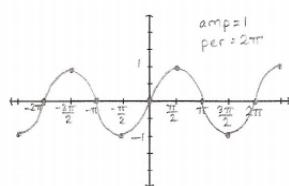
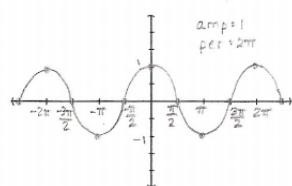


Graphing Trigonometric Functions continued...

$$y = \sin x$$

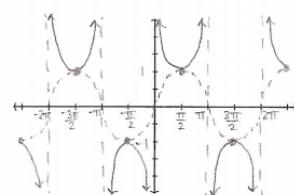


$$y = \cos x$$



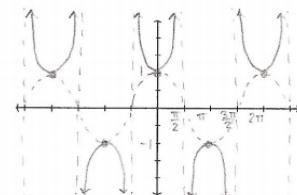
$$y = \csc x = \frac{1}{\sin x}$$

no zeros; asymptotes when $\sin x = 0$



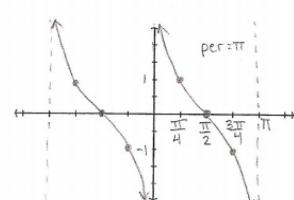
$$y = \sec x = \frac{1}{\cos x}$$

no zeros; asymptotes when $\cos x = 0$



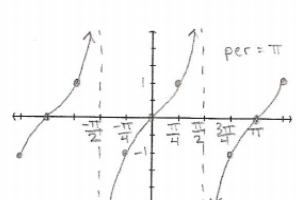
$$y = \cot x = \frac{\cos x}{\sin x}$$

zeros when $\cos x = 0$; asymptotes when $\sin x = 0$



$$y = \tan x = \frac{\sin x}{\cos x}$$

zeros when $\sin x = 0$; asymptotes when $\cos x = 0$

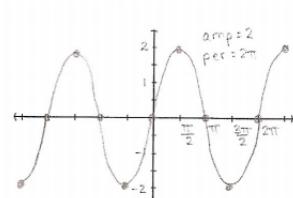


$$y = af(x)$$

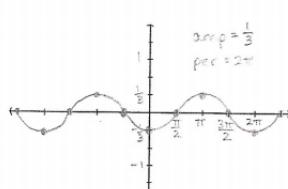
For $y = \sin x$ and $y = \cos x$, $|a|$ is the **amplitude** of the function. If $a < 0$, flip the graph vertically.

Ex.

$$y = 2 \sin x$$



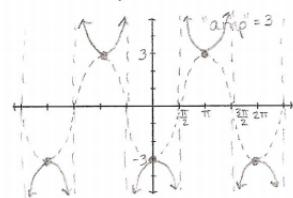
$$y = -\frac{1}{3} \cos x$$



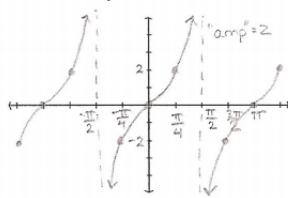
For $y = \sec x$, $y = \csc x$, $y = \tan x$, and $y = \cot x$, $|a|$ is the "amplitude" of reference points of the function. For $\sec x$ and $\csc x$, these are the maximum and minimum points, and for $\tan x$ and $\cot x$, these are the points halfway in between the zeros and vertical asymptotes.

