

HW #10 - due Fri, 10/2
 5.7 #35-75 odd Solving equations by factoring

HW #11 - due Mon, 10/5
 6.1 #39-79 odd Simplifying rational expressions

HW #12 - due Fri, 10/8
 6.2 #3-95 odd Operations on rational expressions
 6.6 #5-25 odd Literal Equations

HW #13 - due **wed.**
 7.1 #39-73 odd, 85-113 odd, 125-149 odd Rational Exponents and Radical Expressions

HW #14
 7.2 #11-21 odd, 43-51 odd, 57-65 odd, 85-91 odd, 97-103 odd, 113-121 odd Operations on Radical Expressions
 8.2 #59-69 odd Quadratic Equations
 6.3 #17,23,25,33,41,43 Complex Fractions
 6.4 #19,25,29,31 Rational Equations

Test 4
 Tues
 10/20

68. $4p^2 - 7p = -3$

$$\frac{7 \pm \sqrt{-7^2 - 4(4)(3)}}{2(4)}$$

$$\frac{7 \pm \sqrt{49 - 48}}{8}$$

$$\left(\frac{7 \pm \sqrt{1}}{8} \right) \cdot 8$$

$$\frac{7 \pm 1}{8}$$

$$\frac{7+1}{8}, \frac{7-1}{8}$$

$$\frac{8}{8} = 1, \frac{6}{8} = \frac{3}{4}$$

$$x = \left\{ \frac{3}{4}, 1 \right\}$$

$$x = \frac{3}{4}, 1$$

$$\text{If } ax^2 + bx + c = 0,$$

$$\text{then } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x^2 + x + 2 = 0$$

$$a=1, b=1, c=2$$

$$x = \frac{-1 \pm \sqrt{1^2 - 4(1)(2)}}{2(1)}$$

$$= \frac{-1 \pm \sqrt{1-8}}{2}$$

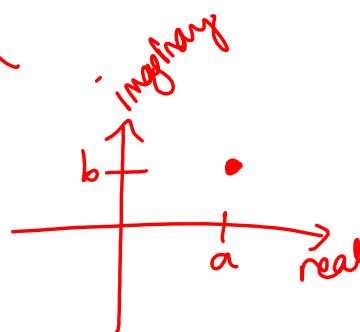
$$= \frac{-1 \pm \sqrt{-7}}{2} = \boxed{-\frac{1}{2} \pm \frac{\sqrt{7}}{2}i}$$

If $ax^2+bx+c=0$,
then $x = \frac{-b \pm \sqrt{b^2-4ac}}{2a}$

Complex #'s

$$a+bi, \quad a, b \in \mathbb{R}$$

\uparrow real part \uparrow imaginary part
 $i = \sqrt{-1}$



$$\begin{aligned}\sqrt{-9} &= \sqrt{(-1)(9)} = \sqrt{-1} \cdot \sqrt{9} = i \cdot 3 \\ &= 3i\end{aligned}$$



$$\begin{aligned}\sqrt{-50} &= \sqrt{(-1)(5)^2 \cdot 2} = \sqrt{-1} \cdot \sqrt{5^2} \cdot \sqrt{2} \\ &= i \cdot 5 \cdot \sqrt{2} \\ &= \boxed{5i\sqrt{2}} = (5\sqrt{2})i\end{aligned}$$

$$i = \sqrt{-1}$$

$$i^2 = -1$$

$$\begin{aligned}(3+2i)(3-5i) &= 9 - 15i + 6i - 10i^2 \\ &= 9 - 9i - 10(-1) \\ &= 9 - 9i + 10 = \boxed{19 - 9i}\end{aligned}$$

$$\begin{aligned} & (3-2i)(4+5i) \\ &= 12 + 15i - 8i - 10i^2 \\ &= 12 + 7i - 10(-1) \\ &= 12 + 7i + 10 \\ &= \boxed{22 + 7i} \end{aligned}$$

- 0-dim
- 1-dim
- 2-dim
-  3-dim
-  4-dim

Subtract and simplify. State the values which are not in the domain for each variable.

$$\begin{aligned}
 \frac{2x-1}{x-4} - \frac{x^2-10x-7}{x^2+x-20} &= \frac{(2x-1)(x+5)}{(x-4)(x+5)} - \frac{x^2-10x-7}{(x+5)(x-4)} \\
 &= \frac{2x^2+10x-x-5}{(x-4)(x+5)} - \frac{x^2-10x-7}{(x+5)(x-4)} \\
 &= \frac{2x^2+10x-x-5 - (x^2-10x-7)}{(x-4)(x+5)} \\
 &= \frac{2x^2+9x-5-x^2+10x+7}{(x-4)(x+5)} \\
 &= \frac{x^2+19x+2}{(x-4)(x+5)}, x \neq 4, -5
 \end{aligned}$$

