

1.2:

- #15-29odd (determining if a relation is a function; determining function values)
- #40,41,42,45,48 (determining domain of a function)
- #59-70all (determining if a graph is a function; domain & range from graph)

1.4:

- #35-47odd; 53-63odd (determining equations of lines; parallel v. perpendicular)

1.5:

- #1-16all (determining characteristics of functions from graphs)
- #47-61odd (determining function values of & graphing piecewise functions)
- #69-74all (finding domain, range & equation given graph of a piecewise function)

1.6: #23,29,31; 45, 49, 51; 63, 71,75; 81, 83 (algebra of functions)

1.7: #9,11,21,23; 39-47odd (symmetry tests)

#59-69odd; 77-83 odd; 93-101odd; 115-121odd (graphing with transformations)

2.4: #1,2; 15-22all; 23-27odd (parabolas)

2.4: #3-13 odd

1.3/1.4 - Linear functions (taken from <http://mathemartiste.com/prec/Pre calculusNotes.pdf>)

A linear function is one of the form $f(x) = mx + b$, where m is the slope of the line and b is the y-intercept. $y = mx + b$ is called the slope-intercept form of the equation of a line.

The slope of a linear function can be found by taking the ratio of change in y-values over the change in x-values.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \text{"rise" over "run"}$$

Given the slope m and a point (x_1, y_1) on a line, the slope-intercept form can be easily found by plugging these values into the point-slope equation: $y - y_1 = m(x - x_1)$.

Lines with a 0-slope are called horizontal lines and are of the form $y = k$ for some constant k . Vertical lines are said to have "no slope" and are of the form $x = k$.

Two lines in a plane are parallel if they never intersect. Two lines are perpendicular if their intersection forms a 90° angle.

Let l_1 be the graph of $f_1(x) = m_1x + b_1$ and let l_2 be the graph of $f_2(x) = m_2x + b_2$. l_1 and l_2 are parallel if $m_1 = m_2$.

This is denoted $l_1 \parallel l_2$. l_1 and l_2 are perpendicular if $m_1 = -\frac{1}{m_2}$. This is denoted $l_1 \perp l_2$.

slope-intercept form

$$y = mx + b$$

point-slope equation

$$y - y_1 = m(x - x_1)$$

Slope

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

horizontal lines

$y = k$ for some constant k (0 slope)

vertical lines

$x = k$ (no slope)

Parallel

$$m_1 = m_2$$

Perpendicular

$$m_1 = -\frac{1}{m_2}$$

1.5 More on Functions

Topics to cover in this section:

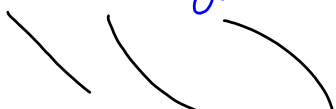
- identifying intervals on which a function is increasing, decreasing, constant
- identifying relative maxima and minima
- graphing piecewise functions
- greatest integer function

i.e. LOTS OF GRAPHING!

increasing

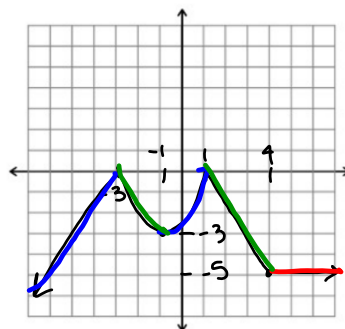


decreasing



constant

↖ horizontal



domain: $(-\infty, \infty)$
 \mathbb{R}

range: $(-\infty, 0]$

constant: $(4, \infty)$

increasing: $(-\infty, -3) \cup (-1, 1)$

decreasing: $(-3, -1) \cup (1, 4)$

increasing:

$$(-\infty, -3) \cup (-3, 0)$$

decreasing:

$$(0, 3) \cup (3, \infty)$$

constant:

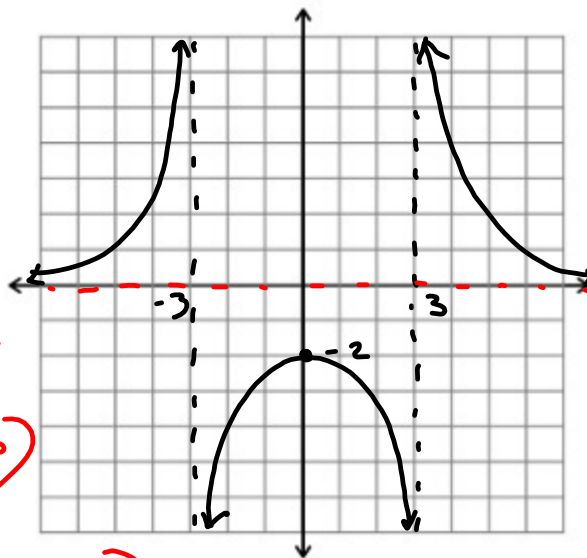
$$N/A \quad \{x \mid x \neq -3, 3\}$$

domain:

