

$$a_{n+1} = a_n + d$$

$$a_n = a_1 + (n - 1)d$$

$$S_n = \frac{n}{2}(a_1 + a_n)$$

$$a_n = a_1 r^{n-1}$$

$$S_n = \frac{a_1(1 - r^n)}{1 - r}$$

$$S_\infty = \frac{a_1}{1 - r}$$

$$(a + b)^n = \sum_{k=0}^n \binom{n}{k} a^{n-k} b^k$$

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$

$$P(t) = P_0 e^{kt}$$

1. Find the indicated term of the sequence.

$$a_n = \left(1 + \frac{1}{n}\right)^2; a_{80} = \left(1 + \frac{1}{80}\right)^2 = \left(\frac{80+1}{80}\right)^2 = \frac{81^2}{80^2} = \frac{6561}{6400}$$

2. Predict the nth term of the sequence.

$$\begin{matrix} 2 & 3 & 4 & 5 & 6 \\ 3 & 4 & 5 & 6 & 7 & \dots \end{matrix}$$

$n^{\text{th}} \rightarrow \frac{n}{2}, \frac{n}{3}, \frac{n}{4}, \frac{n}{5}$

$$\frac{n+1}{n+2} \approx 1.025$$

3. Find and evaluate the sum.

$$\sum_{k=1}^8 (-1)^{k+1} 3k = (-1)^{1+1} \cdot 3(1) + (-1)^{2+1} \cdot 3(2) + 3(3) - 3(4) + 3(5) - 3(6) + 3(7) - 3(8) = -12$$

4. Write sigma notation for the series.

$$4 - 9 + 16 - 25 + \dots + (-1)^n n^2$$

$$\sum_{i=2}^n (-1)^i i^2 \quad \sum_{i=1}^n (-1)^{i+1} (i+1)^2$$

5. Write the 4th term of $(2x + y)^5$.

$$\begin{aligned} a &= 2x \\ b &= y \\ n &= 5 \\ k &= 3 \end{aligned}$$

$$\binom{5}{3} (2x)^{5-3} (y)^3$$

$$\frac{5!}{3!(5-3)!} (2x)^2 y^3 = \frac{5!}{3! \cdot 2!} (4x^2 y^3)$$

$$= \frac{5 \cdot 4 \cdot 3!}{3! \cdot 2} (4x^2 y^3) = 40x^2 y^3$$

Given the polynomial $f(x) = -\frac{1}{3}(x + \frac{3}{2})^2(x - 1)^3(x - 2)^4$, $= -\frac{1}{3}(x + \frac{3}{2})^2(x - 1)^3(x - 2)^4$

a. (5 points) Find the real zeros and state the multiplicity of each.

$-\frac{3}{2}$ 2 even
 1 3 odd
 2 4 even

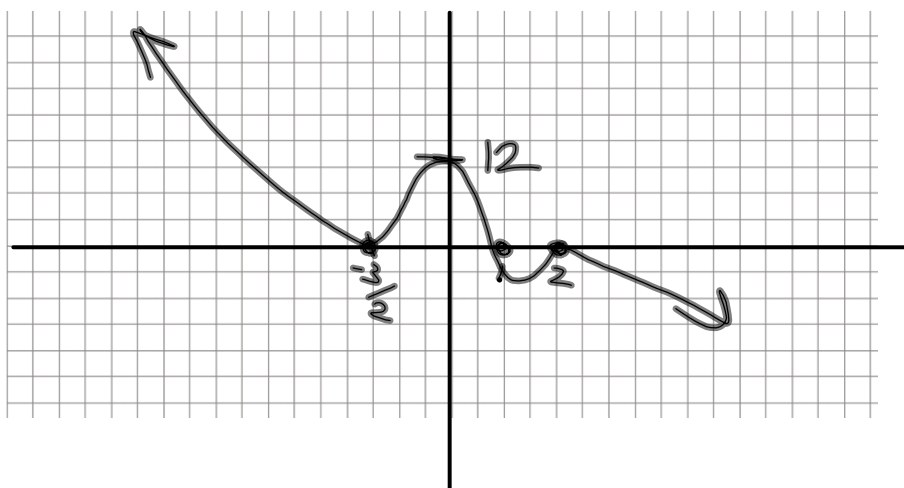
b. (5 points) State the lead term and make a sketch depicting the end behavior of the graph.

$-\frac{1}{3}x^9$

c. (3 points) State the y-intercept as an ordered pair.

$-\frac{1}{3}(\frac{3}{2})^2(-1)^3(-2)^4 = \frac{1}{3} \cdot \frac{3^2}{2^2} \cdot \frac{2^4}{1} = 12$ $(0, 12)$

d. (6 points) Graph the polynomial. Label x- and y-intercepts.



Find a formula for the inverse of the one-to-one function.

$f(x) = \frac{x - 1}{x + 7}$ $(f \circ f^{-1})(x) = ?$

$x = \frac{y - 1}{y + 7}$

$f^{-1}(x) = \frac{1 + 7x}{1 - x}$

$x(y + 7) = y - 1$
 $xy + 7x = y - 1$
 $xy - y = -1 - 7x$
 $y(x - 1) = -1 - 7x$
 $y = \frac{-1 - 7x}{x - 1}$

f & g are inverses if
 $(f \circ g)(x) = x$ &
 $(g \circ f)(x) = x$

$$\begin{aligned}
 \frac{\frac{1+7x}{1-x} - 1}{\frac{1+7x}{1-x} + 7} &= \frac{1+7x - (1-x)}{1-x} \\
 &= \frac{1+7x - 1 + x}{1-x} \cdot \frac{\cancel{1-x}}{1+7x+7-7x} \\
 &= \frac{\cancel{1-x}}{\cancel{1-x}} = x
 \end{aligned}$$