

- 3.6 #15-39odd Solving polynomial inequalities
- #47, 53-61odd Solving rational inequalities
- 3.7: #23-37 odd Variation
- 4.1 #17-23 odd prove f is one-to-one; prove g is not one-to-one
- #59-63 odd determine if f is on.to.one and if so, determine its inverse
- #77-81 odd sketch the inverse function by reflecting over y=x
- #83-87 odd use composition to show that the functions are inverses
- 4.2 #5-10all match an exponential function to its graph
- #11-41odd sketch graphs of exponential functions using transformations
- #43a,b,c,45,47 compound interest word problems
- 4.3 #1-8all sketch graphs of logarithmic functions
- #9-33odd evaluate log expressions without a calculator
- #35-53 odd convert between logarithmic and exponential expressions
- #69-77 odd apply change of base formula & calculator to approximate log expressions
- #83-90 all graph logarithmic functions using transformations
- 4.4 # 31,33, 49-55 odd; 65-75 odd; 107 applying log rules
- 4.5 # 1-25 odd; solving exponential equations; #27-47 odd solving logarithmic equations
- 4.6 #5,7,9,15,17 application problems

$$f(x) = \frac{x}{x-5}$$

$$y = \frac{x}{x-5}$$

$$(y-5)x = \frac{y}{\cancel{y-5}} \cdot \cancel{y-5}$$

$$x(y-5) = y$$

$$xy - 5x = y$$

$$xy - y = 5x$$

$$y(x-1) = 5x$$

$$y = \frac{5x}{x-1}$$

$$f^{-1}(x) = \frac{5x}{x-1}$$

$$3^{2 \log_3 4} = 3^{\log_3 4^2} = 4^2 = 16$$

f & g are inverses if
 $f(g(x)) = x$ & $g(f(x)) = x$
 $f(x) = \log_a x$; $g(x) = a^x$

$$\log_a(a^x) = x$$

$$a^{(\log_a x)} = x$$

$$\begin{aligned} \log_a \sqrt{\frac{a^4 b^8}{a^2 b^5}} &= \log_a \sqrt{a^4 b^3} = \\ &= \log_a (a^4 b^3)^{1/2} = \log_a (a^2 b^{3/2}) \\ &= \log_a a^2 + \log_a b^{3/2} \\ &= 2 + \frac{3}{2} \log_a b \end{aligned}$$

Determine whether the statement is true. Assume that a , x , M , and N are positive.

102. $\log_N(MN)^x = x \log_N M + x$

$$\begin{aligned} \text{LHS} &= \log_N (MN)^x = \log_N (M^x N^x) \\ &= \log_N M^x + \log_N N^x \\ &= x \log_N M + x = \text{RHS} \checkmark \end{aligned}$$

Write without using logarithms.

106. $\log_a x + \log_a y - mz = 0$

$$\log_a(xy) - mz = 0$$

$$\log_a(xy) = mz$$

$$a^{mz} = xy$$

$$\begin{array}{l} \log_a b = c \\ \longleftrightarrow \\ a^c = b \end{array}$$

4.5 Solving Exponential & Logarithmic Equations

$$3^{2x} = 3^5$$

$$\log_3(3^{2x}) = \log_3 3^5$$

$$2x = 5$$

$$x = 5/2$$

For any $a > 0, a \neq 1$,

$$a^x = a^y \leftrightarrow x = y$$

$$\log_3 2x = \log_3 5$$

$$3^{\log_3 2x} = 3^{\log_3 5}$$

$$2x = 5$$

$$x = 5/2$$

Similarly, for $M, N > 0, a > 0, a \neq 1$,

$$\log_a M = \log_a N \leftrightarrow M = N$$

$$2^x = 7$$

$$\log_2 2^x = \log_2 7$$

$$x = \log_2 7$$

$$\ln(2^x) = \ln 7$$

$$x \ln 2 = \ln 7$$

$$x = \frac{\ln 7}{\ln 2}$$

$$e^{50t} = 300$$

$$\ln(e^{50t}) = \ln 300$$

$$50t = \ln 300$$

$$t = \frac{(\ln 300)}{50}$$

$$\neq \ln \frac{300}{50}$$

$$(\ln 300)/50$$

$$\log x + \log(x + 3) = 1$$

$$\log [x(x+3)] = 1$$

$$\log_{10}(x^2 + 3x) = 1$$

$$10^1 = x^2 + 3x$$

$$0 = x^2 + 3x - 10$$

$$0 = (x+5)(x-2)$$

$$\log_a b = c \Leftrightarrow a^c = b$$

$$\Rightarrow x = \cancel{-5}, 2$$

$$4. 3^{7x} = 27$$

$$3^{7x} = 3^3$$

$$7x = 3$$

$$x = \frac{3}{7}$$

$$10. 3^{x^2+4x} = \frac{1}{27} = \frac{1}{3^3}$$

$$3^{x^2+4x} = 3^{-3}$$

$$x^2 + 4x = -3$$

$$x^2 + 4x + 3 = 0$$

$$(x+3)(x+1) = 0$$

$$x = -3, -1$$