

$$2\sin^2 2x - \sin 2x = 0 \quad 0 \leq x < 2\pi$$

$$\sin 2x (2\sin 2x - 1) = 0 \quad 0 \leq 2x < 4\pi$$

$$\sin 2x = 0 \quad \sin 2x = \frac{1}{2}$$

$$2x = 0, \pi, 2\pi, 3\pi$$

$$x = 0, \frac{\pi}{2}, \pi, \frac{3\pi}{2}$$

$$2x = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{13\pi}{6}, \frac{17\pi}{6}$$

$$x = \frac{\pi}{12}, \frac{5\pi}{12}, \frac{13\pi}{12}, \frac{17\pi}{12}$$

$$\sin x - 1 = \cos x \sin x - \cos x$$

$$0 = \underbrace{\cos x \sin x - \cos x} - \underbrace{\sin x + 1}$$

$$0 = \cos x (\sin x - 1) - 1 (\sin x - 1)$$

$$0 = (\sin x - 1)(\cos x - 1)$$

$$\sin x = 1, \quad \cos x = 1$$

$$x = \frac{\pi}{2}$$

$$x = 0$$

$$2\sin^2 2x = 1 - \cos 2x$$

$$\begin{aligned}\sin^2 \theta + \cos^2 \theta &= 1 \\ \sin^2 \theta &= 1 - \cos^2 \theta\end{aligned}$$

$$2(1 - \cos^2 2x) = 1 - \cos 2x$$

$$2 - 2\cos^2 2x = 1 - \cos 2x$$

$$0 = 2\cos^2 2x - \cos 2x - 1$$

$$0 = (2\cos 2x + 1)(\cos 2x - 1)$$

$$\cos 2x = -1/2 \quad \cos 2x = 1$$

$$2x = \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{8\pi}{3}, \frac{10\pi}{3}$$

$$2x = 0, 2\pi$$

$$x = \frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{5\pi}{3}$$

$$x = 0, \pi$$

$$V = \frac{60 \text{ mi}}{\text{h}}, \quad r = 12 \text{ in}, \quad \omega = ? \frac{\text{rev}}{\text{min}}$$

$$\frac{V}{r} = \cancel{r} \omega \Rightarrow \omega = \frac{V}{r} = \frac{V}{1} \cdot \frac{1}{r}$$

$$\omega = \frac{60 \text{ mi}}{\text{h}} \cdot \frac{1}{12 \text{ in}} \cdot \frac{1 \text{ h}}{60 \text{ min}} \cdot \frac{12 \text{ in}}{1 \text{ ft}} \cdot \frac{5280 \text{ ft}}{1 \text{ mi}} \cdot \frac{1 \text{ rev}}{2\pi}$$

$$= \frac{2640}{\pi} \text{ rev/min}$$

$y = -3 \sec\left(2x + \frac{3\pi}{2}\right) - 1$
 $y = a f(bx+c) + d$
 amplitude: $|a|$ 3 (vert. flip)
 period: $\frac{\pi \text{ or } 2\pi}{|b|}$ $\frac{2\pi}{2} = \pi$
 vertical shift: d -1 down
 phase shift (horizontal): $-\frac{c}{b}$ $-\frac{3\pi/2}{2} = -\frac{3\pi}{4}$ left (3+uxs)

$$\frac{\sin x - \cos x}{\cos^2 x} = \frac{\tan^2 x - 1}{\sin x + \cos x}$$

$$\begin{aligned}
 \text{LHS} &= \frac{\sin x - \cos x}{\cos^2 x} \cdot \frac{\sin x + \cos x}{\sin x + \cos x} \\
 &= \frac{(\sin^2 x - \cos^2 x)}{\cos^2 x (\sin x + \cos x)} \cdot \frac{1}{\cos^2 x} = \frac{\sin^2 x - \cos^2 x}{\cos^2 x (\sin x + \cos x)} = \text{RHS}
 \end{aligned}$$

$$A=50^\circ, b=81, c=34 \quad \text{SAS}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$a = \sqrt{81^2 + 34^2 - 2(81)(34) \cos 50^\circ}$$

$$2 \cos^3 x = \cos x$$

$$2 \cos^3 x - \cos x = 0$$

$$\cos x (2 \cos^2 x - 1) = 0$$

$$\cos x = 0$$

$$x = \frac{\pi}{2}, \frac{3\pi}{2}$$

$$2 \cos^2 x = 1$$

$$\cos^2 x = \frac{1}{2}$$

$$\cos x = \pm \frac{1}{\sqrt{2}}$$

$$x = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$$

$$2 \cos^3 x = \cos x$$

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$$x = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$$

$$\tan \frac{x}{2} = \frac{\tan x}{\sec x + 1}$$

$$\text{LHS} = \frac{\sin x}{1 + \cos x} =$$

$$\tan \frac{x}{2} = \frac{1 - \cos x}{\sin x}$$

$$= \frac{\sin x}{1 + \cos x}$$

$$\frac{\cancel{\cos x} \cdot \sin x}{\cancel{\cos x} + \cos x} = \frac{\cos x}{\cos x} \cdot \frac{\sin x}{\left(\frac{1}{\cos x} + 1\right)} = \text{RHS}$$

$$\sin 3x \cos 3x = \frac{1}{2} \sin 6x$$

$$\sin 2\theta = 2 \sin \theta \cos \theta$$

$$\begin{aligned} \text{RHS} &= \frac{1}{2} \sin 2(3x) \\ &= \frac{1}{2} \cdot 2 \sin 3x \cos 3x \\ &= \text{LHS} \end{aligned}$$