Ex.

$$y = -3 \sec x$$

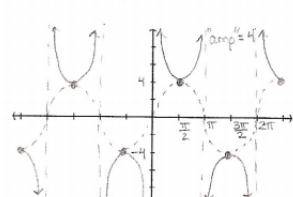


$$y = 2 \tan x$$

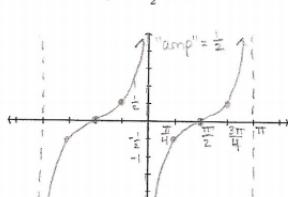


Ex.

$$y = 4 \csc x$$



$$y = -\frac{1}{2} \cot x$$



$$y = f(bx)$$

amp : $|a|$ in $y = af(x)$

The period of $y = \sin x, y = \cos x, y = \sec x$, and $y = \csc x$ is 2π . The period of $y = \tan x$ and $y = \cot x$ is π . This is how often the graph repeats itself. When x is multiplied by a constant, the period changes.

$$\text{new period} = \frac{\text{period of original function } (\pi \text{ or } 2\pi)}{|b|}$$

$$y = \sin \frac{1}{2}x$$

$$\text{per: } \frac{2\pi}{\frac{1}{2}} = 2\pi \cdot \frac{2}{1} = \boxed{4\pi}$$

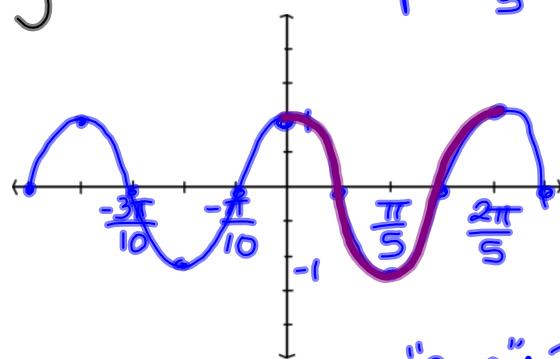
$$y = \tan \frac{\pi}{8}x$$

$$\text{per: } \frac{\pi}{\frac{\pi}{8}} = \frac{\pi}{1} \cdot \frac{8}{\pi} = \boxed{8}$$

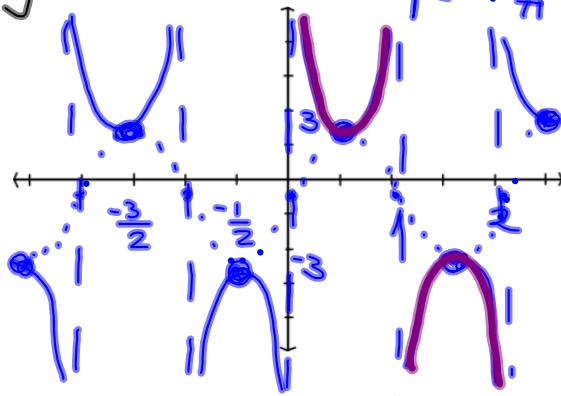
$$y = \sec \frac{259}{\pi^2}x$$

$$\begin{aligned} \text{per: } & \frac{2\pi}{\frac{259}{\pi^2}} = 2\pi \cdot \frac{\pi^2}{259} \\ & = \boxed{\frac{2\pi^3}{259}} \end{aligned}$$

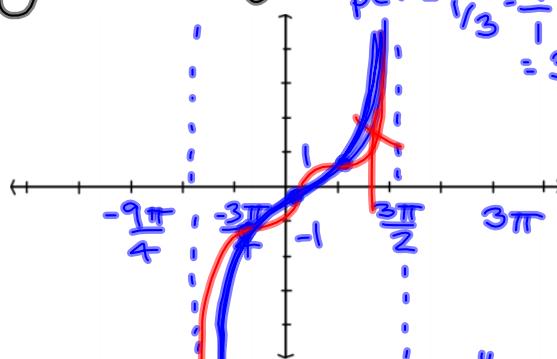
$$y = \cos 5x \quad \begin{matrix} \text{amp: } 1 \\ \text{per: } \frac{2\pi}{5} \end{matrix}$$



