

Review

$$\text{Simplify: } \frac{2x^{-5}y^4}{3x^2y} \cdot \frac{3^{-2}xy^3}{2^3x} = \frac{2y^{1-1}}{3x^{2+5}} \cdot \frac{y^3}{2^3 \cdot 3^2}$$

$$= \frac{2y^3 y^3}{3x^7 \cdot 8 \cdot 9} = \boxed{\frac{y^6}{108x^7}}$$

Find the equation of the line passing through the points  $(5, -3)$  &  $(-1, 1)$ .

$$m = \frac{-3-1}{5-(-1)} = \frac{-4}{6} = -\frac{2}{3}$$

$$y - y_1 = m(x - x_1) \quad y - 1 = -\frac{2}{3}(x + 1)$$

$$y - 1 = -\frac{2}{3}x - \frac{2}{3}$$

$$\boxed{y = -\frac{2}{3}x + \frac{1}{3}}$$

5.3 Multiplication of Polynomials

Distributive Property:  $a(b + c) = ab + ac$

$$a(b + c + d + e + f) = ab + ac + ad + ae + af$$

Multiplying a Polynomial by a Monomial

$$-3xy^2(2x^3y - xy^4 + 4x^3y^2)$$

$$(-3xy^2)(2x^3y) + (-3xy^2)(-xy^4) + (-3xy^2)(4x^3y^2)$$

$$\boxed{-6x^4y^3 + 3x^2y^6 - 12x^4y^4}$$

In general, multiply every term by every other term and then combine like terms.

$$(3x^5 - 2x^3 + 3)(4x^2 - 5x)$$

$$(3x^5)(4x^2) + (3x^5)(-5x) + (-2x^3)(4x^2) + (-2x^3)(-5x) + 3(4x^2) + 3(-5x)$$

$$12x^7 - 15x^6 - 8x^5 + 10x^4 + 12x^2 - 15x$$

Lead-term:  $12x^7$

degree: 7

Leading coeff: 12

constant term: 0

$$(2x - 3 + 4x^2)(5x^3 - x^8 + 2x)$$

$$\begin{aligned} & 2x(5x^3) + 2x(-x^8) + 2x(2x) + (-3)(5x^3) + (-3)(x^8) + (-3)(2x) + \\ & + 4x^2(5x^3) + 4x^2(-x^8) + 4x^2(2x) \\ = & \cancel{10x^4} - \cancel{2x^9} + \cancel{4x^2} - \cancel{15x^3} - \cancel{3x^8} - \cancel{6x} + \cancel{20x^5} - \cancel{4x^{15}} + \cancel{8x^3} \\ = & -4x^{10} - 2x^9 - 3x^8 + 20x^5 + 10x^4 - 7x^3 + 4x^2 - 6x \end{aligned}$$

### Multiplying Two Binomials (FOIL Method)

$$(x + 3)(x^2 - 4x)$$

$$x^3 - 4x^2 + 3x^2 - 12x$$

Special Cases:

F	O	I	L
r	u	n	a
s	+ s	s	s
t	s i	d t	
e	d e	e	

$$(a + b)(a - b) = a^2 - ab + ab - b^2 = a^2 - b^2$$

$$(a + b)^2 = (a + b)(a + b) = a^2 + ab + ab + b^2 = a^2 + 2ab + b^2$$

$$(a - b)^2 = (a - b)(a - b) = a^2 - ab - ab + b^2 = a^2 - 2ab + b^2$$

$$(a + b)(a - b) = a^2 - b^2$$

$$(a + b)^2 = a^2 + 2ab + b^2$$

$$(a - b)^2 = a^2 - 2ab + b^2$$

Book Problems from section 5.3:

$$a^m a^n = a^{m+n}$$

26.  $a^{n+4}(a^{n-2} + 5a^2 - 3)$

$$a^{n+4}a^{n-2} + a^{n+4}(5a^2) + a^{n+4}(-3)$$

$$a^{2n+2} + 5a^{n+6} - 3a^{n+4}$$

50.  $(2a^n - b^n)(3a^n + 2b^n)$

$$(2a^n)(3a^n) + (2a^n)(2b^n) + (-b^n)(3a^n) + (-b^n)(2b^n)$$

$$6a^{2n} + 4a^n b^n - 3a^n b^n - 2b^{2n}$$

66.  $(x^n + y^n)(x^n - 2x^n y^n + 3y^n)$

$$x^n x^n + x^n(-2x^n y^n) + x^n(3y^n) + y^n x^n + y^n(-2x^n y^n) + y^n(3y^n)$$

$$= x^{n+n} - 2x^{n+n} y^n + 3x^n y^n + x^n y^n - 2x^n y^{n+n} + 3y^{n+n}$$

$$= \boxed{x^{2n} - 2x^{2n} y^n + 4x^n y^n - 2x^n y^{2n} + 3y^{2n}}$$

Simplify.

108.  $\frac{(2x + 1)^5}{(2x + 1)^3}$

116.  $[x + (y + 1)][x - (y + 1)]$

126. Find  $(3n^4)^3$  if  $5(n - 1) = 2(3n - 2)$ .

Recommended textbook problems:

5.1 #63-85 odd

5.2 #3-7odd, 15-25odd, 35-49odd

5.3 #25-29odd, 43-51odd, 61-67odd, 89-97odd, 109-117odd