

e 1.  $\tan(a + b) =$

$$\frac{\sin^2 x + \cos^2 x}{\sin^2 x} = 1$$

a.  $1 - \sin^2 x$

d 2.  $\csc^2 x =$

b.  $\cos a \cos b - \sin a \sin b$

i 3.  $\sin(a + b) =$

c.  $1 - 2\sin^2 x$

h 4.  $\sec^2 x =$

d.  $1 + \cot^2 x$

j 5.  $\sin(a - b) =$

e.  $\frac{\tan a + \tan b}{1 - \tan a \tan b}$

b 6.  $\cos(a + b) =$

f.  $\frac{\tan a - \tan b}{1 + \tan a \tan b}$

C 7.  $\cos 2x =$

g.  $\cos a \cos b + \sin a \sin b$

a 8.  $\cos^2 x =$

h.  $1 + \tan^2 x$

f 9.  $\tan(a - b) =$

i.  $\sin a \cos b + \cos a \sin b$

g 10.  $\cos(a - b) =$

j.  $\sin a \cos b - \cos a \sin b$

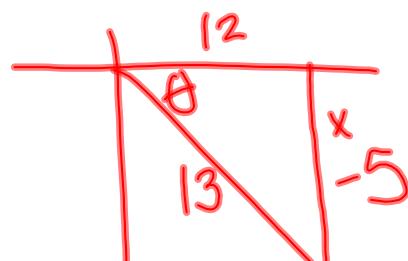
11. Find  $\cos 2\theta$  given that  $\cos \theta = \frac{12}{13}$  and  $\theta$  is in Quadrant IV.

$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta$$

$$= \left(\frac{12}{13}\right)^2 - \left(-\frac{5}{13}\right)^2$$

$$= \frac{144}{169} - \frac{25}{169}$$

$$= \boxed{\frac{119}{169}}$$



$$12^2 + x^2 = 13^2$$

$$144 + x^2 = 169$$

$$x^2 = 25$$

$$x = 5$$

12. Use the half-angle identity to evaluate  $\tan \frac{11\pi}{12}$  exactly.

$$\begin{aligned} \tan \frac{x}{2} &= \frac{1 - \cos x}{\sin x} & \frac{11\pi}{12} &= \frac{x}{2} \\ \tan \frac{\frac{11\pi}{6}}{2} &= \frac{1 - \cos \frac{11\pi}{6}}{\sin \frac{11\pi}{6}} & 2 \left( \frac{11\pi}{12} \right) &= x \\ &= \frac{1 - \frac{\sqrt{3}}{2}}{-\frac{1}{2}} = \left( 1 - \frac{\sqrt{3}}{2} \right) \cdot (-2) & \frac{11\pi}{6} &= x \\ &= -2 + \sqrt{3} & \text{Diagram: A right triangle with hypotenuse } \sqrt{3}, \text{ angle } 30^\circ, \text{ and side } -1. \end{aligned}$$

$$\frac{2 - \frac{\sqrt{3}}{2}}{-\frac{1}{2}}$$

$$\frac{2 - \sqrt{3}}{2} \cdot \frac{-1}{-1} = -2 + \sqrt{3}$$

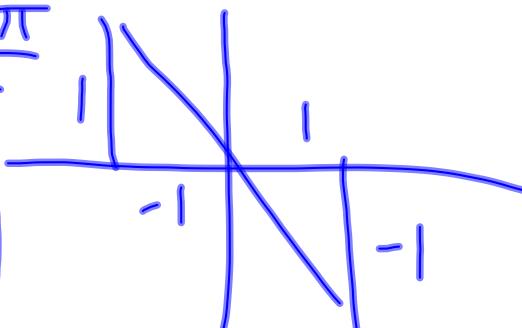
13. Find all solutions (in radians) in the interval  $0 \leq x < 2\pi$ .  $\tan(2x) + 1 = 0$

$$\tan(2x) = -1$$

go around unit circle x2 looking for solutions!

$$2x = \frac{3\pi}{4}, \frac{7\pi}{4}, \frac{11\pi}{4}, \frac{15\pi}{4}$$

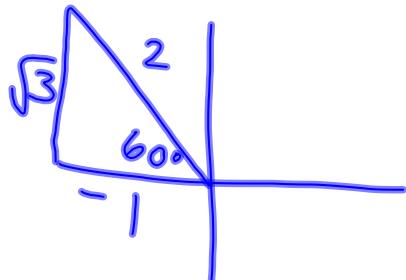
$$x = \frac{3\pi}{8}, \frac{7\pi}{8}, \frac{11\pi}{8}, \frac{15\pi}{8}$$



14. Find the exact value of  $\frac{\tan 218^\circ - \tan 98^\circ}{1 + \tan 218^\circ \tan 98^\circ}$ .

$$\tan(a-b) = \frac{\tan a - \tan b}{1 + \tan a \tan b} \quad a = 218^\circ \quad b = 98^\circ$$

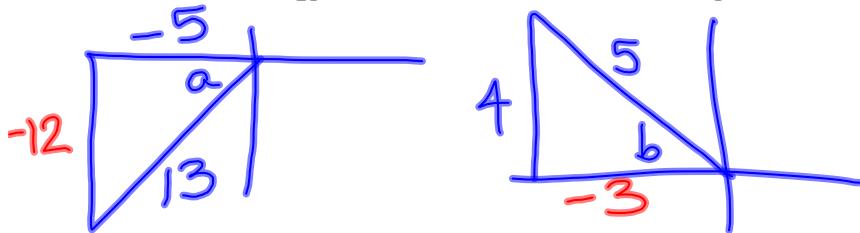
$$\tan(218^\circ - 98^\circ) = \tan 120^\circ = -\sqrt{3}$$



15. Prove the identity. Show ALL steps  
 $\cot x \cos 2x = \cot x - \sin 2x$

$$\begin{aligned}
 \text{LHS} &= \cot x (1 - 2\sin^2 x) \\
 &= \cot x - 2\sin^2 x \cot x \\
 &= \cot x - 2\sin^2 x \cdot \frac{\cos x}{\sin x} \\
 &= \cot x - \sin 2x \\
 &= \text{RHS}
 \end{aligned}$$

16. Given  $\cos a = -\frac{5}{13}$ ,  $a$  is in Quadrant III,  $\sin b = \frac{4}{5}$ , and  $b$  is in Quadrant II, find  $\sin(a - b)$ .

