

Review:

1. Define: *a relation in which each input has exactly one output*
- a. function *the set of all input values for which the function is defined*
- b. domain *the set of all input values for which the function is defined*
2. Write the domain in interval notation:
- a. $f(x) = \sqrt{x-3}$ $x-3 \geq 0$ $x \geq 3$ $[3, \infty)$
- b. $f(x) = \frac{2}{x+6}$ $(-\infty, -6) \cup (-6, \infty)$

Turn in Homework # (stapled in order, sections/problems numbered, name on first page)

- 1.2: #15-29odd, #40, 41, 42, 45, 48, #59-70all
- 1.4: #35-47odd; 53-63odd
- 1.5: #1-16all, #47-53odd

3. State the formula/equation:

- a. Slope of the line that passes through the points (x_1, y_1) and (x_2, y_2) . $m = \frac{y_2 - y_1}{x_2 - x_1}$
- b. Slope-intercept form of the equation of a line. $y = mx + b$
- c. Point-slope form of the equation of a line. $y - y_1 = m(x - x_1)$

4. Fill in the blanks:

Two lines $y = m_1x + b_1$ and $y = m_2x + b_2$ are

- a. parallel if $m_1 = m_2$ and $b_1 \neq b_2$
- b. perpendicular if $m_1 = -\frac{1}{m_2}$ or $m_1 m_2 = -1$

5. Determine equations of the lines passing through the point $(-1, 2)$ that satisfy the following:

- a. having zero slope $y = 2$

- b. having no slope $x = -1$

- c. perpendicular to the line $2x - 3y = 4$

$$-3y = 2x + 4$$

$$y = \frac{2}{3}x + \frac{4}{3}$$

$$m = -\frac{3}{2}$$

$$y - 2 = -\frac{3}{2}(x - (-1))$$

$$y - 2 = -\frac{3}{2}x - \frac{3}{2}$$

$$\boxed{y = -\frac{3}{2}x + \frac{1}{2}}$$

domain: $[-4, \infty)$

range: $[-2, 4]$

relative min: $(1, -2)$

absolute min:

$$-2 @ x = -1$$

relative max: $(-4, 4)$

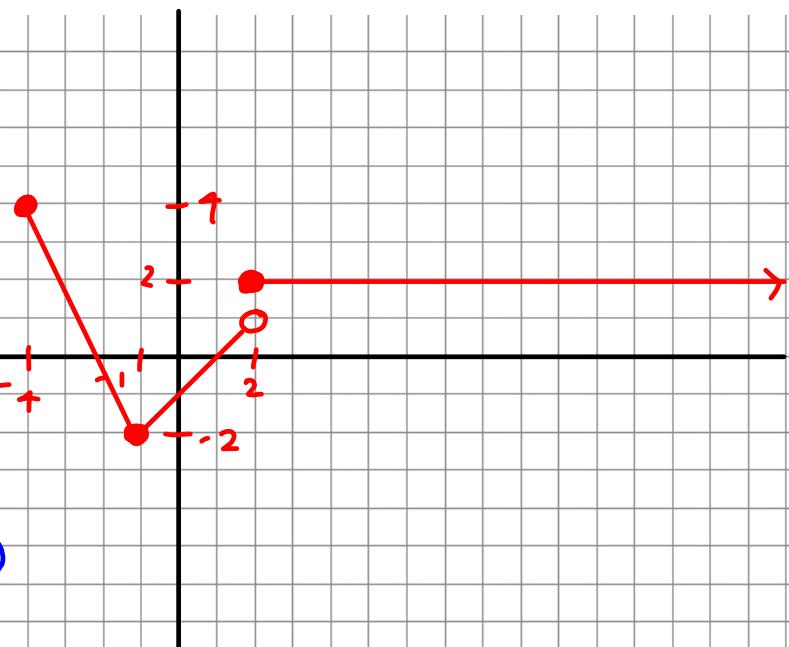
absolute max:

