

Review

Evaluate the trigonometric expression:

$$\sin(-120^\circ) = -\frac{\sqrt{3}}{2}$$

$$\cos 225^\circ = -\frac{1}{\sqrt{2}}$$

$$\tan(-270^\circ) = \text{undefined}$$

$$(x, y) = (\cos \theta, \sin \theta)$$

$$\sec 180^\circ = \frac{1}{\cos 180^\circ} = \frac{1}{-1} = -1$$

$$\csc 330^\circ = -2$$

$$\cot 135^\circ = -1$$

Convert to degrees:

$$\frac{3\pi}{4} \cdot \frac{180^\circ}{\pi} = 135^\circ \quad \frac{4\pi}{3} = 240^\circ$$

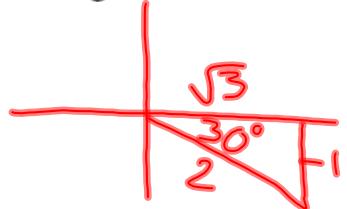
$$\frac{11\pi}{6} = 330^\circ$$

$$-\frac{5\pi}{2} = -450^\circ$$

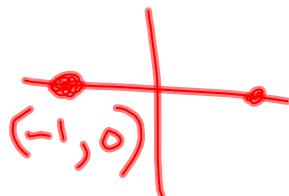
Homework questions?

Evaluate the trigonometric function of an angle given in radians

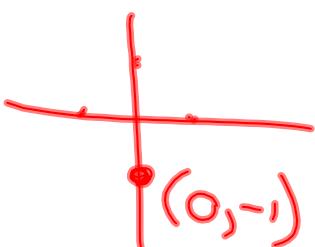
$$\cos \frac{11\pi}{6} = \frac{\sqrt{3}}{2}$$



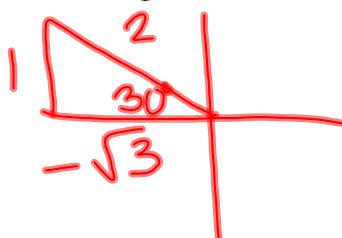
$$\sin 329\pi = \textcircled{0}$$



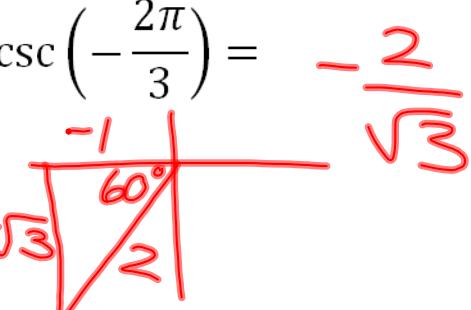
$$\tan \frac{7\pi}{2} = \text{undefined.}$$



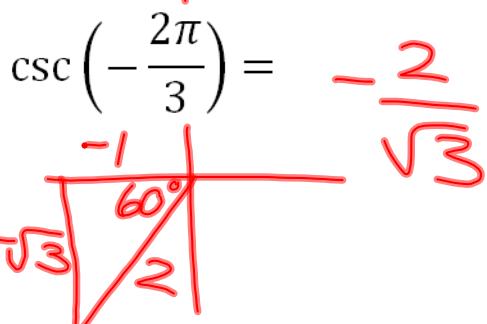
$$\sec \frac{5\pi}{6} = -\frac{2}{\sqrt{3}}$$



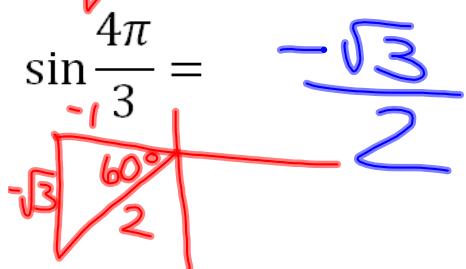
$$\cot \frac{3\pi}{4} = -1$$



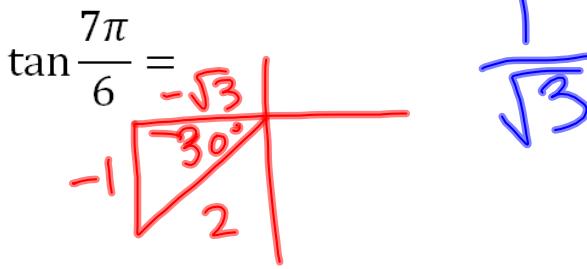
$$\sec \frac{7\pi}{4} = \frac{\sqrt{2}}{1}$$



