

5. Graph $\frac{1}{2} \tan\left(\frac{1}{3}x - \frac{\pi}{4}\right) + \frac{3}{2}$

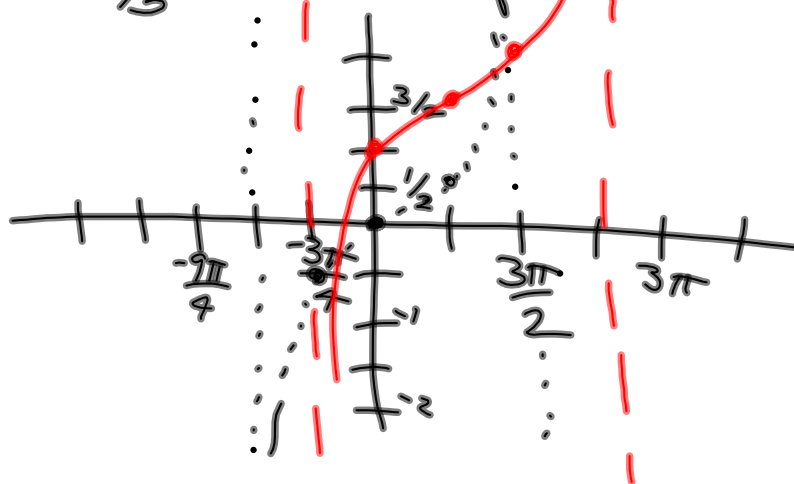
$= \frac{1}{2} \tan\frac{1}{3}\left(x - \frac{3\pi}{4}\right) + \frac{3}{2}$

"amp": $\frac{1}{2}$

period: $\frac{\pi}{1/3} = 3\pi$

right $3\pi/4$

up $3/2$



9. Prove. $\frac{\sin x - \cos x}{\cos^2 x} = \frac{\tan^2 x - 1}{\sin x + \cos x}$

RHS = $\frac{\sec^2 x - 1}{\sin x + \cos x}$

$\sin^2 x + \cos^2 x = 1$
 $\tan^2 x + 1 = \sec^2 x$
 $\tan^2 x = \sec^2 x - 1$

$= \frac{\sec^2 x - 2 \sin x \cos x}{\sin x + \cos x} \cdot \frac{\sin x - \cos x}{\sin x - \cos x}$
 $= \frac{\left(\frac{1}{\cos^2 x} - \frac{2 \cos x \sin x}{\cos^2 x}\right) (\sin x - \cos x)}{(\sin x + \cos x)(\sin x - \cos x)}$

$= \frac{\left(\frac{1 - 2 \cos^2 x}{\cos^2 x}\right) (\sin x - \cos x)}{(\sin^2 x - \cos^2 x)}$

$\cos^2 x = 2 \cos^2 x - 1$
 $= \cos^2 x - \sin^2 x$

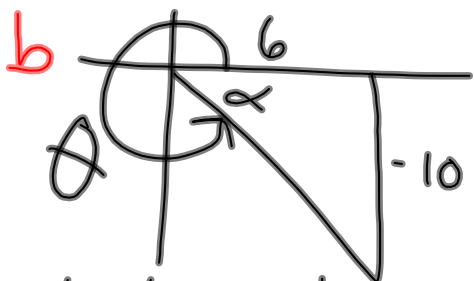
$= \frac{\sin x - \cos x}{\cos^2 x} \cdot \frac{1 - 2 \cos^2 x}{\sin^2 x - \cos^2 x}$

$= \frac{\sin x - \cos x}{\cos^2 x} \cdot \frac{-\cos^2 x}{-\cos^2 x} = \text{LHS}$

$$19. \vec{v} = \langle 6, -10 \rangle$$

$$\sqrt{136} = 2\sqrt{34}$$

$$a) |\vec{v}| = \sqrt{a^2 + b^2} = \sqrt{6^2 + 10^2} = \sqrt{136} = 2\sqrt{34}$$

