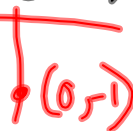


Review: Evaluate the following trigonometric expressions.

$$\tan \frac{5\pi}{2} = \frac{1}{0} = \text{undefined}$$



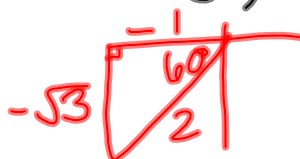
$$\sec \left( \frac{3\pi}{2} \right) = \frac{1}{0} = \text{undefined}$$



$$\sin \left( -\frac{5\pi}{6} \right) = -\frac{1}{2}$$



$$\csc \left( \frac{4\pi}{3} \right) = -\frac{2}{\sqrt{3}}$$



$$\cos \left( -\frac{5\pi}{4} \right) = \frac{-1}{\sqrt{2}}$$



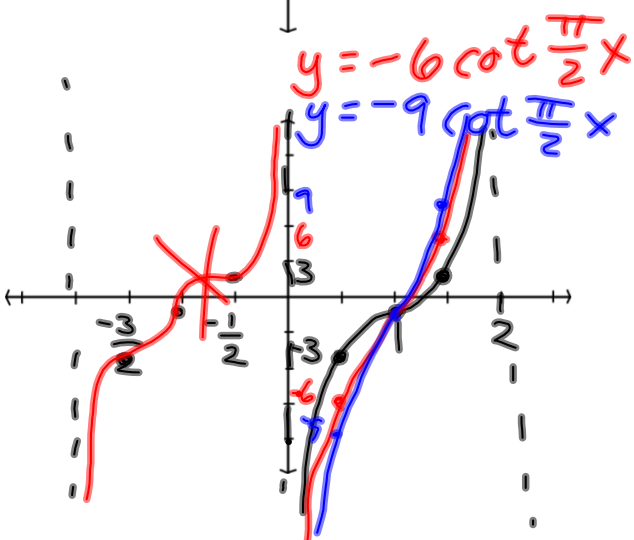
$$\cot \left( -\frac{9\pi}{4} \right) = -1$$



$$y = -3 \cot \frac{\pi}{2} x$$

"amp" = 3

$$\text{period} = \frac{\pi}{\frac{\pi}{2}} = \frac{\pi}{1} \cdot \frac{2}{\pi} = 2$$



$$y = a f(bx)$$

amplitude or

"amplitude" of relevant

reference points = |a|

$$\text{period} = \frac{\pi \text{ or } 2\pi}{|b|}$$

cot has asymptotes @ 0 & the period



$$y = -2 \sec 17x$$

$$\text{amp: } |-2| = 2$$

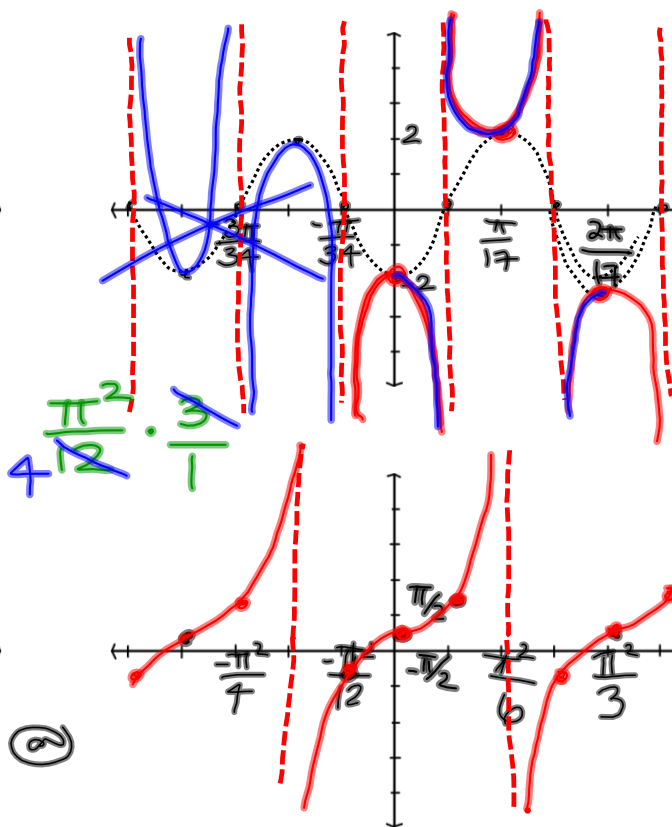
$$\text{per: } \frac{2\pi}{17}$$

$$y = \frac{\pi}{2} \tan\left(\frac{3}{\pi}x\right)$$

$$\text{amp: } \frac{\pi}{2}$$

$$\text{per: } \frac{\pi}{\frac{3}{\pi}} = \frac{\pi}{1} \cdot \frac{\pi}{3} = \frac{\pi^2}{3}$$

