

HW#3 - Due Tuesday, 09/08:

3.1 - #3-29 odd

ordered pairs, distance, midpoint

3.2 - #3-16 all, 21-43 odd, 49-87 odd

functions, domain, range

HW#4 - Due Friday, 09/11:

3.3 - #3-9 odd, 15-33 odd

graph by plotting points, x- and y-intercepts

3.4 - #3-19 odd, 29-41 odd

finding slope, graph using slope and y-intercept

3.5 - #3-49 odd

finding equations of lines

4.1 - #9,11,13,15,29,37,43,49

solving systems with graphing and substitution

4.2 - #9,13,17,25,27,31,35

solving systems with elimination

Test #2 - MONDAY, 9/14

H 1. slope-intercept formula

~~A.~~ $\frac{y_2 - y_1}{x_2 - x_1}$ *nothing!*

~~O.~~ $-a$

N 2. slope

~~B.~~ $x = c$

~~P.~~ system of equations with no solution

R 3. point-slope formula

C. system of equations with only one solution

~~Q.~~ $y = c$

O 4. additive inverse

D. $a + b = b + a$ *independent*

~~R.~~ $y - y_1 = m(x - x_1)$

I 5. multiplicative inverse

~~E.~~ equation that is true for only some values of x *commutativity*

~~S.~~ 1

F 6. distributive property

~~F.~~ $a(b + c) = ab + ac$

~~T.~~ $a + (b + c) = (a + b) + c$

T 7. associativity

G. 0 *additive identity*

~~X.~~ $(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2})$

K 8. dependent

~~H.~~ $y = mx + b$



L 9. distance formula

~~I.~~ $1/a$

(x_2, y_2)

Q 10. horizontal line

~~J.~~ equation that is never true

P 11. inconsistent

~~K.~~ system of equations with infinitely many solutions

U 12. midpoint formula

~~L.~~ $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

E 13. conditional

M. equation that is always true *identity*

J 14. contradiction

~~N.~~ $\frac{y_2 - y_1}{x_2 - x_1}$

B 15. vertical line

S 16. multiplicative identity

17. Solve for x . $4[3 + 5(3 - x) + 2x] = 2 - 2x$

$$4[3 + 15 - 5x + 2x] = 2 - 2x$$

$$4[18 - 3x] = 2 - 2x$$

$$72 - 12x = 2 - 2x$$

$$70 = 10x$$

$$x = 7$$

18. State whether each of the following relations is a function (yes or no).

a. $\{(1,2), (2,3), (3,4), (4,2)\}$

yes

b. $\{(7,5), (7,4), (7,3), (7,2)\}$

no

c. $\{(2,1), (3,1), (4,1), (5,1)\}$

yes

19. Evaluate $F(-3)$, given that $F(x) = x^2 + 4x - 5$.

$$F(-3) = (-3)^2 + 4(-3) - 5$$

$$= 9 - 12 - 5$$

$$= -8$$

note: $(-3, -8)$

is a point on

the graph of f

20. Find the distance between the points $P_1(-4,4)$ and $P_2(1,2)$.

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(1 - (-4))^2 + (2 - 4)^2}$$

$$= \sqrt{(5)^2 + (-2)^2} = \sqrt{25 + 4} = \sqrt{29}$$

21. Find the midpoint of the line segment between the points $P_1(3, -7)$ and $P_2(-1, 5)$.

$$(x_m, y_m) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$= \left(\frac{3 + (-1)}{2}, \frac{-7 + 5}{2} \right) = \left(\frac{2}{2}, \frac{-2}{2} \right) = (1, -1)$$

22. What values are excluded from the domain of the function? List your answer(s) using the roster method.

- a. $g(x) = \frac{2x+6}{3}$ \emptyset domain: $\mathbb{R} = (-\infty, \infty)$
 b. $G(x) = \frac{1}{4-x}$ $\{4\}$ domain: $\{x|x \neq 4\} = (-\infty, 4) \cup (4, \infty)$
 c. $f(x) = \frac{x-5}{x+9}$ $\{-9\}$ domain: $\{x|x \neq -9\} = (-\infty, -9) \cup (-9, \infty)$