$$4 @ x = -4$$

increasing: $(-1, 2)$

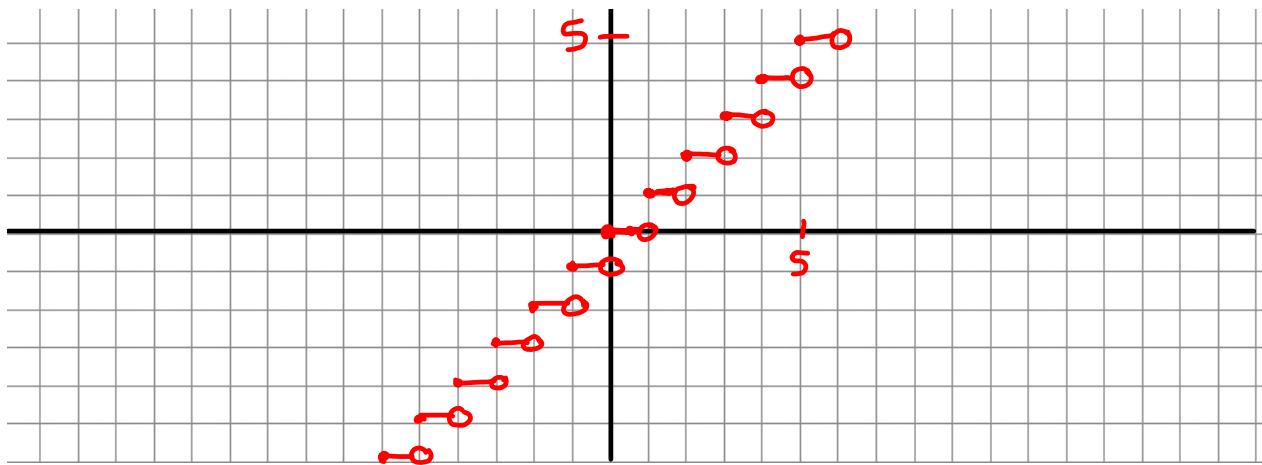
decreasing: $(-4, -1)$

constant: $(2, \infty)$



74.

$$f(x) = \begin{cases} -2x - 4 & , -4 \leq x \leq -1 \\ x - 1 & , -1 \leq x < 2 \\ 2 & , x \geq 2 \end{cases}$$

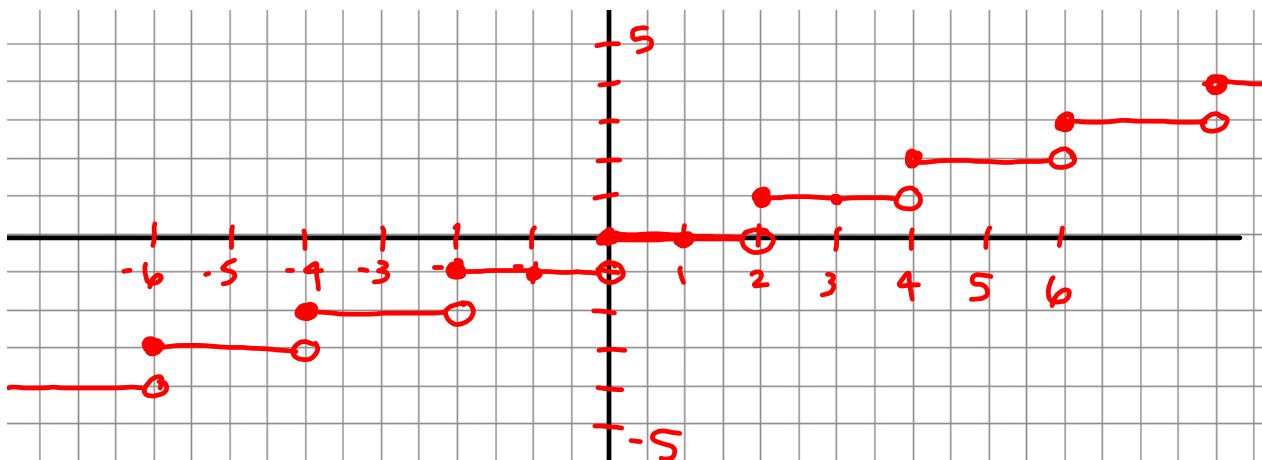


Greatest Integer Function

$\llbracket x \rrbracket$ = greatest integer less than or equal to x .

$$y = \llbracket x \rrbracket$$

"step function"



$$y = \llbracket \frac{1}{2} x \rrbracket$$

1.6 The Algebra of Functions

Given f & g , what are $(f+g)(x)$, $(f-g)(x)$,
 $(fg)(x)$, $(\frac{f}{g})(x)$, $(f \circ g)(x)$, $(g \circ f)(x)$

$$f(x) = x^2 - x, \quad g(x) = x + 1$$

$$(f+g)(x) = f(x) + g(x) = x^2 - x + x + 1 = x^2 + 1$$

domain: $(-\infty, \infty)$ range: $[1, \infty)$

$$(f-g)(x) = f(x) - g(x) = x^2 - x - (x + 1) = x^2 - 2x - 1$$

domain: $(-\infty, \infty)$ range: TOO HARD!

$$(fg)(x) = f(x) \cdot g(x) = (x^2 - x)(x + 1) = x^3 + x^2 - x^2 - x = x^3 - x$$

domain: $(-\infty, \infty)$ range: $(-\infty, \infty)$ (b/c it's an odd polynomial)

$$\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)} = \frac{x^2 - x}{x + 1}$$

domain: $(-\infty, -1) \cup (-1, \infty)$

$$(f \circ g)(x) = f(g(x)) =$$

domain:

$$(g \circ f)(x) = g(f(x)) =$$

HW #2 (due next Fri, 08/22--Test Day!)

- 1 • 1.5: #55-61odd (determining function values of & graphing piecewise functions)
2 • #69-74all (finding domain, range & equation given graph of a piecewise function)
- 3 • 1.6: #23, 29, 31; 45, 49, 51; 63, 71, 75; 81, 83 (algebra of functions)
- 1.7: #9, 11, 21, 23; 39-47odd (symmetry tests)

Quiz #1 - Monday, 8/18

Test #1 - Friday, 8/22