$$(-\infty, -3) \cup (-3, 3) \cup (3, \infty)$$

range: $(-\infty, -2] \cup (0, \infty)$

$$\{x \mid x \leq -2 \text{ or } x > 0\}$$



increasing:

$$(-\infty, -4) \cup (-2, -1) \cup (-1, 1)$$

decreasing:

$$(1, \infty)$$

constant:

$$(-4, -2)$$

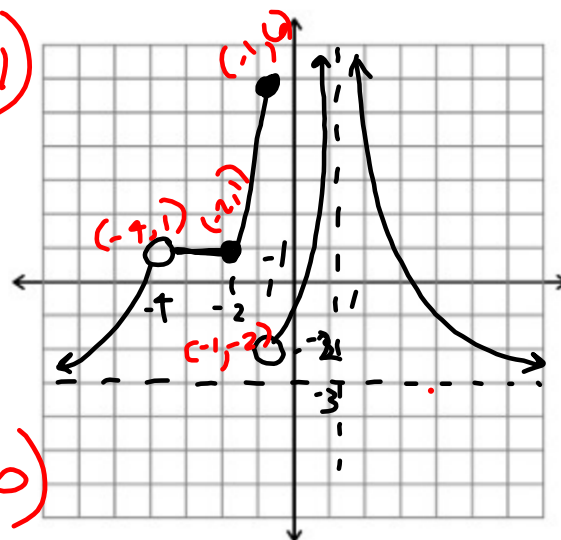
domain:

$$\{x \mid x \neq -4, 1\}$$

$$(-\infty, -4) \cup (-4, 1) \cup (1, \infty)$$

range:

$$(-3, \infty)$$



increasing:

$$(-3, 0) \cup (4, \infty)$$

decreasing:

$$(0, 2)$$

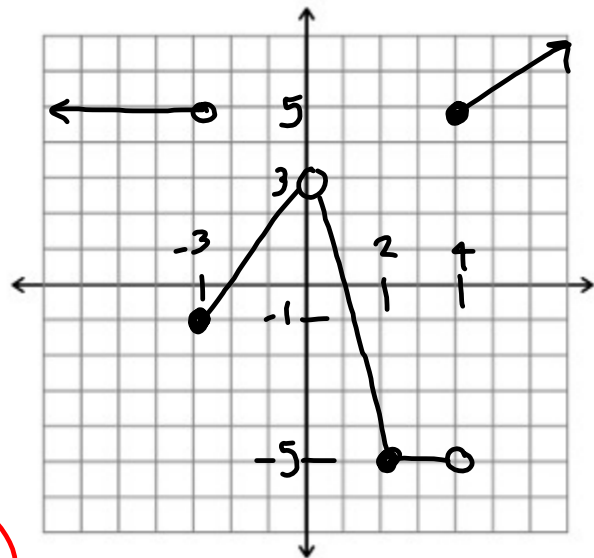
constant:

