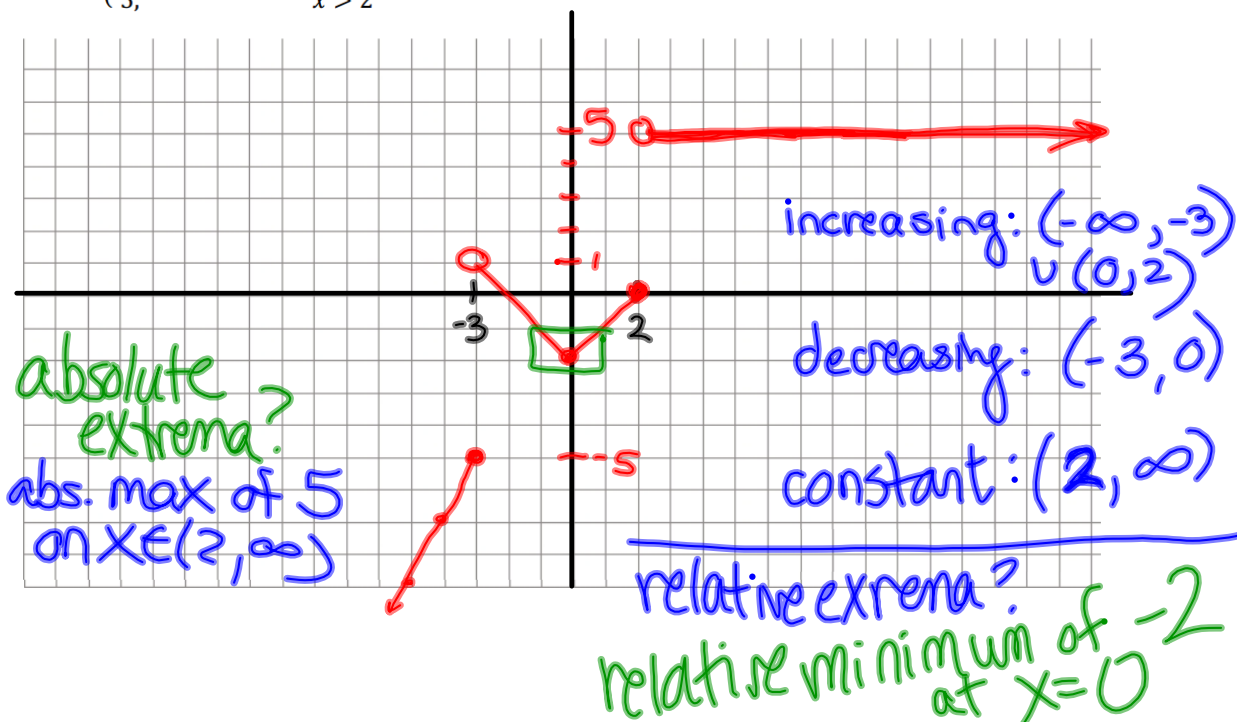


6. Graph the piecewise function and state the intervals over which the function is increasing, decreasing, or constant.

$$f(x) = \begin{cases} 2x + 1, & x \leq -3 \\ |x| - 2, & -3 < x \leq 2 \\ 5, & x > 2 \end{cases}$$



Homework questions?

10.2

29. Sum of mult's of 7 from 7 to 98, inclusive.

$$1 \cdot 7 + 7 \cdot 2 + 7 \cdot 3 + \dots + 7 \cdot 14$$

$$\sum_{n=1}^{14} 7n$$

$$\begin{aligned} S_n &= \frac{n}{2} (a_1 + a_n) \\ &= \frac{14}{2} (7 + 98) = \boxed{735} \end{aligned}$$

10.2

$$36. \sum_{k=2}^{50} (2000 - 3k)$$

$$a_1 = 2000 - 3(2)$$

$$a_n = 2000 - 3(50)$$

$$n = 49$$

$$S_{49} = \frac{49}{2} (2000 - 3(2) + 2000 - 3(50)) =$$

$$= 94,178$$

Geometric Sequences/Series:

10.3

Definition: A sequence is geometric if there is a number r , called the **common ratio**, such that

$$\frac{a_{n+1}}{a_n} = r, \text{ or } a_{n+1} = a_n r, \text{ for any integer } n \geq 1.$$

The **nth term of a geometric sequence** is given by

$$a_n = a_1 r^{n-1}, \text{ for any integer } n \geq 1.$$

The **sum of the first n terms** of a geometric sequence is given by

$$S_n = \frac{a_1(1-r^n)}{1-r}, \text{ for any } r \neq 1.$$

When $|r| < 1$, the **limit or sum of an infinite geometric series** is given by

$$S_\infty = \frac{a_1}{1-r}$$

$$18, -6, 2, \frac{-2}{3}$$

common ratio: $r = -\frac{1}{3}$

$$2, -10, +50, -250, \dots$$

find the 9th term:

