

4.5 #1-25 odd; #27-47 odd	solving exponential equations; solving logarithmic equations
4.6 #5,7,9,15,17	application problems with logs/exp functions
10.1 #7,9,23-31 odd #59,63,67	find the general (nth) term of the sequence write sigma notation
10.2 #9,15,19,21,25,29, 35,37	arithmetic sequences and series
10.3 #15,19,21,25,35,37,43,45,49,57	geometric sequences and series
10.7 #1,7,21,27,31-39 odd	binomial theorem

*solving log/exp eq.  
applications  
simple seq/series*

Quiz on log/exp equations & applications - this week

*Thurs?*

Test #4 - Feb 6-8??

*Monday  
(special Math Lab on Monday)*

Arithmetic Sequences/Series:

10.2

**Definition:** A sequence is arithmetic if there exists a number  $d$ , called the common difference, such that  $a_{n+1} = a_n + d$  for any integer  $n \geq 1$ .

The nth term of an arithmetic sequence is given by  $a_n = a_1 + (n - 1)d$ , for any integer  $n \geq 1$ .

The sum of the first n terms of an arithmetic sequence is given by

$$S_n = \frac{n}{2}(a_1 + a_n) = \sum_{i=1}^n a_i$$

11 + 7 + 3 + ...

$S_{14} =$

$$\frac{14}{2}(11 + (-41))$$

$$= 7(-30) = \boxed{-210}$$

*$d = -4 ; n = 14 ; a_1 = 11$*

*$a_{14} = 11 + (14 - 1)(-4)$*

*$= 11 - 13(4) = -41 = a_{14}$*

$$-8, -5, -2, 1, 4, \dots$$

$$\text{common difference: } d = 3$$

$$n^{\text{th}} \text{ term: } a_n = a_1 + (n-1)d$$

$$a_n = -8 + (n-1)(3) = -11 + 3n$$

12<sup>th</sup> term:

$$a_{12} = -11 + 3(12) = \boxed{25}$$

$$7, 4, 1, \dots$$

find the 17<sup>th</sup> term.

$$\begin{aligned} a_{17} &= 7 + (17-1)(-3) \\ &= 7 - 16(3) \\ &= 7 - 48 = \boxed{-41} \end{aligned}$$

$$34. \sum_{k=5}^{20} 8k = 40 + 48 + 56 + \dots + 160$$

$$n = 20 - 5 + 1$$

$$S_n = \frac{n}{2}(a_1 + a_n) = 16$$

$$S_{16} = \frac{16}{2}(40 + 160) = 8(200) = \boxed{1600}$$

$$\sum_{i=2}^5 i = \underbrace{2 + 3 + 4 + 5}$$

4 terms

$$(5-2)+1$$

10.2

$$36. \sum_{k=2}^{50} (2000 - 3k)$$

$$= 2000 - 3(2) + \dots + 2000 - 3(50)$$

$$= 1994 + \dots + 1850$$

$$S_{49} = \frac{49}{2}(1994 + 1850) = \boxed{94,178}$$

### Geometric Sequences/Series:

**10.3**

**Definition:** A sequence is geometric if there is a number  $r$ , called the **common ratio**, such that

$$\frac{a_{n+1}}{a_n} = r, \text{ or } a_{n+1} = a_n r, \text{ for any integer } n \geq 1.$$

The **nth term of a geometric sequence** is given by

$$a_n = a_1 r^{n-1}, \text{ for any integer } n \geq 1.$$

The **sum of the first n terms** of a geometric sequence is given by

$$S_n = \frac{a_1(1-r^n)}{1-r}, \text{ for any } r \neq 1.$$

When  $|r| < 1$ , the **limit or sum of an infinite geometric series** is given by

$$S_\infty = \frac{a_1}{1-r}$$

$$18, -6, 2, \frac{-2}{3}$$

common ratio:  $\boxed{\frac{-1}{3}}$   $\Rightarrow \frac{-6}{18} = \frac{2}{-6} = \frac{-\frac{2}{3}}{2}$ , etc.

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$$2, -10, +50, -250, \dots \quad r = -5$$

find the 9<sup>th</sup> term:

$$a_9 = (2)(-5)^{9-1} = 2(-5)^8 = \boxed{781,250}$$

$$16 - 8 + 4 - 2 + \dots$$

Find the sum of the first 10 terms.

$$S_n = \frac{a_1(1-r^n)}{1-r}$$

$$S_{10} = \frac{16\left(1 - \left(\frac{-1}{2}\right)^{10}\right)}{1 - \left(\frac{-1}{2}\right)} = \boxed{\frac{341}{32}}$$

$$\sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^n = \left(\frac{1}{2}\right)^0 + \left(\frac{1}{2}\right)^1 + \left(\frac{1}{2}\right)^2 + \dots$$
$$= 1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots$$

$$S_{\infty} = \frac{1}{1 - \frac{1}{2}} = \frac{1}{\frac{2}{2} - \frac{1}{2}} = \frac{1}{\left(\frac{1}{2}\right)} = 1 \cdot \frac{2}{1} = \boxed{2}$$

$$\sum_{n=0}^{\infty} \frac{1}{2^n} = 1 + \frac{1}{2} + \frac{1}{4} + \dots = 2$$

In general, when  $|r| < 1$ ,  
the sum of an infinite geometric  
series is  $S_{\infty} = \frac{a_1}{1-r}$   
(or  $S_{\infty} = \frac{a_0}{1-r}$  if series starts w/ $a_0$ )



$$100 - 10 + 1 - \frac{1}{10} + \frac{1}{100} - \dots$$

what is the sum of this infinite geometric series?

$$\begin{aligned}
 S_{\infty} &= \frac{a_1}{1-r} = \frac{100}{1 - (-\frac{1}{10})} = \frac{100}{\frac{10}{10} + \frac{1}{10}} = \frac{100}{(\frac{11}{10})} \\
 &= 100 - \frac{10}{11} = \boxed{\frac{1000}{11}}
 \end{aligned}$$

$$50. \sum_{k=1}^{\infty} \frac{8}{3} \left(\frac{1}{2}\right)^{k-1}$$

$$= \frac{8}{3} \left(\frac{1}{2}\right)^{1-1} + \frac{8}{3} \left(\frac{1}{2}\right)^{2-1} + \left(\frac{8}{3}\right) \left(\frac{1}{2}\right)^{3-1} + \dots$$

$$= \frac{8}{3} + \frac{4}{3} + \frac{2}{3} + \dots \quad r = \frac{1}{2}$$

$$S_{\infty} = \frac{\frac{8}{3}}{1 - \left(\frac{1}{2}\right)} = \frac{\frac{8}{3}}{\frac{1}{2}} = \frac{8}{3} \cdot \frac{2}{1} = \boxed{\frac{16}{3}}$$