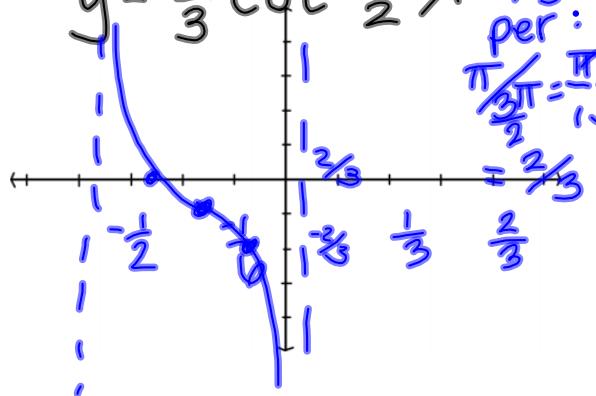
$$y = 3 \csc \pi x \quad \begin{matrix} \text{"amp": } 3 \\ \text{per: } \frac{2\pi}{\pi} = 2 \end{matrix}$$



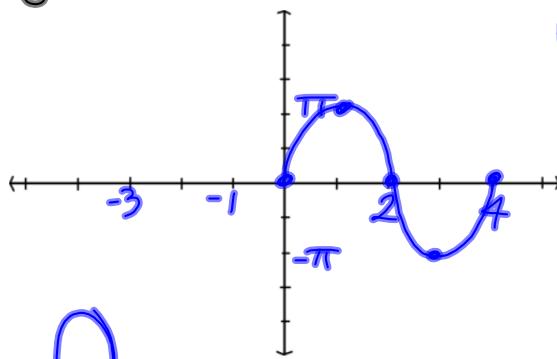
$$y = \tan \frac{1}{3}x \quad \begin{matrix} \text{"amp": } 1 \\ \text{per: } \frac{\pi}{1/3} = \frac{\pi}{1} \cdot \frac{3}{1} = 3\pi \end{matrix}$$



$$y = \frac{2}{3} \cot \frac{3\pi}{2}x \quad \begin{matrix} \text{"amp": } \frac{2}{3} \\ \text{per: } \frac{\pi}{3\pi/2} = \frac{\pi}{1} \cdot \frac{2}{3} = \frac{2}{3} \end{matrix}$$