$$a_n = a_1 r^{n-1}$$

$$a_9 = 2 \cdot (-5)^{9-1} = 2(-5)^8 = \boxed{781,250}$$

$$16 - 8 + 4 - 2 + \dots$$

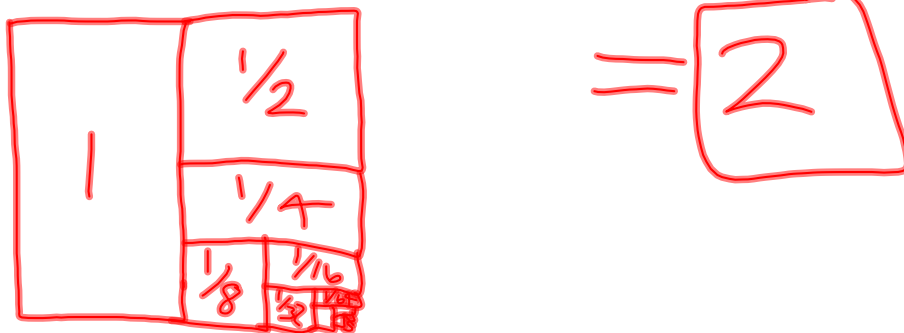
Find the sum of the first 10 terms.

$$S_n = \frac{a_1(1-r^n)}{1-r}$$

$$S_{10} = \frac{16 \left(1 - \left(-\frac{1}{2}\right)^{10}\right)}{1 - \left(-\frac{1}{2}\right)} = \frac{16 \left(1 - \frac{1}{2^{10}}\right)}{\frac{3}{2}}$$

$$\frac{2}{3} \cdot 16 \left(1 - \frac{1}{1024}\right) = \boxed{\frac{341}{32} \approx 10.65625}$$

$$\begin{aligned} \left(\frac{1}{2}\right)^n &= \left(\frac{1}{2}\right)^0 + \left(\frac{1}{2}\right)^1 + \left(\frac{1}{2}\right)^2 + \dots \\ &= 1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \dots \end{aligned}$$



$$\sum_{n=0}^{\infty} \frac{1}{2^n} = 1 + \frac{1}{2} + \frac{1}{4} + \dots = 2$$

In general, when $|r| < 1$,
the sum of an infinite geometric
series is $S_{\infty} = \frac{a_1}{1-r}$

(or $S_{\infty} = \frac{a_0}{1-r}$ if series starts w/ a_0)

$$100 - 10 + 1 - \frac{1}{10} + \frac{1}{100} - \dots$$

what is the sum of this infinite geometric series?

$$S_{\infty} = \frac{a_1}{1-r}$$

$$a_1 = 100$$

$$r = -\frac{1}{10}$$

$$S_{\infty} = \frac{100}{1 - (-\frac{1}{10})}$$

$$= \frac{100}{1 + \frac{1}{10}} = \frac{100}{\frac{10}{10} + \frac{1}{10}} = \frac{100}{\frac{11}{10}}$$

$$= 100 \cdot \frac{10}{11} = \boxed{\frac{1000}{11}}$$

$$50. \sum_{k=1}^{\infty} \frac{8}{3} \left(\frac{1}{2}\right)^{k-1}$$

$$= \frac{8}{3} + \frac{4}{3} + \frac{2}{3} + \frac{1}{3} + \dots$$

$$a_1 = \frac{8}{3}, r = \frac{1}{2}$$

$$S_{\infty} = \frac{\frac{8}{3}}{1 - \frac{1}{2}} = \boxed{\frac{16}{3}}$$

Find Fraction Notation.

$$52. \quad 0.222\dots = 0.\overline{2}$$

$$0.2 + 0.02 + 0.002 + 0.0002 + \dots$$

$$2 \cdot \frac{1}{10} + 2 \cdot \frac{1}{10^2} + 2 \cdot \frac{1}{10^3} + 2 \cdot \frac{1}{10^4} + \dots$$

$$a_n = \frac{2}{10^n} \quad ; \quad a_1 = \frac{1}{5} \quad ; \quad r = \frac{1}{10}$$

$$0.\overline{2} = \frac{\frac{1}{5}}{1 - \frac{1}{10}} = \boxed{\frac{2}{9}}$$

$$54. \quad 6.1\overline{616}$$

$$6.1 \cdot 1$$

$$+ 0.061 = 6.1 \times 10^{-2} = 6.1 \left(\frac{1}{100}\right)^1$$

$$+ 0.00061 = 6.1 \times 10^{-4} = 6.1 \left(\frac{1}{100}\right)^2$$

$$+ 0.0000061 = 6.1 \times 10^{-6} = 6.1 \left(\frac{1}{100}\right)^3$$

$$a_1 = 6.1$$

$$r = \frac{1}{100}$$

$$S_{\infty} = \frac{6.1}{1 - \frac{1}{100}} = \frac{6.1}{\frac{99}{100}} = \boxed{\frac{610}{99}}$$

10.3

58. Someone offers you a job for the month of February (28 days)

You will be paid \$0.01 the 1st day, \$0.02 the 2nd day, \$0.04 the 3rd day, doubling your previous day's salary each day

$$\sum_{n=0}^{28} \frac{1}{100} \cdot 2^n = \frac{0.01(1-2^{28})}{1-2}$$

$$S_n = \frac{a_1(1-r^n)}{1-r}$$

$$= \$2,684,355$$

$$\frac{10.2}{\# 35, 37}$$

$$\frac{10.3}{\# 15, 19, 21, 25, 35, 37, 43, 45, 49, 57}$$