

Review

What values are excluded from the domain?

$$f(x) = \frac{(x-2)(x+3)}{x(x-4)(x+5)}$$

$$x \neq 0, 4, -5$$

6.1, 6.2 Rational Functions

A rational function is of the form $f(x) = \frac{p(x)}{q(x)}$, where

p & q are polynomials.

Simplify.

Factor First!

$$46. \frac{(3a^2 - 6a)}{(12 - 6a)} = \frac{3a(a-2)}{-6(-2+a)} = \frac{\cancel{3a}(a-2)}{-\cancel{6}(a-2)}$$

$$= \frac{a}{-2} = \frac{-a}{2} = \boxed{-\frac{a}{2}, a \neq 2}$$

$$52. \frac{3x^3y^3 - 12x^2y^2 + 15xy}{3xy}$$

$$= \frac{\cancel{3xy}(x^2y^2 - 4xy + 5)}{\cancel{3xy}}$$

$$= \boxed{x^2y^2 - 4xy + 5, x \neq 0, y \neq 0}$$

$$60. \frac{2x^2 + 7xy - 4y^2}{4x^2 - 4xy + y^2}$$

$$= \frac{2x^2 + 8xy - xy - 4y^2}{4x^2 - 2xy - 2xy + y^2}$$

$$= \frac{2x(x+4y) - y(x+4y)}{2x(2x-y) - y(2x-y)}$$

$$= \frac{(x+4y)\cancel{(2x-y)}}{\cancel{(2x-y)}\cancel{(2x-y)}} = \frac{x+4y}{2x-y}, \quad \begin{array}{l} 2x-y \neq 0 \\ 2x \neq y \\ x \neq y/2 \end{array}$$

$$72. \frac{4a^2 - 8ab + 4b^2}{4a^2 - 4b^2}$$

$$= \frac{4(a^2 - 2ab + b^2)}{4(a^2 - b^2)}$$

$$= \frac{\cancel{4}(a-b)(a-b)}{\cancel{4}(a-b)(a+b)} = \frac{a-b}{a+b}, \quad a \neq -b, b$$

$a-b \neq 0 \quad a+b \neq 0$

$$78. \frac{x^4 - 2x^2 - 3}{x^4 + 2x^2 + 1}$$

$$= \frac{x^4 + x^2 - 3x^2 - 3}{x^4 + x^2 + x^2 + 1}$$

$$= \frac{x^2(x^2 + 1) - 3(x^2 + 1)}{x^2(x^2 + 1) + 1(x^2 + 1)}$$

$$= \frac{\cancel{(x^2 + 1)}(x^2 - 3)}{\cancel{(x^2 + 1)}(x^2 + 1)}$$

$$= \frac{x^2 - 3}{x^2 + 1}$$

domain is
all real #'s
 $x^2 + 1$ is never
equal to 0

6.2 Operations on Rational Functions

(Same rules of fractions apply)

$$\frac{a}{b} \pm \frac{c}{d} = \frac{a}{b} \cdot \frac{d}{d} \pm \frac{c}{d} \cdot \frac{b}{b} = \frac{ad \pm cb}{bd}$$

$$\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$$

$$\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \cdot \frac{d}{c} = \frac{ad}{bc}$$

$$8. \frac{2x^2 - 5x + 3}{x^6 y^3} \cdot \frac{x^4 y^4}{2x^2 - x - 3}$$

(Red annotations: $2x^2 - 2x - 3x + 3$ above numerator; $2x^2 + 2x - 3x - 3$ below denominator)

$$= \frac{2x(x-1) - 3(x-1)}{x^6 y^3} \cdot \frac{x^4 y^4}{2x(x+1) - 3(x+1)}$$

$$= \frac{(x-1)(2x-3) \cdot \cancel{x^4 y^4}}{x^{\cancel{6}} y^{\cancel{3}} (x+1)(2x-3)} = \frac{y(x-1)}{x^2(x+1)}, \quad \begin{matrix} x \neq 0, -1 \\ y \neq 0 \end{matrix}$$

(Red annotations: $2x-3 \neq 0$ below denominator; $x \neq 0, -1$ and $y \neq 0$ in a red box)

$$18. \frac{x^4 - 5x^2 + 4}{3x^2 - 4x - 4} \cdot \frac{3x^2 - 10x - 8}{x^2 - 4}$$

$$= \frac{\cancel{(x-2)}(x+2) \cdot \cancel{(x-1)}(x+1)}{\cancel{(x-4)}(x-2)} \cdot \frac{\cancel{(3x+2)}(x-4)}{\cancel{(x-2)}(x+2)}$$

$3x^2 - 4x - 4$ $3x^2 - 6x + 2x - 4$ $3x(x-2) + 2(x-2)$ $(x-2)(3x+2)$	$3x^2 - 10x - 8$ $3x^2 - 12x + 2x - 8$ $3x(x-4) + 2(x-4)$ $(x-4)(3x+2)$	$x^4 - 5x^2 + 4$ $x^4 - x^2 - 4x^2 + 4$ $x^2(x^2-1) - 4(x^2-1)$ $(x^2-1)(x^2-4)$
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$$= \frac{(x-1)(x+1)(x-4)}{x-2}, \quad x \neq 2, -2, -2/3$$

Hw:

6.1 # 39-79 odd

6.2 # 3-17 odd