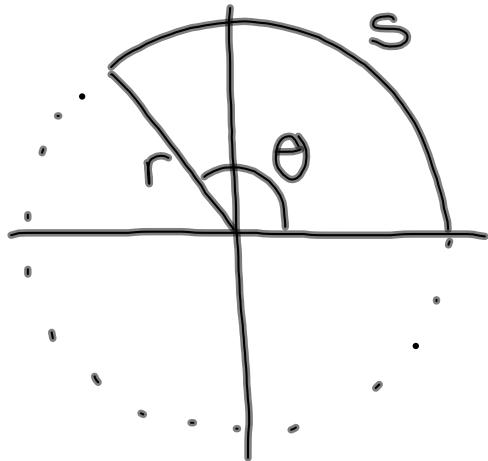
$$\csc \frac{3\pi}{2} = -1$$



$$\tan \frac{7\pi}{6} = \frac{1}{\sqrt{3}}$$



5.4 Arc Length & Angular Speed



Arc Length

r = radius or distance from the center of rotation
(in, cm, km, etc.)

s = arc length or distance traveled along the circumference of a circle
(in, cm, km, etc.)

θ = angle or amount of rotation
(deg, rad, revolutions, etc.)

$$s = r\theta$$

1. $r = 5 \text{ in}$; $\theta = 45^\circ$; $s = ? \text{ in}$

$$s = r\theta = 5 \text{ in} \cdot 45^\circ \cdot \frac{\pi}{180^\circ} = \boxed{\frac{5\pi}{4} \text{ in}}$$

2. $s = 16 \text{ yards}$; $\theta = 5$; $r = ? \text{ yards}$

$$r = \frac{s}{\theta} = \boxed{\frac{16 \text{ yd}}{5}}$$

3. Find the measure of a rotation in radians when a point 2 meters from the center of rotation travels 4 meters.

$$\theta = ? \text{ rad} ; \quad r = 2 \text{ m} ; \quad s = 4 \text{ m}$$

$$\frac{s}{r} = k \theta$$

$$\theta = \frac{s}{r} = \frac{\cancel{4} \pi}{\cancel{2} m} = \boxed{2}$$

Linear Speed

$$v = \frac{s}{t}$$

Angular Speed

$$\omega = \frac{\theta}{t}$$

Arc Length

$$s = r\theta$$

Relating Linear & Angular Speed

$$v = \frac{s}{t} = \frac{r\theta}{t} = r \cdot \frac{\theta}{t} = r\omega$$

$$v = r\omega$$

r = radius or distance from the center of rotation (in, cm, km, etc.)

s = arc length or linear distance along the circumference of a circle (in, cm, km, etc.)

θ = angle or amount of rotation (deg, rad, revolutions, etc.)

t = time (sec, min, hours, years, etc.)

v = $\frac{\text{linear distance}}{\text{time}} = \text{linear speed}$
 $\left(\frac{\text{km}}{\text{s}}, \frac{\text{mi}}{\text{h}}, \text{etc.} \right)$

ω = $\frac{\text{amount of rotation}}{\text{time}} = \text{angular speed}$
 $\left(\frac{\text{rev}}{\text{min}}, \frac{\text{deg}}{\text{s}}, \text{etc.} \right)$

