

D 1. $a^m a^n$

E 2. a^{-n}

G 3. $(ab)^2$

B 4. $\frac{a^m}{a^n}$

F 5. $(a - b)^2$

H 6. $(a^m)^n$

L 7. $\left(\frac{a}{b}\right)^2$

C 8. $(a + b)^2$

I 9. a^0

A 10. $(a - b)(a + b)$

A. $a^2 - b^2$

B. a^{m-n}

C. $a^2 + 2ab + b^2$

D. a^{m+n}

E. $\frac{1}{a^n}$

F. $a^2 - 2ab + b^2$

G. $a^2 b^2$

H. a^{mn}

I. 1

J. $a^2 + b^2$

K. $a^2 + ab + b^2$

L. $\frac{a^2}{b^2}$

M. a^{n-m}

N. $a^2 - ab + b^2$

O. 0

11. Write the interval in set-builder notation:

[-2, 5)

{\color{red} \{x | -2 \leq x < 5\}}

12. Write the set in interval notation:

{\color{red} \{x | x > -4\}}

{\color{red} (-4, \infty)}

15. A system of equations with a single solution is called _____

A pair of lines intersecting at a single point is an example of this.

independent

16. A system of equations with no solution is called _____

A pair of parallel lines (which never intersect) is an example of this.

inconsistent

17. A system of equations with infinitely many solutions is called _____

A pair of equations representing the same line is an example of this.

dependent13. State the equation of the line passing through the point $(-4, 9)$ whose slope is undefined.

$x = -4$

14. State the distributive property of real numbers.

$$a(b+c) = ab+ac$$

5.6

Special Factoring

$$a^2 - b^2 = (\dot{a} + b)(a - b)$$

$$a^2 + 2ab + b^2 = (a + b)(a + b) = (a + b)^2$$

$$a^2 - 2ab + b^2 = (a - b)(a - b) = (a - b)^2$$

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

$$\frac{5.6}{12} \cdot a^2 b^2 - 25$$

$$a^2 - b^2 = (a-b)(a+b)$$

$$(ab)^2 - 5^2$$

$$(ab - 5)(ab + 5)$$

$$42. \quad 64a^3 + 27$$

$$(4a)^3 + 3^3$$

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

$$(4a+3)(16a^2 - 12a + 9)$$

$$16. \quad 4x^2y^2 + 12xy + 9$$

$$(2xy)^2 + 2(2xy)(3) + 3^2$$

$$(a+b)^2 = (a+b)(a+b) \\ = a^2 + 2ab + b^2$$

$$(2xy + 3)^2$$

$$= (2xy + 3)(2xy + 3)$$

$$22. \quad b^2 - 18b + 81$$

$$b^2 - 2(b)(9) + 9^2$$

$$(b-9)^2 = (b-9)(b-9)$$

$$(a-b)^2 = a^2 - 2ab + b^2$$

48. $1 - 125b^3$

$$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$

$$1^3 - (5b)^3$$

$$(1-5b)(1+5b+25b^2)$$

54. $27x^3 - 8y^3$

$$(3x)^3 - (2y)^3$$

$$(3x-2y)(9x^2 + 6xy + 4y^2)$$

58. $a^3 + (a+b)^3$

$$x^3 + y^3 = (x+y)(x^2 - xy + y^2)$$

$$(a+b)^3 = (a+b)(a+b)(a+b) = a^3 + ab + ab + b^3$$

$$(a+a+b)(a^2 - a(a+b) + (a+b)^2)$$

$$(2a+b)(a^2 - a^2 - ab + a^2 + 2ab + b^2)$$

$$(2a+b)(a^2 + ab + b^2)$$

60. $x^{3n} + y^{3n}$

$$(x^n)^3 + (y^n)^3$$

$$(a^m)^3 = a^{3m}$$

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

$$(x^n + y^n)(x^{2n} - x^n y^n + y^{2n})$$

86. $3x^4 - 81x$

$$3x(x^3 - 27)$$

$$3x(x-3)(x^2 + 3x + 9)$$

102. $4x^3 + 8x^2 - 9x - 18$

$$4x^2(x+2) - 9(x+2)$$

$$(x+2)(4x^2 - 9)$$

$$(x+2)(2x-3)(2x+3)$$

$$108. \ 8x^4 - 40x^3 + 50x^2$$

$$2x^2(4x^2 - 20x + 25)$$

$(2x)^2 - 2(2x)(5) + 5^2$

$$2x^2(2x - 5)^2$$

$$(a-b)^2 = a^2 - 2ab + b^2$$

$$2x^2(2x-5)(2x-5)$$

$$120. \ 24a^2b^2 - 14ab^3 - 90b^4$$

$$2b^2(12a^2 - 7ab - 45b^2)$$

$$\begin{matrix} 12(-45) \\ \hat{3} \cdot \hat{4} \quad \hat{5} \cdot \hat{9} \quad (-1) \\ \hat{\hat{3}} \cdot \hat{\hat{3}} \end{matrix}$$

$$\underbrace{3 \cdot 3 \cdot 3 \cdot 4 \cdot 5}_{3 \cdot 3} \cdot (-1)$$

$$2b^2(12a^2 - 27ab + 20ab - 45b^2)$$

$$2b^2[3a(4a-9b) + 5b(4a-9b)]$$

$$2b^2(4a-9b)(3a+5b)$$

126.
$$\begin{aligned} & \underbrace{4x^4 - x^2}_{x^2(4x^2-1)} - \underbrace{4xy^2 + y^2}_{y^2(4x^2-1)} \\ & (4x^2-1)(x^2-y^2) \\ & (2x-1)^2(2x+1)^2 \\ & \boxed{(2x-1)(2x+1)(x-y)(x+y)} \end{aligned}$$

128.
$$\begin{aligned} & \underbrace{x^6y^3 + x^3y^3}_{x^3(x^3y^3+1)} - \underbrace{x^3y^3 - 1}_{-1(x^3y^3+1)} \\ & (x^3y^3+1)(x^3-1) \\ & ((xy)^3 + 1^3)(x^3 - 1^3) \\ & \boxed{(xy+1)(x^2y^2-xy+1)(x-1)(x^2+x+1)} \end{aligned}$$

80.
$$\begin{aligned} & 3x^4 + 20x^2 + 32 \\ & \begin{array}{l} \overbrace{3(32)}^{3 \cdot 8 \cdot 4} \\ \quad \quad \quad \end{array} \quad \begin{array}{l} \overbrace{3x^4 + 12x^2}^{3x^2(x^2+4)} + \overbrace{8x^2 + 32}^{8(x^2+4)} \\ \quad \quad \quad \end{array} \\ & (x^2+4)(3x^2+8) \end{aligned}$$

$$132. \quad 3b^{n+2} + 4b^{n+1} - 4b^n$$

$$b^n(3b^2 + 4b - 4)$$

$$3(-1) = -12 = 6(-2)$$

$$b^n(3b^2 + \underbrace{6b - 2b}_{6b - 2b} - 4)$$

$$b^n[3b(b+2) - 2(b+2)]$$

$$\boxed{b^n(b+2)(3b-2)}$$

5.6

#3-13 | odd