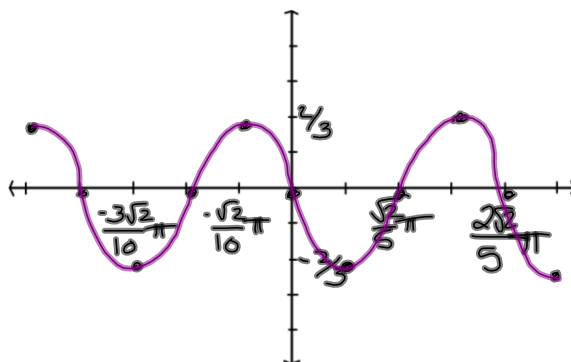
\*tangent has V.A.'s @  $\pm$  half the period



$$y = -\frac{2}{3} \sin\left(\frac{5}{\sqrt{2}}x\right)$$

$$\text{amp: } \frac{2}{3}$$

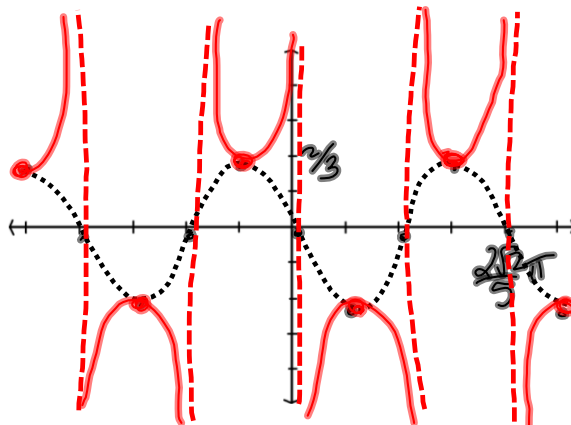
$$\text{per: } \frac{2\pi}{\frac{5}{\sqrt{2}}} = \frac{2\pi}{1} \cdot \frac{\sqrt{2}}{5} = \frac{2\sqrt{2}\pi}{5}$$



$$y = -\frac{2}{3} \csc\left(\frac{5}{\sqrt{2}}x\right)$$

$$\text{amp: } \frac{2}{3}$$

$$\text{per: } \frac{2\sqrt{2}}{5} \pi$$



$y = af(bx)$  ✓ *scaling*

ultimate goal:  $y = a [f(bx+c)] + d$

$y = f(x+c) + d$  *shifting*

outside - vertically as we would expect  
 inside - horizontally, opposite

$d =$  vertical shift  
 $d > 0$  up  
 $d < 0$  down

$c =$  horizontal shift  
 $c > 0$  left  
 $c < 0$  right



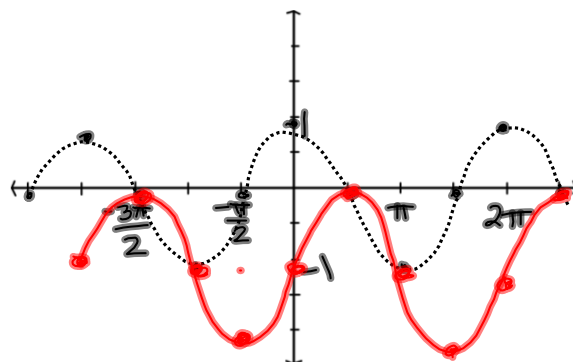
$y = \cos(x - \frac{\pi}{2}) - 1$

amp: 1

per:  $2\pi$

right  $\frac{\pi}{2}$  (1 tick)

down 1 (2 ticks)



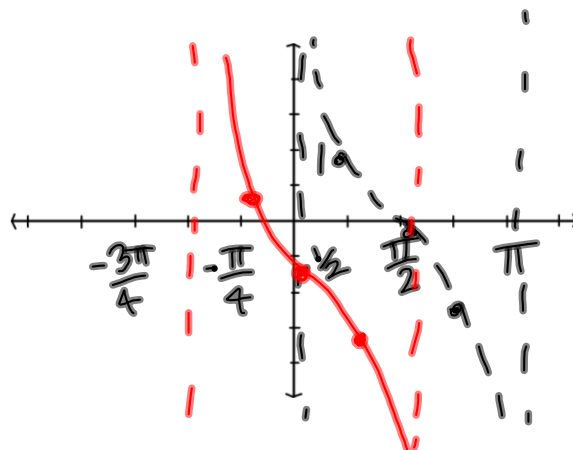
$y = \cot(x + \frac{\pi}{2}) - \frac{1}{2}$

amp: 1

per:  $\pi$

left  $\frac{\pi}{2}$

down  $\frac{1}{2}$



→ #36

