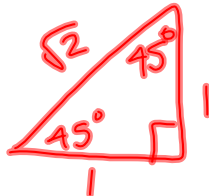


Review:

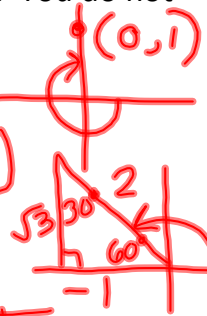
A reference angle for an angle whose initial side is on the positive x-axis and terminal side may lie in any of the four quadrants is positive acute angle between the terminal side of the angle and the x-axis

Evaluate the following trigonometric expressions. Give exact answers. You do not have to rationalize. Draw a picture if this helps you.

$\sin 45^\circ$   
 $\frac{1}{\sqrt{2}}$



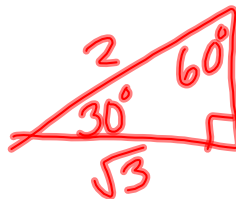
$\sec(-270^\circ) = \frac{1}{\cos(-270^\circ)}$   
 $= \frac{1}{0} = \text{undefined}$



$\tan 60^\circ$   
 $\sqrt{3}$

$\cot(120^\circ)$   
 $-\frac{1}{\sqrt{3}}$

$\sec 45^\circ$   
 $\sqrt{2}$



$\csc(-135^\circ)$   
 $\frac{1}{\sin(-135^\circ)} = -\sqrt{2}$

$\csc 30^\circ$   
 $2$

$\tan(540^\circ) = \frac{\sin(540^\circ)}{\cos(540^\circ)} = \frac{0}{-1} = 0$



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17 total possible points; grades out of 15 points

Quiz #1 Solutions

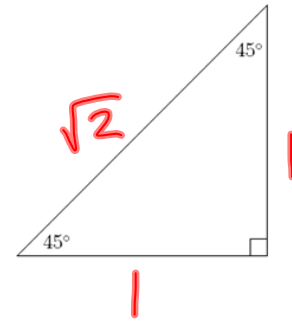
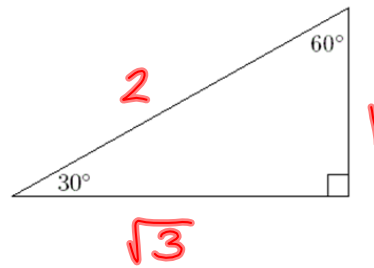
$$\frac{1}{\sec x} = \cos x$$

$$\frac{\sin x}{\cos x} = \tan x$$

$$\frac{1}{\sin x} = \csc x$$

$$\csc(90^\circ - x) = \sec x$$

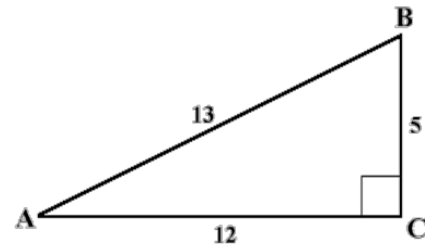
$$\tan(90^\circ - x) = \cot x$$



$$\sin B = \frac{12}{13}$$

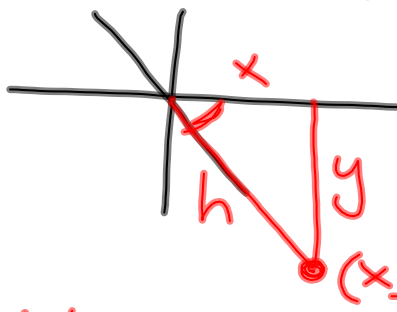
$$\tan A = \frac{5}{12}$$

$$\csc A = \frac{13}{5}$$



$$ax + by = c \quad \text{Q IV}$$

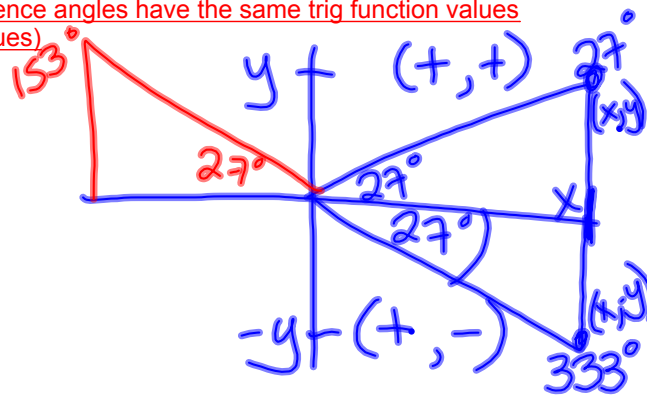
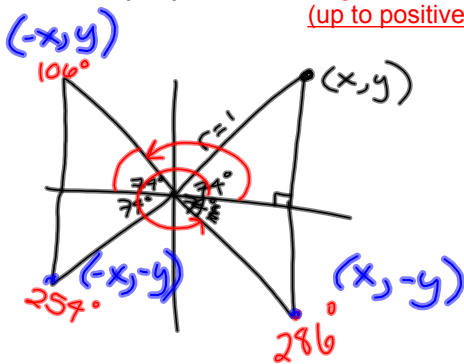
1. rewrite as  $y = mx + b$



