

## Solving Trigonometric Equations

Evaluate

$$\sin^{-1}\left(\frac{1}{2}\right)$$

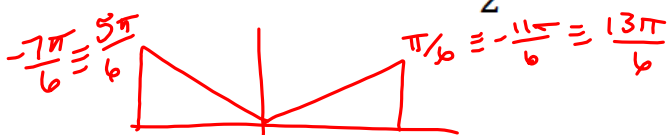
single answer  
in  $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$   
(restricted domain)  
of sine

$$\frac{\pi}{6}$$

Solve

$$\sin x = \frac{1}{2}$$

versus



infinitely many  $x$ 's  
all coterminal  
w/  $\frac{\pi}{6}$  or  $\frac{5\pi}{6}$

$$x = \frac{\pi}{6} + 2\pi k$$

$$x = \frac{5\pi}{6} + 2\pi k$$

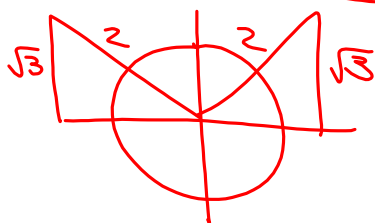
$k \in \mathbb{Z}$   
is an element of  
the set  
of integers  
(+ whole #s)

Solve for  $x \in [0, 2\pi)$ .

2.  $2 \sin x = \sqrt{3}$

$$\sin x = \frac{\sqrt{3}}{2}$$

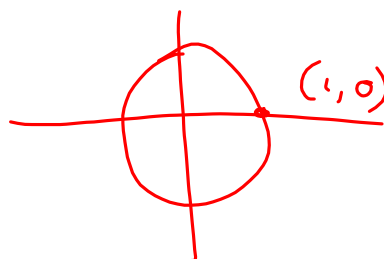
$$x = \frac{\pi}{3}, \frac{2\pi}{3}$$



4.  $\cos x - 1 = 0$

$$\cos x = 1$$

$$x = 0$$



$$6. \frac{2 \sin x \cos x}{\sin x} = \frac{\sqrt{3} \sin x}{\sin x}$$

$$2 \cos x = \sqrt{3}$$

$$\cos x = \frac{\sqrt{3}}{2}$$

~~$$x^2 = x$$

$$x = \sqrt{x}$$

$$\frac{x^2}{x} = \frac{x}{x}$$

$$x = 1$$~~

$$x^2 - x = 0$$

$$x(x-1) = 0$$

$$x = 0, x-1 = 0$$

$$x = 0, x = 1$$

### Algebra Review

$$(x - 2)(x - 3)(x - 4) = 0$$

$$\Rightarrow x - 2 = 0 \quad \text{or} \quad x - 3 = 0 \quad \text{or} \quad x - 4 = 0$$

$$\Rightarrow x = 2 \quad \text{or} \quad x = 3 \quad \text{or} \quad x = 4$$

The **Zero Product Property** states:

If  $AB = 0$ , then  $A = 0$  or  $B = 0$ .

$$x^2 = 9$$

$$x = \pm\sqrt{9} = \pm 3$$

$$\sqrt{4} = 2$$

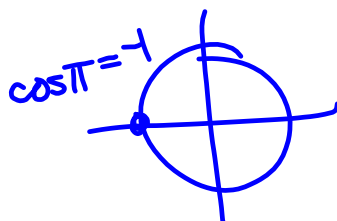
The **Square Root Theorem** states:

If  $[f(x)]^2 = c$ , then  $f(x) = \pm\sqrt{c}$

$$e^{\pi i} + 1 = 0$$

Euler's equation

$$e^{\pi i} = -1$$



$$6. 2 \sin x \cos x = \sqrt{3} \sin x$$

Solve for  $x \in [0, 2\pi)$

$$2 \sin x \cos x - \sqrt{3} \sin x = 0$$

$$\sin x (2 \cos x - \sqrt{3}) = 0$$

$$\sin x = 0$$

$$x = 0, \pi$$

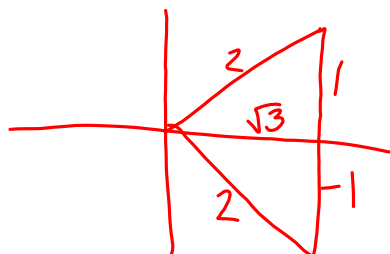
or

$$2 \cos x - \sqrt{3} = 0$$

$$2 \cos x = \sqrt{3}$$

$$\cos x = \frac{\sqrt{3}}{2}$$

$$x = \frac{\pi}{6}, \frac{11\pi}{6}$$



6.6 Solving Trigonometric Equations

Solve for all values of  $x$  in the interval  $[0, 2\pi)$

$$8. \cos^2 x - 1 = 0$$

factor

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$$-\sin^2 x = 0$$

$$\sin^2 x = 0$$

$$\sin x = 0$$

+1 & sqrt

$$\cos^2 x = 1$$

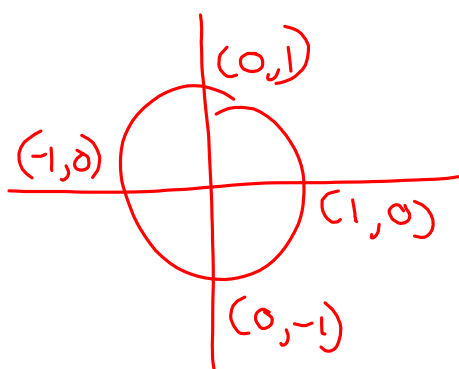
$$\cos x = \pm \sqrt{1}$$

$$\cos x = \pm 1$$

$$(\cos x - 1)(\cos x + 1) = 0$$

$$\cos x - 1 = 0, \cos x + 1 = 0$$

$$\cos x = \pm 1$$



$$x = 0, \pi$$