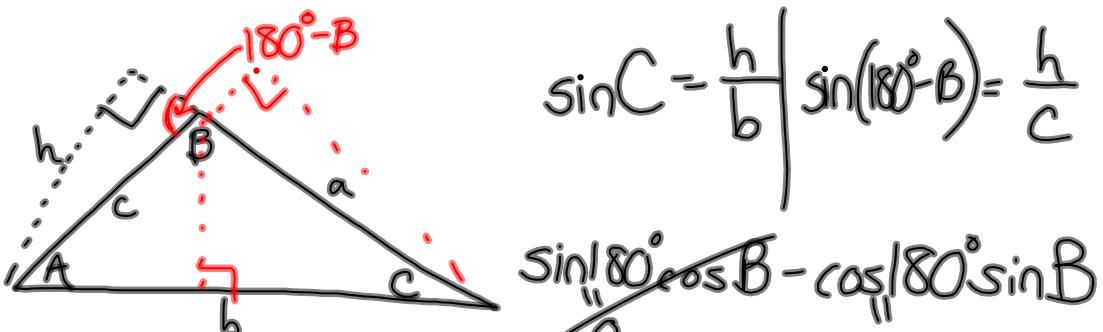


## 7.1 The Law of Sines

Solving oblique (not right) triangles.



$$\sin C = \frac{h}{b} \quad | \quad \sin(180^\circ - B) = \frac{h}{c}$$

$$\sin C = \frac{h}{b}, \quad \sin B = \frac{h}{c}$$

$$h = b \sin C, \quad h = c \sin B$$

~~$$\frac{b \sin C}{b c} = \frac{c \sin B}{b c}$$~~

~~$$\frac{\sin C}{c} = \frac{\sin B}{b}$$~~

~~$$\frac{b \sin C}{\sin B \sin C} = \frac{c \sin B}{\sin B \sin C}$$~~

~~$$\frac{b}{\sin B} = \frac{c}{\sin C}$$~~

# The Law of Sines :

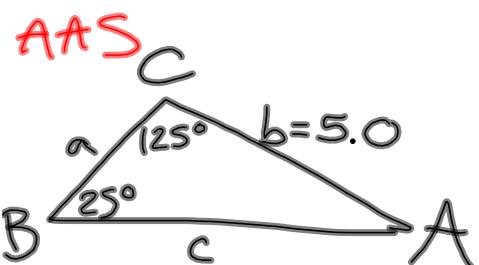
$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

OR

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

## 7.1 hardout

2.  $B=25^\circ$ ,  $C=125^\circ$ ,  $b=5.0$



$$A = 180^\circ - 125^\circ - 25^\circ \\ = 30^\circ$$

$$\frac{c}{\sin C} = \frac{b}{\sin B}$$

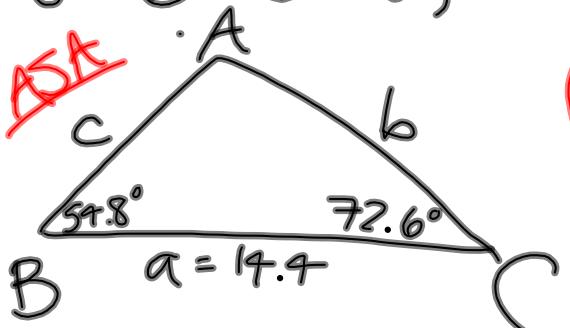
$$\frac{a}{\sin 30^\circ} = \frac{5}{\sin 25^\circ}$$

$$\frac{c}{\sin 125^\circ} = \frac{5}{\sin 25^\circ}$$

$$a = \frac{5 \sin 30^\circ}{\sin 25^\circ} \approx 5.9$$

$$c = \frac{5 \sin 125^\circ}{\sin 25^\circ} \approx 9.7$$

8.  $B = 54.8^\circ$ ,  $C = 72.6^\circ$ ,  $a = 14.4$



$$\begin{aligned} A &= 180^\circ - 54.8^\circ - 72.6^\circ \\ &= 52.6^\circ \end{aligned}$$