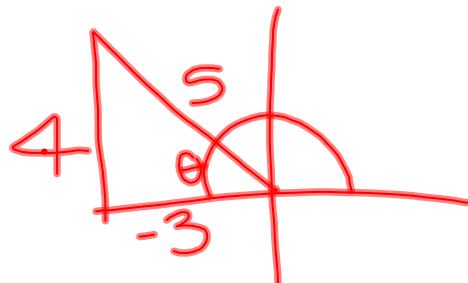


$$\begin{aligned}\sin(a-b) &= \sin a \cos b - \cos a \sin b \\ &= \left(-\frac{12}{13}\right)\left(\frac{-3}{5}\right) - \left(-\frac{5}{13}\right)\left(\frac{4}{5}\right) \\ &= \frac{36}{65} + \frac{20}{65} = \boxed{\frac{56}{65}}\end{aligned}$$

17. Evaluate  $\sin\left(\sec^{-1}\left(-\frac{5}{3}\right)\right)$ .

$$\theta$$

$$= \boxed{\frac{4}{5}}$$



18. Find all solutions (in radians) in the interval  $0 \leq x < 2\pi$ .  $\cos x = 2 \sin^2 x \cos x$

$$0 = 2 \sin^2 x \cos x - \cos x$$

$$0 = \cos x (2 \sin^2 x - 1)$$

$$\cos x = 0 \quad 2 \sin^2 x - 1 = 0$$

$$\sin^2 x = \frac{1}{2}$$

$$x = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$$

$$\sin x = \pm \frac{1}{\sqrt{2}}$$

$$x = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$$

19. Prove the identity. Show ALL steps

$$\frac{1 + 2 \cos^2 x}{\sin^2 x} = 3 \csc^2 x - 2$$

$$\frac{\sin^2 x + \cos^2 x}{\sin^2 x}$$

$$1 + \cot^2 x = \csc^2 x$$

$$\cot^2 x = \csc^2 x - 1$$

$$LHS = \frac{1}{\sin^2 x} + \frac{2 \cos^2 x}{\sin^2 x} = \csc^2 x + 2 \cot^2 x =$$

$$= \csc^2 x + 2(\csc^2 x - 1) = \csc^2 x + 2 \csc^2 x - 2 =$$

$$= 3 \csc^2 x - 2 = RHS \checkmark$$

$$LHS = \frac{1 + 2(1 - \sin^2 x)}{\sin^2 x} = \frac{1 + 2 - 2 \sin^2 x}{\sin^2 x} =$$

$$= \frac{3 - 2 \sin^2 x}{\sin^2 x} = \frac{3}{\sin^2 x} - \frac{2 \sin^2 x}{\sin^2 x} = 3 \csc^2 x - 2 = RHS$$

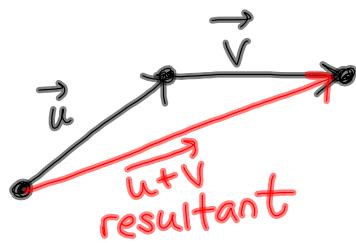
## 7.5, 7.6 - Vectors

A vector is a directed line segment;  
it has a unique length (magnitude) and direction angle



### Vector Addition:

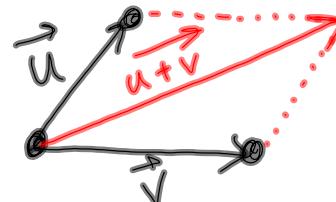
Vectors can be added using the  
Triangle Method or the



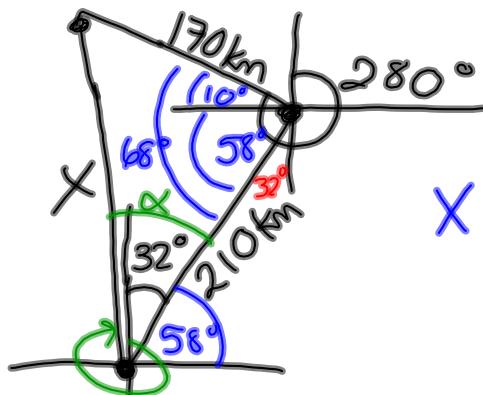
positioning tail/initial pt  
of  $\vec{v}$  at the head/terminal  
pt. of  $\vec{u}$

### Parallelogram Method

position both vectors  
so they have the same  
initial point



7.5 #28. An airplane flies  $032^\circ$  for 210 km, and then  $280^\circ$  for 170 km. How far is the plane then, from the starting point, and in what direction?



$$x = \sqrt{170^2 + 210^2 - 2(170)(210) \cdot \cos 68^\circ}$$

$$\frac{\sin \alpha}{170} = \frac{\sin 68^\circ}{x}$$

$$\alpha = \sin^{-1} \left( \frac{170 \sin 68^\circ}{x} \right)$$

**Homework:**

- "Chapter 5 Test" on pages 526-527 of your textbook
- "Chapter 6 Test" on page 591 of your textbook  
**(to be collected on Wednesday)**
- **Read sections 7.5 and 7.6 before class tomorrow**  
**(Tuesday)**