

Review: Determine the domain:

$$f(x) = \frac{5}{x-2} ; \quad g(x) = \sqrt{x+3} ; \quad (f \circ g)(x) ; \quad (g \circ f)(x)$$

$$(f \circ g)(x) = \frac{5}{\sqrt{x+3}-2}$$

$x+3 \geq 0$; $\sqrt{x+3}-2 \neq 0$
 $x \geq -3$
 $\sqrt{x+3} \neq 2$
 $x+3 \neq 4$
 $x \neq 1$

$[-3, 1) \cup (1, \infty)$

$$(g \circ f)(x) = \sqrt{\frac{5}{x-2} + 3}$$

$\frac{5}{x-2} + 3 \geq 0$
 $\frac{5+3(x-2)}{x-2} \geq 0$

$\left\{ x \mid \frac{3x-1}{x-2} \geq 0 \right\}$

zeros of a function v. x-intercepts of a function

x is a zero of a function f if $f(x)=0$

That is, zeros of a function are all of the input values that have 0 as their output.

$(x, 0)$ is an x-intercept of a function f if the graph of f intersects the x-axis at the point $(x, 0)$.

Since the x-coordinates of the x-intercepts are exactly those input values that map to 0, we can get our x-intercepts from our list of zeros.

Note, however, that *only real zeros contribute to x-intercepts*.

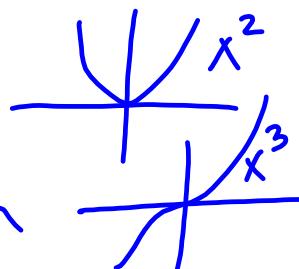
Multiplicity of a zero

$$f(x) = (x-2)^4 (x-3)(x+6)^3 (x+2)^2$$

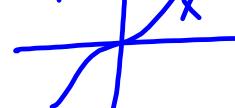
degree: $x^4 \cdot x \cdot x^3 \cdot x^2 = x^{10}$

