

Turn in HW #10

Review

- 10.1 #7,9,23-31odd, #59,63,67
- 10.2 #9,15,19,21,25,29,35,37
- 10.3 #15,19,21,25,35,37,43,45,49,57

Write an equation for $y = \sqrt[3]{x}$, but flipped vertically, stretched vertically by a factor of 4, shifted down 5, and shifted right 2.

$$y = -4\sqrt[3]{x-2} - 5$$

Determine whether the function is even, odd, or neither.

$$f(x) = -5x^2 + \frac{3}{x^4} - 7$$

$$\begin{aligned} f(-x) &= -5(-x)^2 + \frac{3}{(-x)^4} - 7 \\ &= -5x^2 + \frac{3}{x^4} - 7 = f(x) \Rightarrow \text{even} \end{aligned}$$

The Binomial Theorem:

$$(a+b)^n = \sum_{k=0}^n \binom{n}{k} a^{n-k} b^k$$

In particular,

The $(k+1)^{\text{st}}$ term of $(a+b)^n$ is

$$\binom{n}{k} a^{n-k} b^k$$

Find the 5th term of

$$(p-2q)^9 \quad 5^{\text{th}} = (4+1)^{\text{st}}$$

$$\begin{aligned} a &= p \\ b &= -2q \\ n &= 9 \\ k &= 4 \end{aligned}$$

$$\begin{aligned} 5^{\text{th}} \text{ term} &: \binom{9}{4} (p)^{9-4} (-2q)^4 \\ &= \frac{9!}{4!(9-4)!} p^5 (16q^4) \\ &= \frac{9 \cdot 8 \cdot 7 \cdot 6 \cdot 5!}{4 \cdot 3 \cdot 2 \cdot 1 \cdot 5!} (16 p^5 q^4) \\ &= 3 \cdot 7 \cdot 6 \cdot 16 p^5 q^4 = \boxed{2016 p^5 q^4} \end{aligned}$$

$$= 2016 p^5 q^4$$

Given a set with n objects, the # of subsets containing k elements is $\binom{n}{k}$,

so the total # of subsets of any size is $\binom{n}{0} + \binom{n}{1} + \binom{n}{2} + \dots + \binom{n}{n}$

$$(1+1)^n = \binom{n}{0} 1^{n-0} 1^0 + \binom{n}{1} 1^{n-1} 1^1 + \binom{n}{2} 1^{n-2} 1^2 + \dots + \binom{n}{n} 1^{n-n} 1^n$$

$$2^n = \binom{n}{0} + \binom{n}{1} + \binom{n}{2} + \binom{n}{3} + \dots + \binom{n}{n}$$

How many "words" can we write with the English alphabet, which has 26 letters?

$$2^{26} = 67,108,864$$

of groups of any size of class of 11 students:

$$2^{11} = 2048$$

find the 8th term of $(3x - y)^{15}$

$$a = 3x$$

$$b = -y$$

$$n = 15$$

$$k = 7$$

$$(8 = k + 1)$$

$(k+1)^{\text{st}}$ term of $(a+b)^n$
is $\binom{n}{k} a^{n-k} b^k$

$$\binom{15}{7} (3x)^{15-7} (-y)^7$$

$$= \frac{15!}{7!(15-7)!} (3x)^8 (-y)^7$$

$$= \frac{\cancel{15} \cdot \cancel{14} \cdot 13 \cdot \cancel{12} \cdot \cancel{11} \cdot \cancel{10} \cdot \cancel{9} \cdot \cancel{8}!}{\underset{2}{7} \cdot \cancel{6} \cdot \cancel{5} \cdot \cancel{4} \cdot \cancel{3} \cdot \cancel{2} \cdot \cancel{1} \cdot \cancel{8}!} (-3^8 x^8 y^7)$$

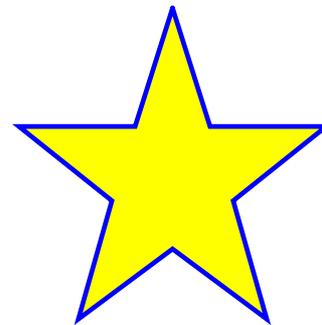
$$= -3^8 \cdot 13 \cdot 11 \cdot 5 \cdot 9 x^8 y^7$$

$$= -42220035 x^8 y^7$$

Quiz #5 on Matrices, Sequences, Series - **NOW!**

HW #11 (due Mon, Oct 27)

- 10.7 #1,7,21,27,31-39odd (Binomial Theorem)
- Final Exam Practice Problems



Review session - 3:30pm, Thursday 10/30

Final Exam - 9:00am, Friday 10/31

Note that your final exam average can replace your lowest test grade!

BRING YOUR TEXTBOOKS TO THE FINAL EXAM!