$$\frac{b}{\sin 54.8^\circ} = \frac{14.4}{\sin 52.6^\circ}$$

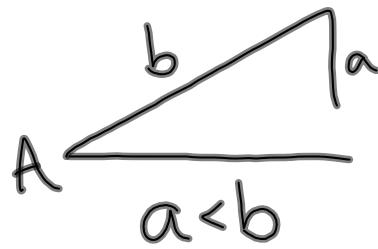
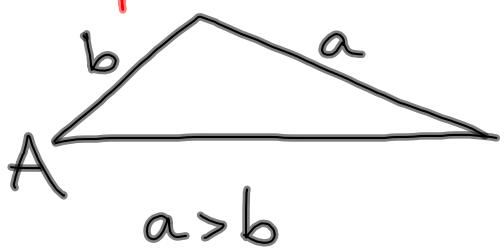
$$\begin{aligned} b &= \frac{14.4 \sin 54.8^\circ}{\sin 52.6^\circ} \\ &\approx 14.8 \end{aligned}$$

$$\frac{c}{\sin 72.6^\circ} = \frac{14.4}{\sin 52.6^\circ}$$

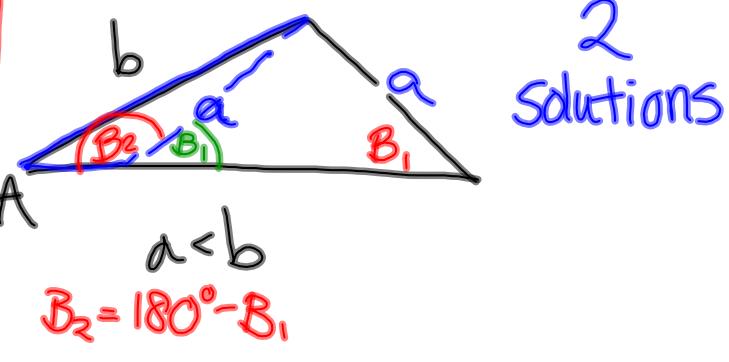
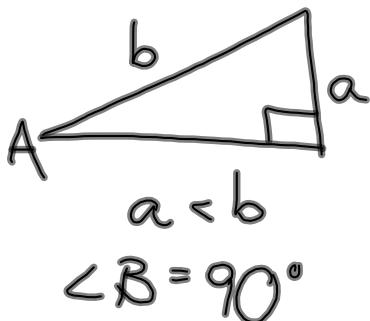
$$\begin{aligned} c &= \frac{14.4 \sin 72.6^\circ}{\sin 52.6^\circ} \\ &\approx 17.3 \end{aligned}$$

## ASS - Problematic $\triangle$

one possible solution:



no Solution



2 Solutions

14.  $B = 32^\circ, c = 14, b = 9$

$$\frac{\sin C}{14} = \frac{\sin 32^\circ}{9}$$

$$\sin C = \frac{14 \sin 32^\circ}{9}$$

$$\sin^{-1}(\sin C) = \sin^{-1}\left(\frac{14 \sin 32^\circ}{9}\right)$$

$$C = \sin^{-1}\left(\frac{14 \sin 32^\circ}{9}\right) \approx 55.5^\circ$$

$$A = 180^\circ - 32^\circ - 55.5^\circ = 92.5^\circ$$

$$\frac{a}{\sin 92.5^\circ} = \frac{9}{\sin 32^\circ}$$

$$a = \frac{9 \sin 92.5^\circ}{\sin 32^\circ} \approx 17$$


---

Case 2

$$LC_2 = 180^\circ - 55.5^\circ = 124.5^\circ$$

$$\frac{c}{\sin 124.5^\circ} = \frac{9}{\sin 32^\circ}$$

$$c = \frac{9 \sin 124.5^\circ}{\sin 32^\circ} \approx$$

2 case soln  
- more tomorrow!

7.1 book

1, 2, 4, 6, 7, 10