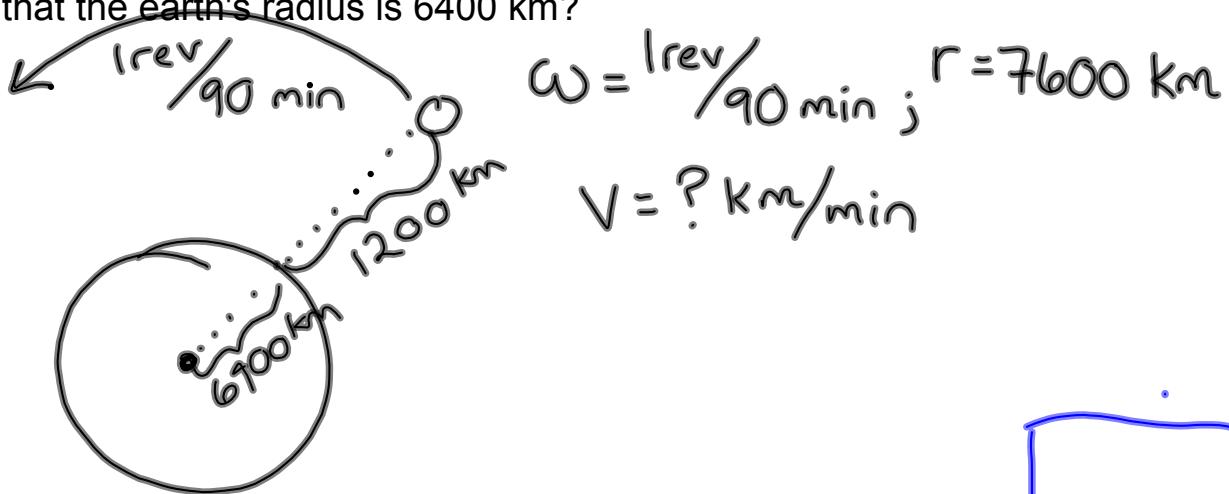
Handout Problems:

1. A wheel with a 15 inch diameter rotates at a rate of 6 radians per second. What is the linear speed of a point on its rim in feet per minute?

$$r = \frac{15}{2} \text{ in} ; \omega = \frac{6 \text{ rad}}{\text{s}} ; v = ? \text{ ft/min}$$

$$v = r\omega = \frac{15 \text{ in}}{2} \cdot \frac{6 \text{ rad}}{\text{s}} \cdot \frac{1 \text{ ft}}{12 \text{ in}} \cdot \frac{5 \text{ s}}{60 \text{ s}} \\ = \boxed{225 \text{ ft/min}}$$

2. An earth satellite in circular orbit 1200 km high makes one complete revolution every 90 minutes. What is its linear speed in km/min, given that the earth's radius is 6400 km?



$$v = r\omega = 7600 \text{ km} \cdot \frac{1 \text{ rev}}{90 \text{ min}} \cdot \frac{2\pi}{1 \text{ rev}} = \boxed{\frac{1520\pi}{9} \text{ km/min}}$$

3. Through how many radians does the minute hand of a clock rotate from 12:45pm to 1:25pm?

$$\theta = ? \text{ rad} ; t = 40 \text{ min} ; \omega = \frac{2\pi}{60 \text{ min}}.$$

$$t \cdot \omega = \frac{\theta}{\cancel{t}} \cdot \cancel{t}$$

$$\theta = \omega t = \frac{2\pi}{\cancel{60 \text{ min}}} \cdot \frac{40 \text{ min}}{1} = \boxed{\frac{4\pi}{3}}$$

4. A car travels at 60 miles per hour. Its wheels have a 24 inch diameter. What is the angular speed of a point on the rim of a wheel in revolutions per minute?

$$V = \frac{60 \text{ mi}}{h} ; r = 12 \text{ in} ; \omega = ? \text{ rev/min}$$

$$\frac{V}{r} = \cancel{R}\omega$$

$$\begin{aligned} \omega &= V \cdot \frac{1}{r} = \frac{60 \text{ mi}}{h} \cdot \frac{1}{12 \text{ in}} \cdot \frac{1 \text{ hr}}{60 \text{ min}} \cdot \frac{12 \text{ in}}{1 \text{ ft}} \cdot \frac{5280 \text{ ft}}{1 \text{ mi}} \cdot \frac{1 \text{ rev}}{2\pi} \\ &= \boxed{\frac{2640}{\pi} \text{ rev/min}} \end{aligned}$$

Homework:

Evaluating trig functions of angles in radians:

5.5 #7-24 all (**super mega-important hw section!)

HW to be checked on Friday: sections 5.3-5.5

Quiz Friday on trig functions of any angle in degrees (like 5.3#39-58)

In class on Friday/homework to have completed by Monday after the break (go ahead and start working on it now if you don't want too much hw over the break!): **Five problems on handout and 5.4#61-79odd**