

$$a_{n+1} = a_n + d$$

$$a_n = a_1 + (n - 1)d$$

$$S_n = \frac{n}{2}(a_1 + a_n)$$

$$a_n = a_1 r^{n-1}$$

$$S_n = \frac{a_1(1 - r^n)}{1 - r}$$

$$S_\infty = \frac{a_1}{1 - r}$$

$$(a + b)^n = \sum_{k=0}^n \binom{n}{k} a^{n-k} b^k$$

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$

$$P(t) = P_0 e^{kt}$$

1. Find the indicated term of the sequence.

$$a_n = \left(1 + \frac{1}{n}\right)^2 ; a_{80} = \left(1 + \frac{1}{80}\right)^2 = \left(\frac{80}{80} + \frac{1}{80}\right)^2 = \frac{81^2}{80^2}$$

2. Predict the nth term of the sequence.

$$\frac{2}{3}, \frac{3}{4}, \frac{4}{5}, \frac{5}{6}, \frac{6}{7}, \dots$$

$$1, 2, 3, 4, 5 \quad a_n = \frac{n+1}{n+2} = \frac{6561}{6400} \approx 1.025$$

3. Find and evaluate the sum.

$$\sum_{k=1}^8 (-1)^{k+1} 3k = (-1)^2 \cdot 3 \cdot 1 - 3 \cdot 2 + 3 \cdot 3 - 3 \cdot 4 + 3 \cdot 5 - 3 \cdot 6 + 3 \cdot 7 - 3 \cdot 8 = -12$$

4. Write sigma notation for the series.

$$4 - 9 + 16 - 25 + \dots + (-1)^n n^2$$

$$\sum_{i=2}^n (-1)^i i^2$$

5. Write the 4th term of $(2x + y)^5$.

$$\begin{aligned} (k+1)^{\text{st}} \\ a = 2x \\ b = y \\ n = 5 \\ k = 3 \end{aligned}$$

$$\sum_{n=2}^k (-1)^n n^2$$

$$\binom{5}{3} (2x)^{5-3} (y)^3 = \frac{5!}{3!(2!) (2x)^2 y^3 = \frac{5 \cdot 4 \cdot 3!}{3! \cdot 2} (4x^2 y^3) = 40x^2 y^3$$

Given the polynomial $f(x) = -\frac{1}{3}(x + \frac{3}{2})^2(x - 1)^3(x - 2)^4$, $-\frac{1}{3}(x + \frac{3}{2})^2(x - 1)^3(x - 2)^4$

a. (5 points) Find the real zeros and state the multiplicity of each.

$-\frac{3}{2}$ 1 2
 even odd even

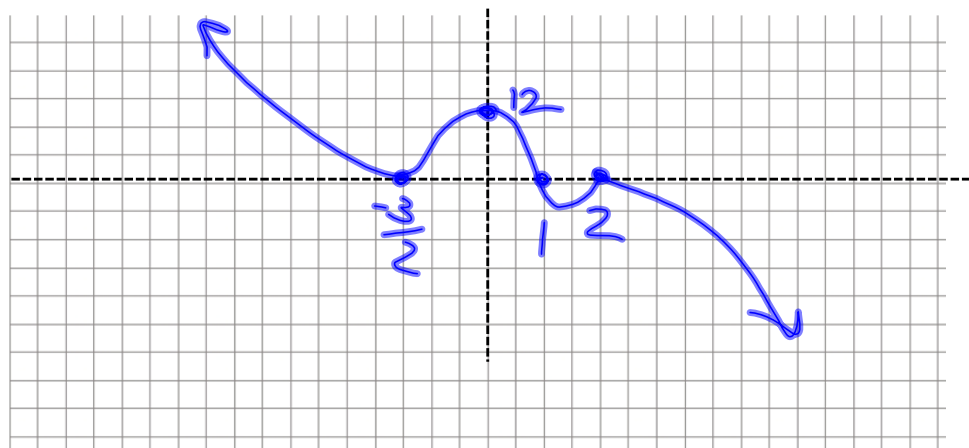
b. (5 points) State the lead term and make a sketch depicting the end behavior of the graph.

$-\frac{1}{3}x^9$

c. (3 points) State the y-intercept as an ordered pair.

$-\frac{1}{3}(\frac{3}{2})^2(-1)^3(-2)^4 = \frac{1}{3} \cdot \frac{3^2}{2^2} \cdot \frac{2^4}{1} = 12$
 $(0, 12)$

d. (6 points) Graph the polynomial. Label x- and y-intercepts.



Find a formula for the inverse of the one-to-one function.

$f(x) = \frac{x - 1}{x + 7}$ $(f \circ f^{-1})(x) = y(x - 1) = -7x - 1$

$x = \frac{y - 1}{y + 7}$

$y = \frac{-7x - 1}{x - 1}$

$x(y + 7) = y - 1$

$xy + 7x = y - 1$

$xy - y = -7x - 1$

$f^{-1}(x) = \frac{7x + 1}{1 - x}$

f & g are inverses if $(f \circ g)(x) = x$ & $(g \circ f)(x) = x$

$$\frac{\frac{1+7x}{1-x} - 1}{\frac{1+7x}{1-x} + 7} = \frac{1+7x - (1-x)}{1-x} \cdot \frac{1-x}{1+7x+7(1-x)}$$

$$= \frac{1+7x-1+x}{\cancel{1-x}} \cdot \frac{\cancel{1-x}}{1+7x+7-7x} =$$

$$= \frac{\cancel{8x}}{\cancel{8}} = x$$