zeros:	2	3	-6	-2
multiplicity:	4	1	3	2

even multiplicity: bounces



odd multiplicity: crosses through

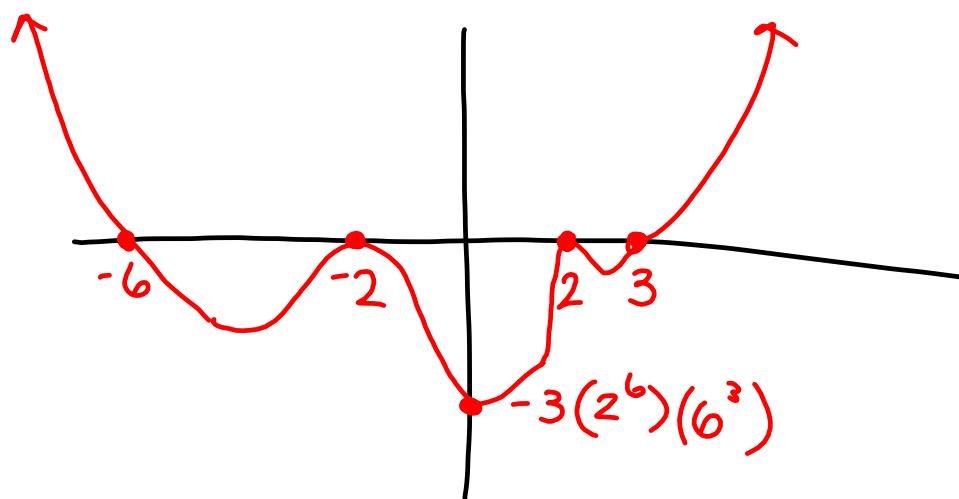


$$f(x) = (x-2)^4 (x-3)(x+6)^3 (x+2)^2$$

lead term: $x^{10} \Rightarrow$ end behavior

zeros:	2	3	-6	-2
multiplicity:	4	1	3	2

constant term:
 $(-2)^4 (-3)(6^3)(2^2) < 0$

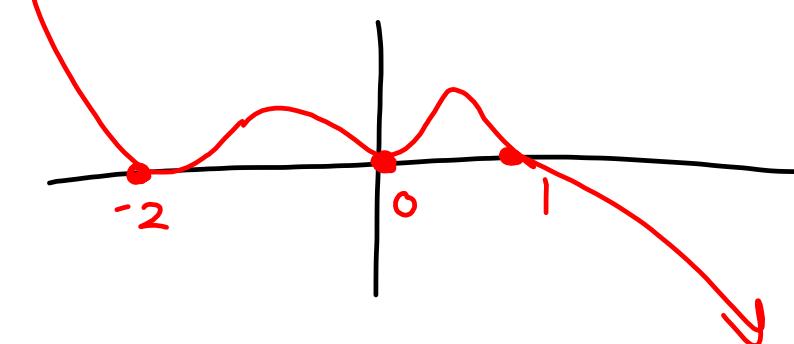


$$f(x) = -3x^2(x-1)^3(x+2)^2$$

Lead term: $(-3x^2)(x^3)(x^2) = -3x^7$

constant term: 0
(y-int)

zeros/	0	1	-2
mult	(2) even	(3) odd	(2) even

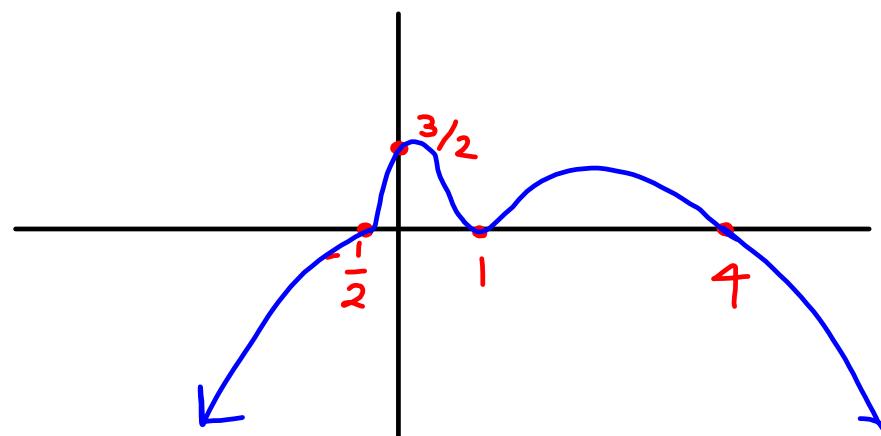


$$f(x) = -3(x-4)(x+\frac{1}{2})^3(x-1)^2$$

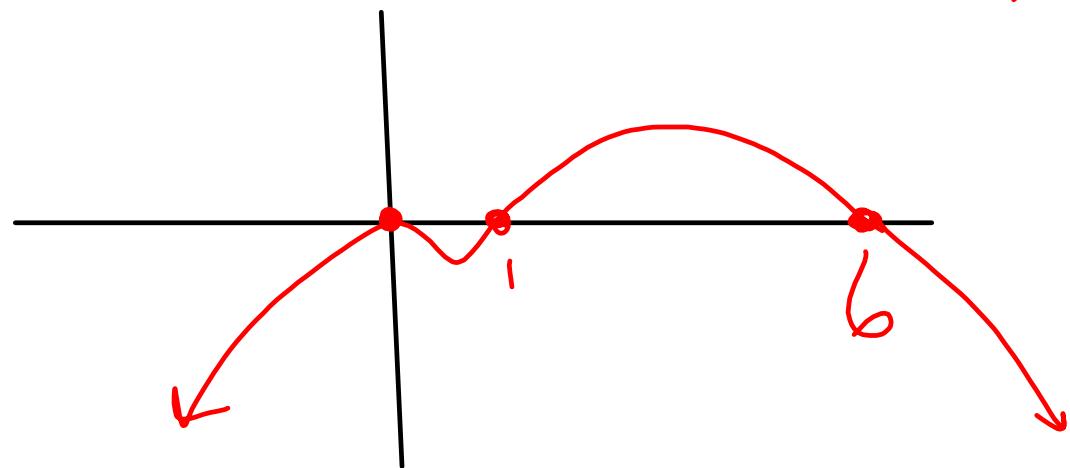
lead term: $-3(x)(x^3)(x^2) = -3x^6$

constant term: $-3(-1)(\frac{1}{2})^3(-1)^2 = 12 \cdot \frac{1}{8} \cdot 1 = \frac{3}{2}$

