

HW #5 - Due Tuesday, 9/15:  
 5.1 #63-85 odd

HW #6 - Due Wednesday, 9/16:  
 5.2 #3-7odd, 15-25odd, 35-49odd

HW #7 - Due Tuesday, 9/22:  
 5.3 #25-29odd, 43-51odd, 61-67odd, 89-97odd, 109-117odd

HW #8 - Due Friday, 9/25:  
 5.4 #19-25 odd; 27-43 odd; 55-61 odd  
 5.5 #21-47 odd

HW #9 - Due Tuesday, 9/29?  
 5.6 #3-131 odd  
 5.7 #35-49 odd, 51-57 odd, 61-75odd

Test 3 - Tuesday, 9/29?

Ch 5 - Exponential Expressions & Polynomials

5.1 - Exponential Expressions

5.2 - Intro to Polynomials

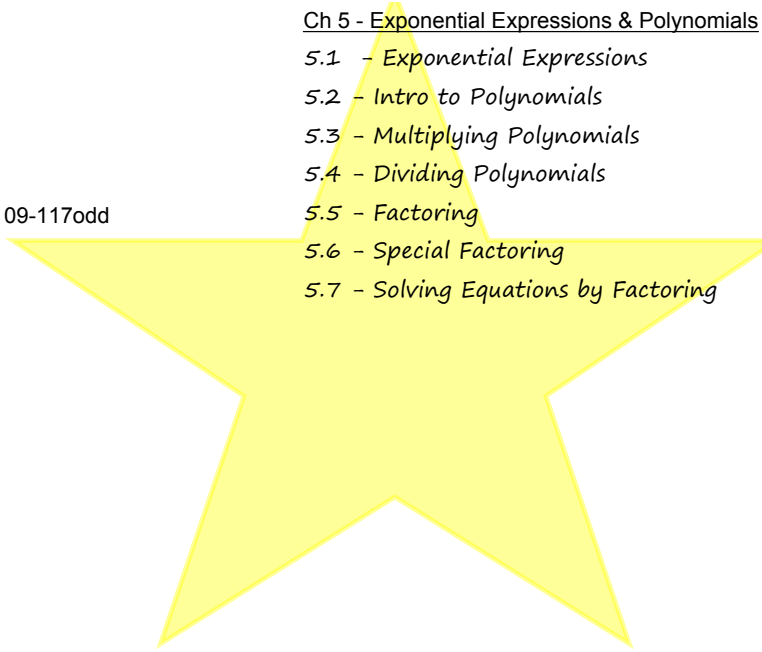
5.3 - Multiplying Polynomials

5.4 - Dividing Polynomials

5.5 - Factoring

5.6 - Special Factoring

5.7 - Solving Equations by Factoring



Review:

Multiply the polynomials:  $(3x^2 - x^3 + 2x + 1)(4x - 5)$

$$12x^3 - 4x^4 + 8x^2 + 4x - 15x^2 + 5x^3 - 10x - 5$$

$$-4x^4 + 17x^3 - 7x^2 - 6x - 5$$

Divide the polynomials:  $\frac{x + 3x^4 - x^2 + 5x^3 - 2}{x + 2}$

$$\begin{array}{r} -2 \overline{) 3 \ 5 \ -1 \ 1 \ -2} \\ \underline{-6 \ 2 \ -2 \ 2} \\ 3 \ -1 \ 1 \ -1 \ 0 \end{array}$$

$$= 3x^3 - x^2 + x - 1$$

M 1.  $a^m a^n$

E 2.  $a^{-n}$

G 3.  $(ab)^2$

D 4.  $\frac{a^m}{a^n}$

N 5.  $(a-b)^2 = (a-b)(a-b)$

H 6.  $(a^m)^n$

L 7.  $\left(\frac{a}{b}\right)^2$

K 8.  $(a+b)^2 = (a+b)(a+b)$

O 9.  $a^0$

J 10.  $(a-b)(a+b)$

A.  $a^2 + b^2$

B.  $a^{n-m}$

C.  $a^2 + ab + b^2$

D.  $a^{m-n}$

E.  $\frac{1}{a^n}$

F.  $a^2 - ab + b^2$

G.  $a^2 b^2$

H.  $a^{mn}$

I. 0

J.  $a^2 - b^2$

K.  $a^2 + 2ab + b^2$

L.  $\frac{a^2}{b^2}$

M.  $a^{m+n}$

N.  $a^2 - 2ab + b^2$

O. 1

11. Write the interval in set-builder notation:

$[-4, 1)$

$$\{x \mid -4 \leq x < 1\}$$

12. Write the set in interval notation:

$\{x \mid x > -7\}$

$$(-7, \infty)$$

13. State the equation of the line passing through the point  $(3, -7)$  whose slope is undefined.

$$x = 3$$

14. State the distributive property of real numbers.

$$a(b+c) = ab+ac$$

15. A system of equations with a single solution is called independent.  
A pair of lines intersecting at a single point is an example of this.