Simplify:

$$\begin{aligned}
 \frac{x^2-12}{x^4-16} + \frac{1}{x^2-4} - \frac{1}{x^2+4} \\
 \frac{x^2-12}{(x^2-4)(x^2+4)} + \frac{1}{x^2-4} \cdot \frac{x^2+4}{x^2+4} - \frac{1}{x^2+4} \cdot \frac{x^2-4}{x^2-4} \\
 = \frac{x^2-12 + x^2+4 - x^2+4}{(x^2-4)(x^2+4)} \\
 = \frac{x^2-4}{(x^2-4)(x^2+4)} = \frac{1}{x^2+4}, x \neq -2, 2
 \end{aligned}$$

6.3 Complex Fractions

$$\begin{aligned}
 6. \frac{\left(1 + \frac{1}{x}\right)}{\left(1 - \frac{1}{x^2}\right)} &= \frac{1 \cdot \frac{x}{x} + \frac{1}{x}}{1 \cdot \frac{x^2}{x^2} - \frac{1}{x^2}} = \frac{\left(\frac{x+1}{x}\right)}{\left(\frac{x^2-1}{x^2}\right)} = \\
 &= \frac{x+1}{x} \cdot \frac{x^2}{x^2-1} = \frac{\cancel{x+1}}{\cancel{x^1}} \cdot \frac{x^{\cancel{2}}}{(x-1)\cancel{(x+1)}} \\
 &= \boxed{\frac{x}{x-1}, x \neq -1, 0, 1}
 \end{aligned}$$

$$\begin{aligned}
 16. \frac{\left(\frac{x}{x+1} - \frac{1}{x}\right)}{\left(\frac{x}{x+1} + \frac{1}{x}\right)} &= \frac{\frac{x}{x+1} \cdot \frac{x}{x} - \frac{1}{x} \cdot \frac{x+1}{x+1}}{\frac{x}{x+1} \cdot \frac{x}{x} + \frac{1}{x} \cdot \frac{x+1}{x+1}} \\
 &= \frac{\left(\frac{x^2 - (x+1)}{x(x+1)}\right)}{\left(\frac{x^2 + x + 1}{x(x+1)}\right)} = \frac{x^2 - x - 1}{x(x+1)} \cdot \frac{\cancel{x(x+1)}}{x^2 + x + 1} \\
 &= \boxed{\frac{x^2 - x - 1}{x^2 + x + 1}, x \neq 0, -1}
 \end{aligned}$$

$$\begin{aligned}
 22. \quad & \frac{1 - \frac{3}{x} - \frac{10}{x^2}}{1 + \frac{11}{x} + \frac{18}{x^2}} = \frac{\frac{x^2}{x^2} - \frac{3x}{x^2} - \frac{10}{x^2}}{\frac{x^2}{x^2} + \frac{11x}{x^2} + \frac{18}{x^2}} \\
 & = \frac{\left(\frac{x^2 - 3x - 10}{x^2}\right)}{\left(\frac{x^2 + 11x + 18}{x^2}\right)} = \frac{x^2 - 3x - 10}{x^2} \cdot \frac{\cancel{x^2}}{x^2 + 11x + 18} \\
 & = \frac{(x-5)(\cancel{x+2})}{(x+9)(\cancel{x+2})} = \frac{x-5}{x+9}, x \neq -9, -2, 0
 \end{aligned}$$

$$\begin{aligned}
 34. \quad & \frac{\frac{y}{y+2} - \frac{y}{y-2}}{\frac{y}{y+2} + \frac{y}{y-2}} = \frac{\left(\frac{y(y-2) - y(y+2)}{(y-2)(y+2)}\right)}{\left(\frac{y(y-2) + y(y+2)}{(y-2)(y+2)}\right)} \\
 & = \frac{y^2 - 2y - y^2 - 2y}{(y-2)(y+2)} \cdot \frac{\cancel{(y-2)}\cancel{(y+2)}}{y^2 - 2y + y^2 + 2y} \\
 & = \frac{-4y}{2y^2} = \frac{-2}{y}, y \neq 0, -2, 2
 \end{aligned}$$

$$\begin{aligned} 40. & \quad 1 - \frac{1}{\left(1 - \frac{1}{b-2}\right)} \\ &= 1 - \frac{1}{\left(\frac{b-2}{b-2} - \frac{1}{b-2}\right)} \\ &= 1 - \frac{1}{\left(\frac{b-3}{b-2}\right)} \\ &= 1 - \frac{b-2}{b-3} = \frac{b-3}{b-3} - \frac{b-2}{b-3} = \frac{-1}{b-3} \\ & \quad \boxed{b \neq 3, 2} \end{aligned}$$