2. pick a point on line

## 5.3 Wrap-up

Angles with the same reference angles have the same trig function values  
(up to positive/negative values)



80. Given that  $\sin 27^\circ \approx 0.4540$ ,  $\cos 27^\circ \approx 0.8910$ , and  $\tan 27^\circ \approx 0.5095$ ,  
find the trigonometric function values for  $333^\circ$ .

$333^\circ$  has a  $27^\circ$  reference angle.

$$\begin{aligned}\cos 153^\circ &= -\cos 27^\circ \\ \sin 153^\circ &= \sin 27^\circ\end{aligned}$$

$$\sin 333^\circ = -\sin 27^\circ = -0.4540$$

$$\cos 333^\circ = \cos 27^\circ = 0.8910$$

$$\tan 333^\circ = -\tan 27^\circ = -0.5095$$

## 5.4 Radians

The circumference of a circle of radius  $r$  is given by the equation:

$$C = 2\pi r$$

Therefore, the unit circle, which has radius 1, has circumference:

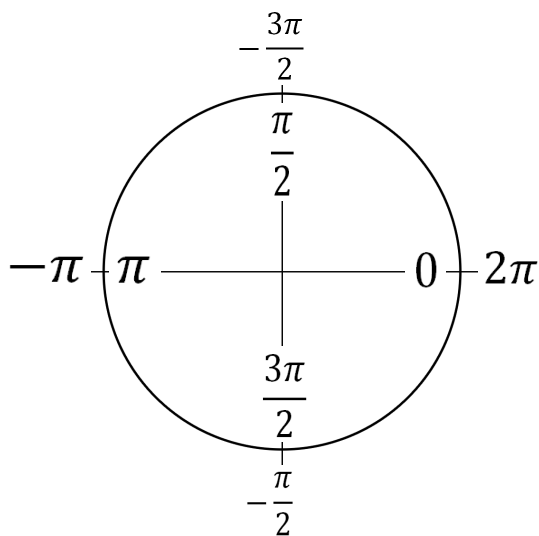
$$2\pi$$

The irrational number pi is approximately:  $\pi \approx 3.14$

Therefore  $2\pi \approx 6.28$

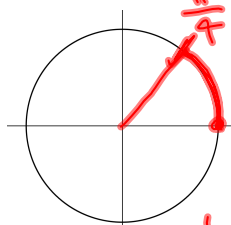
$$4\pi \approx 12.56$$

If we think about these numbers as corresponding to arc lengths around the unit circle, in which quadrant (or on which axis) do we end up?



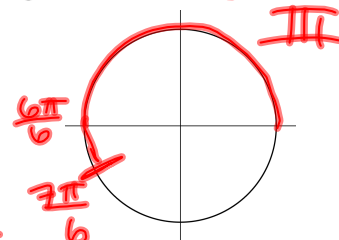
$$\frac{\pi}{4}$$

I



$$\frac{7\pi}{6}$$

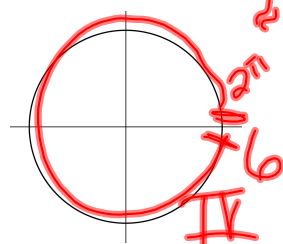
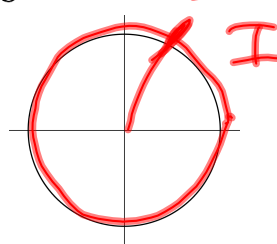
$$= \frac{6\pi}{6} + \frac{\pi}{6}$$



$$\frac{7\pi}{3}$$

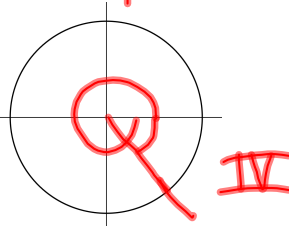
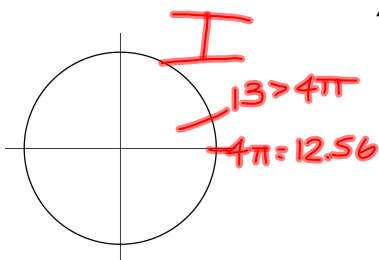
$$= \frac{6\pi}{3} + \frac{\pi}{3}$$