$$(-\infty, -3) \cup (2, 4)$$

domain: $\{x \mid x \neq 0\}$

$$(-\infty, 0) \cup (0, \infty)$$

$$\text{range: } [-5, 3) \cup [5, \infty)$$

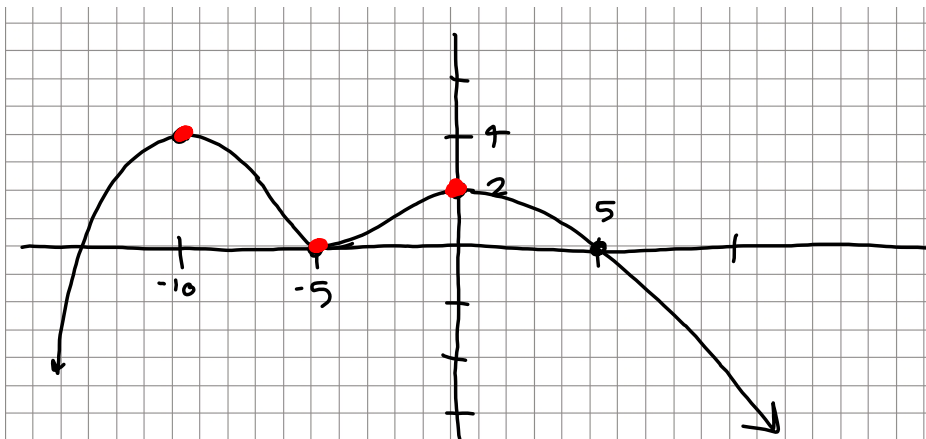


Maxima & Minima =

Extrema of a function

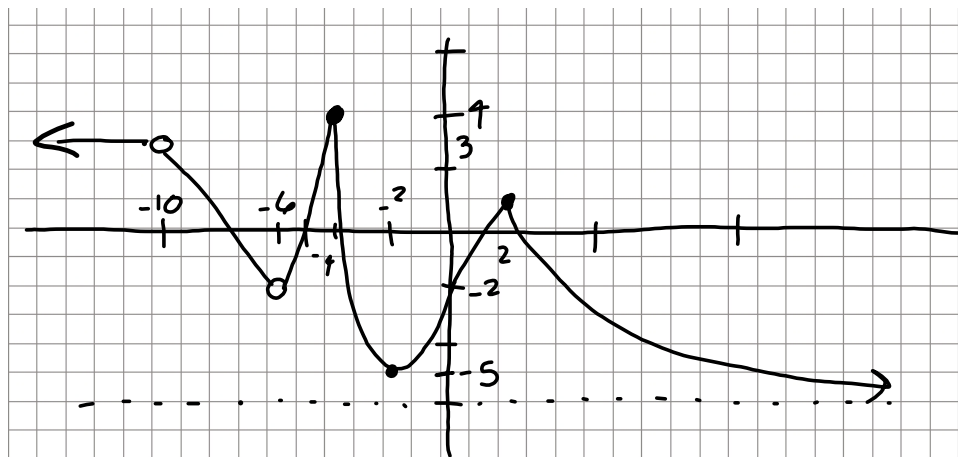
Absolute max/min refer to single highest or lowest values on the graph (if they exist)

Relative max/min refer to highest & lowest values in small intervals



relative max:
 $(-10, 4)$ & $(0, 2)$
 relative min:
 $(-5, 0)$

absolute max:
 $4 @ x = -10$
 absolute min:
 none

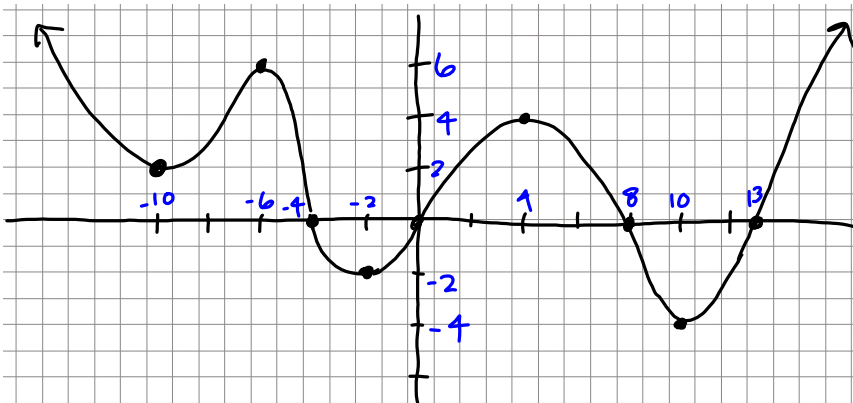
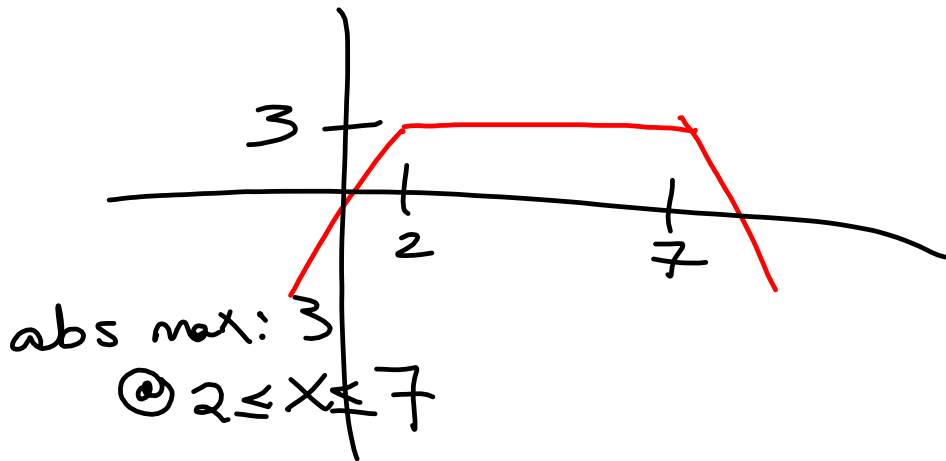


domain:
 $(-\infty, -10) \cup$
 $(-10, -6) \cup$
 $(-6, \infty)$

range:
 $(-6, 4]$

relative min:
 $(-2, -5)$
 relative max:
 $(-4, 4), (2, 2)$

absolute min:
 none
 absolute max:
 $4 @ x = -4$



relative max:
 $(-6, 6), (4, 4)$

relative min:
 $(-10, 2), (-2, -2), (10, -4)$

abs. max:
none

abs. min:
 $-4 @ x=10$

domain:
 $(-\infty, \infty)$

range:
 $[-4, \infty)$

increasing: $(-10, -6) \cup (-2, 4) \cup (10, \infty)$

decreasing:
 $(-\infty, -10) \cup (-6, -2) \cup (4, 10)$