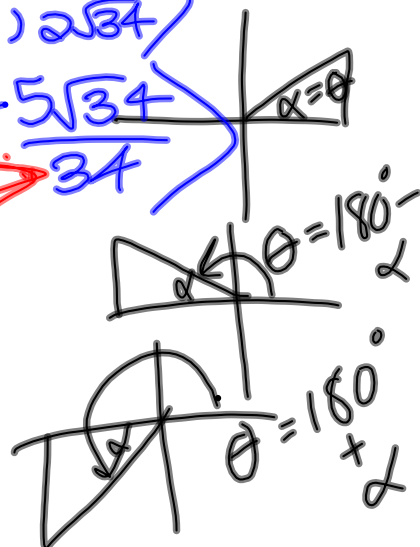


$$\alpha = \left| \tan^{-1} \frac{b}{a} \right| = \tan^{-1} \left(\frac{10}{6} \right)$$

$$\theta = 360^\circ - \alpha$$

$$c) \vec{u} = \left\langle \frac{6}{2\sqrt{34}}, \frac{-10}{2\sqrt{34}} \right\rangle$$

$$= \left\langle \frac{3\sqrt{34}}{34}, \frac{-5\sqrt{34}}{34} \right\rangle$$



7.6

#67 $\vec{a} = \vec{i} + \vec{j}$; $\vec{b} = 2\vec{i} - 3\vec{j}$

angle between \vec{a} & \vec{b}

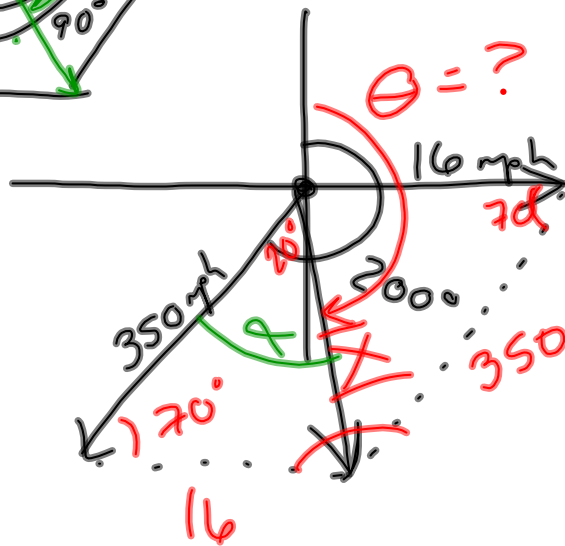
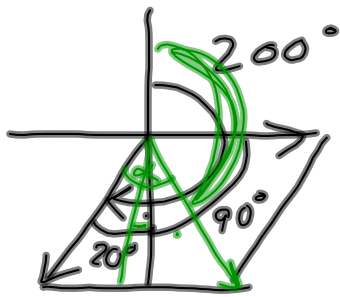
$$\theta = \cos^{-1} \left(\frac{\vec{a} \cdot \vec{b}}{|\vec{a}| |\vec{b}|} \right) = \cos^{-1} \left(\frac{-1}{\sqrt{26}} \right)$$

$$\vec{a} \cdot \vec{b} = 1(2) + 1(-3) = -1$$

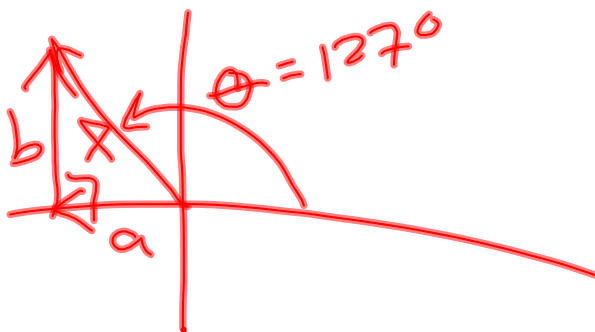
$$|\vec{a}| = \sqrt{1^2 + 1^2} = \sqrt{2}$$

$$|\vec{b}| = \sqrt{2^2 + (-3)^2} = \sqrt{13}$$

$$= 101.3^\circ$$



$$X = \sqrt{16^2 + 350^2 - 2(16)(350)\cos 70^\circ}$$



$$\cos 127^\circ = \frac{a}{4}$$

$$a = 4 \cos 127^\circ = \sim$$

$$\sin 127^\circ = \frac{b}{4}$$

$$b = 4 \sin 127^\circ = \sim$$

$$a\vec{i} + b\vec{j}$$