6



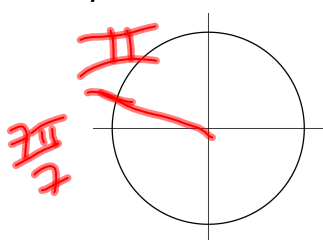
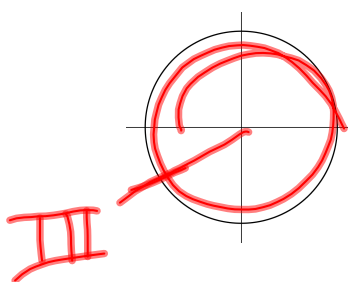
13

$$-\frac{9\pi}{4} = -\frac{8\pi}{4} - \frac{\pi}{4}$$



$$\frac{19\pi}{6} = \frac{18\pi}{6} + \frac{\pi}{6}$$

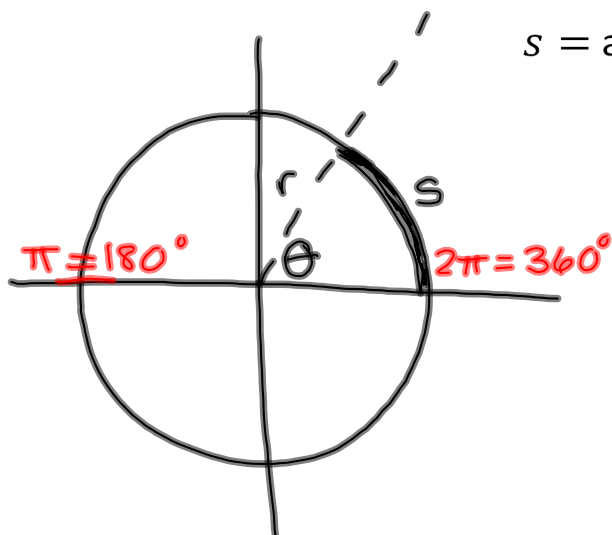
$$\frac{6\pi}{7} = \frac{6}{7}\pi$$



What is a radian?

$r$  = radius length

$s$  = arc length



When  $s = r$ , we say that the corresponding angle  $\theta$  which is subtended by arc  $s$  has measure 1 radian.

$$1 \text{ radian} \approx 57.3^\circ$$

$$\pi = 180^\circ$$

$$2\pi = 360^\circ$$

Note that  $\theta$  is independent of the radius length and any unit of measurement. Therefore radians have no associated units, and any angle measure without a degree symbol is assumed to be in radians.

### Converting between radians and degrees

$$\pi = 180^\circ \quad \therefore \quad \frac{\pi}{180^\circ} = 1 = \frac{180^\circ}{\pi}$$

Convert  $225^\circ$  to radians.

$$\overset{5}{\cancel{5}} \cdot 225^\circ \cdot \frac{\pi}{\overset{5}{\cancel{5}} \cdot 180^\circ} = \boxed{\frac{5\pi}{4}}$$

Convert  $\frac{5\pi}{6}$  to degrees.

$$\frac{\overset{5}{\cancel{5}} \pi}{\overset{6}{\cancel{6}}} \cdot \frac{\overset{30}{\cancel{180^\circ}}}{\cancel{\pi}} = \boxed{150^\circ}$$

Convert  $120^\circ$  to radians.

$$120^\circ \cdot \frac{\pi}{180^\circ} = \boxed{\frac{2\pi}{3}}$$

Convert  $\frac{7\pi}{4}$  to degrees.

$$\frac{7\pi}{4} \cdot \frac{180^\circ}{\pi} = \boxed{315^\circ}$$

Two angles in radians are:  $90^\circ$

complementary if they sum to  $\frac{\pi}{2}$ .

supplementary if they sum to  $180^\circ$  or  $\pi$ .

coterminal if they differ by integer multiples of  $360^\circ$  or  $2\pi$ .