zeros/	4	$-\frac{1}{2}$	1
mult	(1)	(3)	(2)



$$\begin{aligned}
 y = -x^4 + 7x^3 - 6x^2 &= -x^2(x^2 - 7x + 6) \\
 &= -x^2(x-6)(x-1) \\
 \text{lead term: } -x^4 & \\
 \text{const. term: } 0 & \\
 \text{zeros: } 0 & \quad 6 \quad 1 \\
 \text{mult: } (2) & \quad (1) \quad (1)
 \end{aligned}$$



$$f(x) = -x^5 + 5x^4 - 6x^3$$

3.3 Zeros of Polynomials & Polynomial Division

$$f(x) = (x-a)(x-b)(x-c)$$

\Rightarrow zeros are $a, b, \text{ and } c.$

$$12 \div 3 = 4 \Rightarrow 12 = 3 \cdot 4$$

Long Division

33 ÷ 6

$$\begin{array}{r} P(x) = 2x^3 - 3x^2 + x - 1 \\ d(x) = x - 3 \end{array} \quad \frac{P(x)}{d(x)} = P(x) \div d(x)$$

$$\begin{array}{r} 2x^2 + 3x + 10 \leftarrow \text{quotient} \\ x-3 \overline{)2x^3 - 3x^2 + x - 1} \\ - (2x^3 - 6x^2) \\ \hline 3x^2 + x - 1 \\ - (3x^2 - 9x) \\ \hline 10x - 1 \\ - (10x - 30) \\ \hline \end{array}$$

$$\begin{aligned} 2x^3 - 3x^2 + x - 1 &= (x-3)(2x^2 + 3x + 10) + 29 \\ &\quad 5 = 2 \cdot 2 + 1 \\ \frac{2x^3 - 3x^2 + x - 1}{x-3} &= 2x^2 + 3x + 10 + \frac{29}{x-3} \\ \frac{5}{2} &= 2 + \frac{1}{2} \end{aligned}$$

$$8. P(x) = x^3 - 9x^2 + 15x + 25$$

$$d(x) = x - 5$$

$$\begin{array}{r} x^2 - 4x - 5 \\ \hline x-5 \sqrt{x^3 - 9x^2 + 15x + 25} \\ \underline{- (x^3 - 5x^2)} \\ \quad - 4x^2 + 15x + 25 \\ \underline{- (-4x^2 + 20x)} \\ \quad \quad - 5x + 25 \\ \underline{- (-5x + 25)} \\ \quad \quad \quad 0 \end{array}$$

$$P(x) = (x-5)(x^2 - 4x - 5) = (x-5)(x-5)(x+1)$$

HW #5 (due Fri, 09/05)

- 2.4: #3-13 odd Find vertex, etc. and graph
#29-37 odd Find vertex, etc.
#41-49 odd Applications of quadratics
- 3.1: #8-14 all Describing simple characteristics of polynomials
#23-31 all Determining zeros & multiplicities from factored polynomials
- 3.2: #16,17,21,22,24,25,27,28 Graph polynomials that are already factored
- 3.1: #32-38 all Finding zeros & multiplicities of expanded polynomials
- 3.2: #18-20 all, 23, 26, 29-32 all Graphing expanded polynomials
- 3.3: #7,9,13,19,21,23, 35 Long & synthetic polynomial division

HW #6 (due Fri, 09/12)

- 3.4: #7-16 all Given the zeros of a polynomial, find the polynomial
#25-32 all; 43-47 odd Given some zeros of a polynomial, find the other zeros
#51-54 all List all possible rational zeros
#55-69 odd Find all the zeros and write $f(x)$ in factored form
#79, 89, 93 Descartes' rule of signs
#95-98 all Graph the polynomial
- 3.5