23. State the domain of the function $f(x) = \frac{x-1}{x+2}$ in interval notation.



24. Find the range of the function $f(x) = \frac{5}{1-x}$, where the domain is restricted to the set $\{-2, 0, 2\}$. List your answers using the roster method. *range=output of domain*

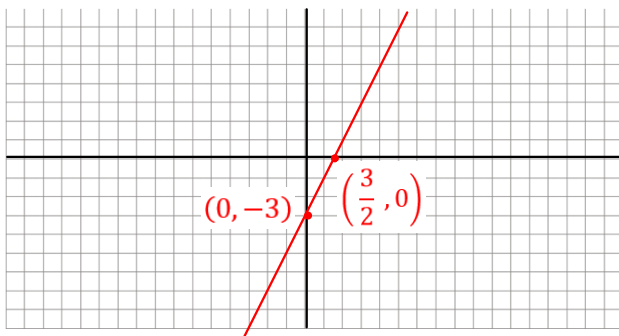
$$f(-2) = \frac{5}{1 - (-2)} = \frac{5}{3}$$

$$f(0) = \frac{5}{1 - 0} = 5$$

$$f(2) = \frac{5}{1 - 2} = \frac{5}{-1} = -5$$

$\{-5, \frac{5}{3}, 5\}$

25. Graph the linear function $2x - y = 3$. Include labels on axes to indicate your scale, and label with an ordered pair (x, y) the coordinates of each of the points you used to draw your line.



*Note: any two points will work to graph a line;
 x- and y-intercepts are two easy points to plot*

$$-y = -2x + 3$$

$$y = 2x - 3$$

slope: 2

x-intercept:
 $2x - 0 = 3$
 $x = 3/2$

y-intercept:
 $2(0) - y = 3$
 $y = -3$

26. Find the x- and y-intercepts of the function $3x + 4y = -8$.

x-intercept: $3x + 4(0) = -8$
 $(x, 0) \quad x = -8/3$ $(-\frac{8}{3}, 0)$

y-intercept: $0x + 4y = -8$
 $(0, y) \quad y = -2$ $(0, -2)$

27. Find the slope of the line containing the points $(-2, 5)$ and $(3, -1)$.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{5 - (-1)}{-2 - 3} = \frac{6}{-5} = \boxed{-\frac{6}{5}}$$

28. Find the equation of the line that has slope 0 and passes through the point $(-4, 7)$.

$y = 7$

note:

vertical lines have undefined slope and are of the form $x=a$

horizontal lines have slope 0 and are of the form $y=b$

29. Find the equation of the line that is parallel to the line $2x - 3y = 2$ and passes through the point $(6, -4)$.

$$y - y_1 = m(x - x_1) \qquad -3y = -2x + 2$$

$$y - (-4) = \frac{2}{3}(x - 6) \qquad y = \frac{2}{3}x - \frac{2}{3}$$

$$y + 4 = \frac{2}{3}x - 4$$

$$m = \frac{2}{3} \quad (x_1, y_1) = (6, -4)$$

$y = \frac{2}{3}x - 8$

Note: if we were asked to find a perpendicular line,

we would have used $m = -3/2$

30. Solve the system of equations. If it exists, give your solution as an ordered pair (x, y) .

$$\begin{cases} (3x + 2y = 5) & (3) \\ (2x - 3y = -14) & (2) \end{cases}$$

$$9x + 6y = 15 \qquad 3(-1) + 2y = 5$$

$$+ \quad 4x - 6y = -28 \qquad -3 + 2y = 5$$

$$13x = -13 \qquad 2y = 8$$

$$x = -1 \qquad y = 4$$

$(-1, 4)$

Check:

$$3(-1) + 2(4) = -3 + 8 = 5 \quad \checkmark$$

$$2(-1) - 3(4) = -2 - 12 = -14 \quad \checkmark$$

Note: if addition yields a contradiction, the system is inconsistent (parallel lines) and there is no solution.

if addition yields an identity, the system is dependent and the solution is all (infinitely many) ordered pairs of the form $(x, mx+b)$