Find the complement and supplement of  $\frac{5\pi}{12}$ .

complement:

$$\frac{6\pi}{2} - \frac{5\pi}{12} = \frac{6\pi}{12} - \frac{5\pi}{12} = \boxed{\frac{\pi}{12}}$$

supplement:

$$\frac{12}{12}\pi - \frac{5\pi}{12} = \boxed{\frac{7\pi}{12}}$$

Find one positive and one negative angle coterminal with  $-\frac{3\pi}{4}$ .

$$\frac{-3\pi}{4} + 2\pi \cdot \frac{1}{4} = \frac{-3\pi}{4} + \frac{8\pi}{4} = \boxed{\frac{5\pi}{4}}$$

$$\frac{-3\pi}{4} - \frac{8\pi}{4} = \boxed{\frac{-11\pi}{4}}$$

Common angles:

(memorize!)

$$\frac{\pi}{6} = 30^\circ$$

$$\frac{\pi}{4} = 45^\circ$$

$$\frac{\pi}{3} = 60^\circ$$

Note:

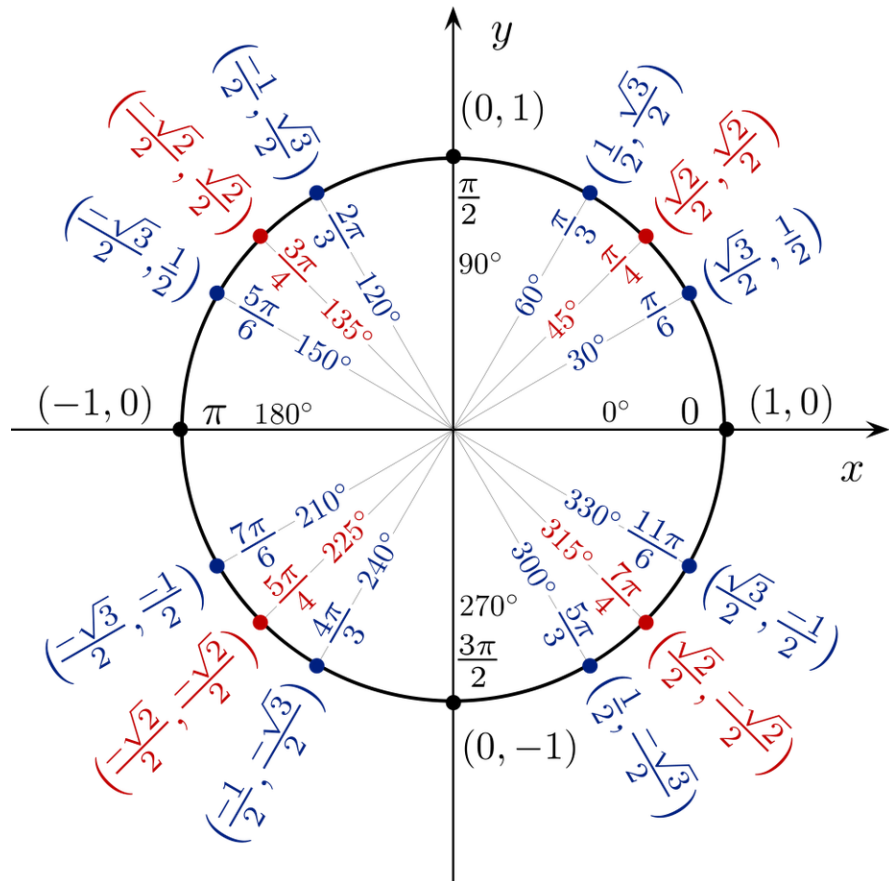
$$\frac{k\pi}{6} \rightarrow 30^\circ \text{ ref. } \angle$$

$$\frac{k\pi}{4} \rightarrow 45^\circ \text{ ref. } \angle$$

$$\frac{k\pi}{3} \rightarrow 60^\circ \text{ ref. } \angle$$

$$\frac{k\pi}{2} \rightarrow 90^\circ \text{ or } 270^\circ$$

$$k\pi \rightarrow 0^\circ \text{ for } k \text{ even;} \\ 180^\circ \text{ for } k \text{ odd}$$



### Homework:

Assigned Friday: 5.1 #

Assigned Monday: 5.3 #29-37 odd; 39-70 all;

### Assigned Tuesday:

5.3 #79-82 all - applying concept of same reference angle

5.4

#1-7 odd - determining quadrant/location of angles in radians

#9-19 odd - compliment/supplement/coterminal angles

#21,23,27,31,45,47,53 - convert between radians and degrees

### Next time:

- determine trigonometric function value of angles given in radians
- arc length/linear speed/angular speed problems