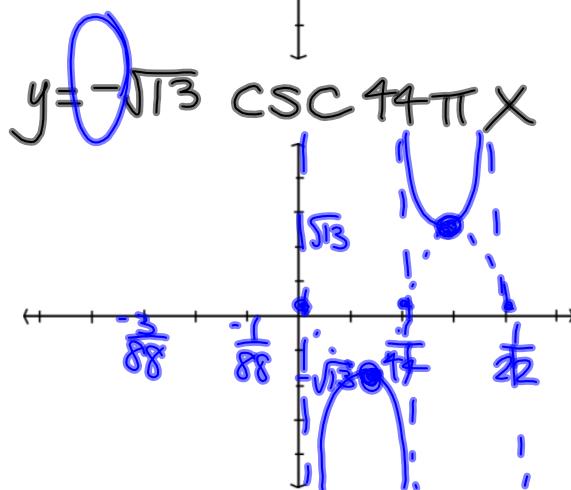


$$y = \pi \sin \frac{\pi}{2}x$$



amp : π

$$\text{per} : \frac{2\pi}{\frac{\pi}{2}} = 2\pi \cdot \frac{2}{\pi} = 4$$



amp : $\sqrt{3}$

$$\text{per} : \frac{2\pi}{44\pi} = \frac{1}{22}$$

* amplitude
is always
positive

$$y = af(bx)$$

$\text{mult} \Rightarrow$ stretching

$$y = f(x+c)+d$$

$\text{add} \Rightarrow$ shifting

d = vertical shift

If $d > 0$ up

$d < 0$ down

c = horizontal shift

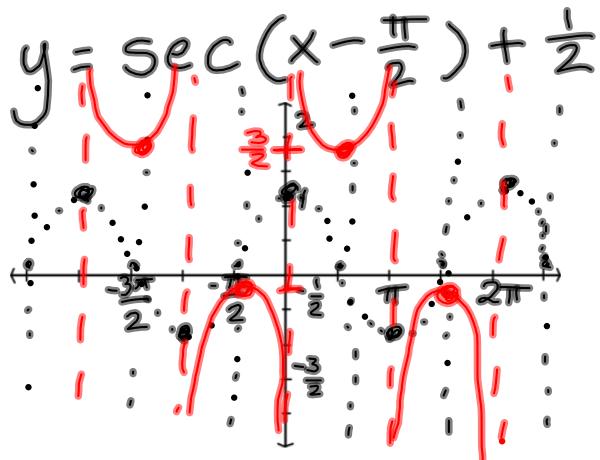
$c > 0$ left

$c < 0$ right

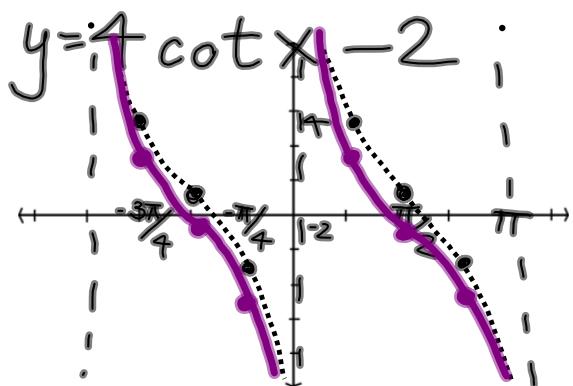
$$g = x^2 \text{ v. } y = (x+1)^2$$

coeff's outside \Rightarrow
vertical as you would expect;

inside \Rightarrow
horizontal, opposite of what you expect

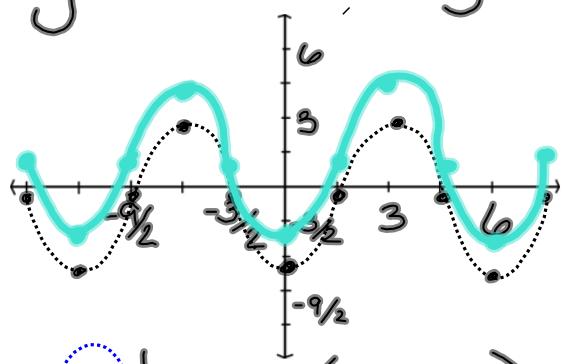


"amp": 1
per: 2π
horizontal shift: right $\frac{\pi}{2}$
vertical shift: up $\frac{1}{2}$



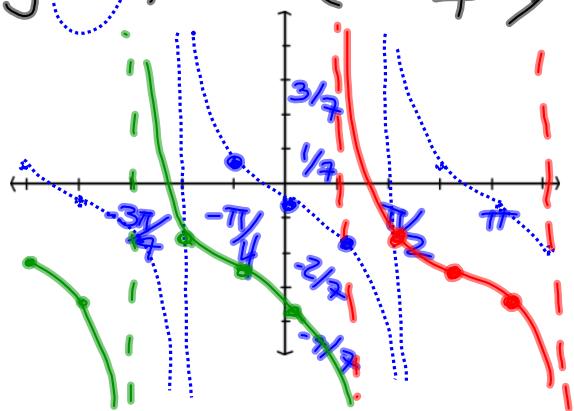
"amp": 4
per: π
h. shift: none
v. shift: down 2

$$y = -3 \cos \frac{\pi}{3}x + \frac{3}{2}$$



amp: 3
per: $\frac{2\pi}{\pi/3} = \frac{2\pi}{\frac{\pi}{3}} = 6$
h. shift: none
v. shift: up $3/2$

$$y = -\frac{1}{7} \tan\left(x - \frac{3\pi}{4}\right) - \frac{2}{7}$$



"amp": $1/7$
per: π
h. shift: right $\frac{3\pi}{4}$
v. shift: down $\frac{2}{7}$

HW : #19-52

(at a minimum, do
through #36 for
tomorrow)