

$$f(x) = \text{~~~~~} \quad [c, d]$$

$$f'(x) = \text{~~~~~}$$

critical #'s : a, b

$$f(a) = A$$

$$f(b) = B$$

$$f(c) = C$$

$$f(d) = D$$

$$\lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$$

$$\frac{f(a)}{g(a)} = \frac{0}{0} \quad \text{or} \quad \frac{\infty}{\infty}$$

$$\lim_{x \rightarrow a} [f(x)]^{g(x)} \quad \left(\lim_{x \rightarrow 0} (1+x)^{\frac{1}{x}} \right)$$

$$f(a)^{g(a)} = 0^0 \text{ or } 1^\infty$$

$$y = \lim_{x \rightarrow a} [f(x)]^{g(x)}$$

$$\ln y = \ln \lim_{x \rightarrow a} [f(x)]^{g(x)}$$

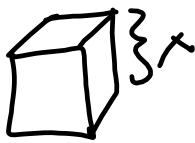
$$\ln y = \lim_{x \rightarrow a} \ln [f(x)]^{g(x)}$$

$$\ln y = \lim_{x \rightarrow a} \underbrace{g(x) \ln [f(x)]}_{\text{rewrite}}$$

$$\ln y = \frac{L}{L} \quad \frac{0}{0} \text{ or } \frac{\infty}{\infty}$$

$$y = e$$

10.



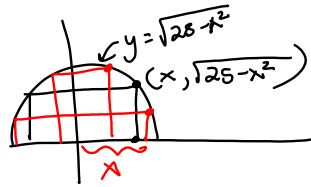
$$\frac{dx}{dt} = 3 \text{ cm/s}$$

$$\frac{dV}{dt} = ? \text{ when } x = 10 \text{ cm}$$

cm^3/s

$$V = x^3$$

$$\frac{dV}{dt} = 3x^2 \cdot \frac{dx}{dt}$$



$$A(x) = \underbrace{(2x)}_{\text{width}} \underbrace{\sqrt{25-x^2}}_{\text{height}} = (2x)(25-x^2)^{1/2}$$

$$A'(x) = 2(25-x^2)^{1/2} + (2x)\left(\frac{1}{2}(25-x^2)^{-1/2}\right)(-2x)$$

$$A'(x) = 2\sqrt{25-x^2} - \frac{2x^2}{\sqrt{25-x^2}}$$

$$2\sqrt{25-x^2} - \frac{2x^2}{\sqrt{25-x^2}} = 0$$

$$2\sqrt{25-x^2} = \frac{2x^2}{\sqrt{25-x^2}} \quad \frac{50}{4} = x^2$$

$$2(25-x^2) = 2x^2 \quad \sqrt{\frac{50}{4}} = x$$

$$50 - 2x^2 = 2x^2 \quad \frac{5\sqrt{2}}{2} = x$$

$$50 = 4x^2$$

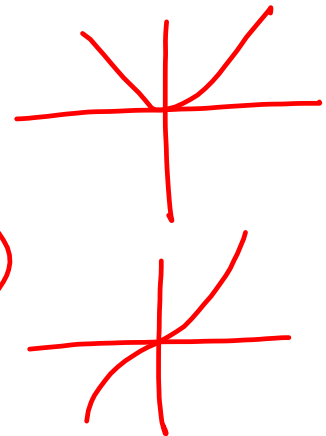
$$\text{width: } 5\sqrt{2}$$

$$\text{height: } \sqrt{25 - \frac{50}{4}} = \sqrt{\frac{50}{4}} = \frac{5\sqrt{2}}{2}$$

odd/even

f is even if $f(-x) = f(x)$

f is odd if $f(-x) = -f(x)$



$$7. f'(-2) = 0$$

$$1 - \frac{k}{4} = 0$$

$$f(x) = x + \frac{k}{x}$$

$$k =$$

$$f'(x) = 1 - \frac{k}{x^2}$$

$$f'(-2) = 1 - \frac{k}{(-2)^2} = 1 - \frac{k}{4}$$

$$\frac{d^2}{dx^2} [f(x)] = f''(x)$$

$$[f(x^3)]' = f'(x^3) \cdot (3x^2)$$

$$[f(x^3)]'' = f''(x^3) \cdot (3x^2) + f'(x^3) \cdot 6x$$

$$f(x^6) \cdot (3x^2) + g(x^3) 6x$$

$$[f(x^3)]' = f'(x^3) \cdot 3x^2$$

$$= g(x^3) \cdot 3x^2$$

$$[f(x^3)]'' = [g'(x^3) \cdot 3x^2] \cdot 3x^2 + g(x^3) \cdot 6x$$
$$= f(x^6) \cdot 9x^4 + g(x^3) \cdot 6x$$