 3 \cdot 3 \cdot 5 \end{matrix}$$

$$2b^2(4a-9b)(3a+5b)$$

$$126. \quad \underbrace{4x^4 - x^2} - \underbrace{4x^2y^2 + y^2}$$

$$x^2(4x^2 - 1) - y^2(4x^2 - 1)$$

$$(4x^2 - 1)(x^2 - y^2)$$

$$(2x-1)(2x+1)(x+y)(x-y)$$

$$128. \quad \underbrace{x^6y^3 + x^3} - \underbrace{x^3y^3 - 1}$$

$$x^3(\underbrace{x^3y^3 + 1}) - 1(\underbrace{x^3y^3 - 1})$$

$$(x^3y^3 + 1)(x^3 - 1)$$

$$(xy + 1)(x^2y^2 - xy + 1)(x - 1)(x^2 + x + 1)$$

$$80. \quad 3x^4 + 20x^2 + 32$$

$$\underbrace{3x^4 + 12x^2} + \underbrace{8x^2 + 32}$$

$$3x^2(x^2 + 4) + 8(x^2 + 4)$$

$$(x^2 + 4)(3x^2 + 8)$$

$$\begin{array}{l} 3 \cdot 32 \\ \underline{3 \cdot 4 \cdot 8} \end{array}$$

$$132. \quad 3b^{n+2} + 4b^{n+1} - 4b^n$$

$$b^n(3b^2 + 4b - 4)$$

$$3(-4) = -12 \\ = 6(-2)$$

$$b^n(3b^2 + 6b - 2b - 4)$$

$$b^n[3b(b+2) - 2(b+2)]$$

$$b^n(b+2)(3b-2)$$

5.6
#3 - |3|
odd