16. A system of equations with no solution is called inconsistent.  
A pair of parallel lines (which never intersect) is an example of this.

17. A system of equations with infinitely many solutions is called dependent.  
A pair of equations representing the same line is an example of this.

## Factor trinomials of the form $ax^2+bx+c$

When  $a=1$ , we look for factors of  $c$  that sum to  $b$ .

When  $a$  is any constant other than 1, we will

- look for factors of  $c \cdot a$  that sum to  $b$ ,
- rewrite  $bx$  as a sum of two terms whose coefficients are those factors,
- factor by grouping.

5.6Special Factoring

$$a^2 - b^2 = (a+b)(a-b)$$

$$a^2 + 2ab + b^2 = (a+b)(a+b) = (a+b)^2$$

$$a^2 - 2ab + b^2 = (a-b)(a-b) = (a-b)^2$$

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

$$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$

$$a^3 + b^3 \neq (a+b)^3$$

$$a^2 - b^2 \neq (a-b)^2$$

$$48. \quad 1 - 125b^3 = 1^3 - (5b)^3$$

$$= (1 - 5b)(1 + 5b + 25b^2)$$

$$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$

$$54. \quad 27x^3 - 8y^3$$

$$(3x)^3 - (2y)^3$$

$$(3x - 2y)(9x^2 + 6xy + 4y^2)$$

58.  $a^3 + (a+b)^3$

$$x^3 + y^3 = (x+y)(x^2 - xy + y^2)$$

$$(a+a+b)(a^2 - a(a+b) + (a+b)^2)$$

$$(2a+b)(a^2 - a^2 - ab + a^2 + 2ab + b^2)$$

$$(2a+b)(a^2 + ab + b^2)$$

60.  $X^{3n} + Y^{3n}$   
 $(x^n)^3 + (y^n)^3$

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

$$(x^n + y^n)(x^{2n} - x^n y^n + y^{2n})$$

$$86. \quad 3x^4 - 81x = 3x(x^3 - 27) = 3x(x^3 - 3^3)$$

$$= \boxed{3x(x-3)(x^2 + 3x + 9)}$$

$$a^2 - b^2 = (a-b)(a+b)$$

$$102. \quad 4x^3 + 8x^2 - 9x - 18$$

$$4x^2(x+2) - 9(x+2)$$

$$(x+2)(4x^2 - 9)$$

$$(x+2)((2x)^2 - 3^2)$$

$$\boxed{(x+2)(2x-3)(2x+3)}$$

$$108. \quad 8x^4 - 40x^3 + 50x^2$$

$$2x^2(4x^2 - 20x + 25)$$

$$2x^2((2x)^2 - 2(2x)(5) + 5^2)$$

$$\boxed{2x^2(2x-5)^2}$$

$$(a-b)^2 = a^2 - 2ab + b^2$$

$$120. 24a^2b^2 - 14ab^3 - 90b^4$$

$$2b^2(12a^2 - 7ab - 45b^2)$$

$$12(-45)$$

$$\underbrace{2 \cdot 2 \cdot 3 \cdot 3 \cdot 3 \cdot 5}$$

$$2b^2(12a^2 + 20ab - 27ab - 45b^2)$$

$$2b^2[4a(3a+5b) - 9b(3a+5b)]$$

$$2b^2(3a+5b)(4a-9b)$$

$$126. \underbrace{4x^4 - x^2} - \underbrace{4x^2y^2 + y^2}$$

$$x^2(4x^2 - 1) - y^2(4x^2 - 1)$$

$$(4x^2 - 1)(x^2 - y^2)$$

$$((2x)^2 - 1^2)(x^2 - y^2)$$

$$(2x-1)(2x+1)(x-y)(x+y)$$

$$128. \quad X^6 y^3 + X^3 - X^3 y^3 - 1$$

$$X^3(X^3 y^3 + 1) - 1(X^3 y^3 + 1)$$

$$(X^3 y^3 + 1)(X^3 - 1)$$

$$(xy+1)(x^2y^2-xy+1)(x-1)(x^2+x+1)$$

$$\underline{3 \cdot 2 \cdot 2} \quad \underline{2 \cdot 2 \cdot 2}$$

$$80. \quad 3x^4 + 20x^2 + 32$$

$$3x^4 + 12x^2 + 8x^2 + 32$$

$$3x^2(x^2 + 4) + 8(x^2 + 4)$$

$$(x^2 + 4)(3x^2 + 8)$$