

This week's Assignments:

01: **Read** sections 1.3 and 1.4 in your textbook by Monday, 22 Aug.

02: Complete at least 45 minutes of exercises on **Khan Academy** on topics related to sections 1.3 and 1.4 by Friday, 26 Aug. In addition, complete "Mastery Challenges" as often as they become available to you.

03: **Textbook exercises**, mostly be completed in class and will be due Friday, 26 Aug.

- 1.3 #11,21,27-39 odd, 41-61 odd; 83, 87      evaluating limits analytically
- 1.3 #63-73 odd; 89, 90      limits with trig, squeeze theorem

Next week's assignments:

01: Read 1.4-1.5

02: 45 minutes of Khan Academy

03: Textbook exercises:

- 1.4 #1-19 odd;
- 1.4 #27-30 all; 43-48 all;
- 1.4 #21,23,25,57,61,65,69,99,102
- 1.4 #87-98 all
- 1.5 #1,3,23,29-57 odd
- Ch 5 Review pp. 91-92 #3-83 odd

Expect another quiz before the test!

Test #1 - Next Friday, 2 Sept

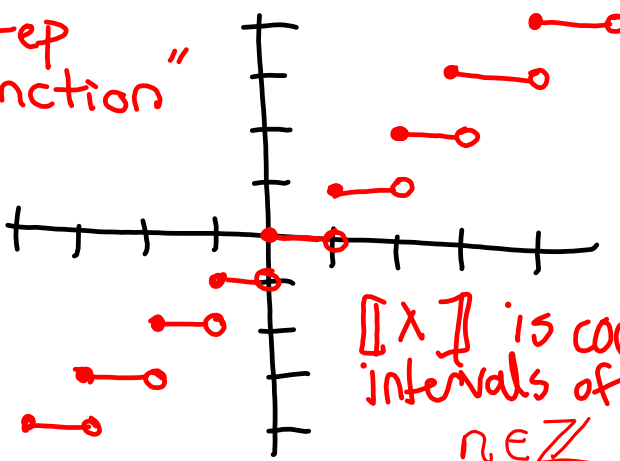
- limits of functions with discontinuities
- discuss (dis)continuity
- misc. continuity problems
- Intermediate Value Theorem
- Infinite Limits
- Review

Discuss the [dis]continuity of the function.

The Greatest Integer Function

$\lfloor x \rfloor$  = the greatest integer less than or equal to  $x$

$\lfloor x \rfloor$  "step function"



$\lfloor x \rfloor$  has non-removable jump discontinuities @ all integers

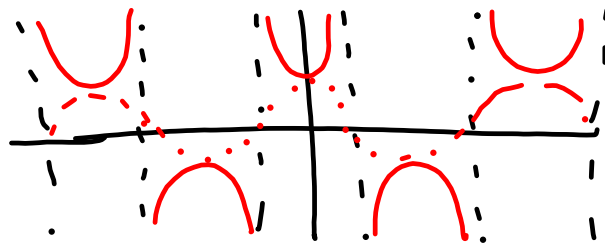
$\lfloor x \rfloor$  is continuous on all intervals of the form  $[n, n+1)$   $n \in \mathbb{Z}$

$$\begin{aligned} 22. \quad & \lim_{x \rightarrow 2^+} 2x - [x] \\ &= \lim_{x \rightarrow 2^+} 2x - \lim_{x \rightarrow 2^+} [x] \\ &= 2(2) - 2 \\ &= \boxed{2} \end{aligned}$$

$$\begin{aligned} 24. \quad & \lim_{x \rightarrow 1} \left( 1 - \left[ \frac{-x}{2} \right] \right) \\ &= \lim_{x \rightarrow 1} 1 - \lim_{x \rightarrow 1} \left[ \frac{-x}{2} \right] \\ &= 1 - (-1) \\ &= \boxed{2} \end{aligned}$$

$$20. \lim_{x \rightarrow \frac{\pi}{2}} \sec x$$

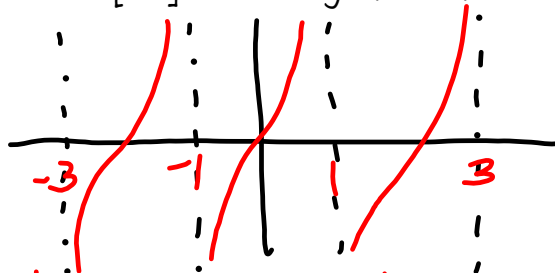
does not exist



$$52. f(x) = \tan \frac{\pi x}{2}$$

Discuss the [dis]continuity of the function.

$$\text{period: } \frac{\pi}{\pi/2} = \pi \cdot \frac{2}{\pi} = 2$$



$f$  has non-removable discontinuities  
at  $x = 2n + 1$   $n \in \mathbb{Z}$

$f$  is continuous on all intervals of  
the form  $(2n - 1, 2n + 1)$

$$b2. f(x) = \frac{1}{\sqrt{x}}, g(x) = x - 1$$

Discuss the continuity of  $f(g(x))$ .

$$f(g(x)) = \frac{1}{\sqrt{x-1}}$$

is continuous on its domain  
 $(1, \infty)$

$$b4. f(x) = \sin x ; g(x) = x^2$$

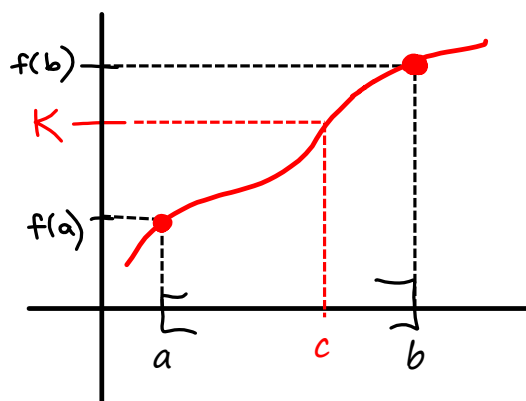
Discuss the continuity of  $f(g(x))$ .

$$f(g(x)) = \sin(x^2)$$

is continuous on  $(-\infty, \infty)$

Intermediate Value Theorem

If  $f$  is continuous on the closed interval  $[a, b]$  and  $k$  is any number between  $f(a)$  and  $f(b)$ , then there is at least one number  $c$  in  $[a, b]$  such that  $f(c) = k$ .



Does the IVT guarantee a zero in the given interval?

$$76. f(x) = x^3 + 3x - 2, [0, 1]$$

$$f(0) = -2 < 0$$

$$f(1) = 2 > 0$$

} IVT guarantees  
a zero in  $[0, 1]$

To find it, set  $x^3 + 3x - 2 = 0$  & solve for  $x$

84.  $f(x) = x^2 - 6x + 8$ ;  $[0, 3]$   $f(c) = 0$

$f(0) = 8 > 0$

$f(3) = 3^2 - 6(3) + 8 = -1 < 0$

} IVT guarantees  
 $a \in [0, 3]$   
 s.t.  $f(c) = 0$

To find it, set  $x^2 - 6x + 8 = 0$

$4 \notin [0, 3] \rightarrow \cancel{x=4}, x=2$

86.  $f(x) = \frac{x^2 + x}{x - 1}$ ,  $[\frac{5}{2}, 4]$ ,  $f(c) = 6$

$f(\frac{5}{2}) = \frac{(\frac{5}{2})^2 + \frac{5}{2}}{\frac{5}{2} - 1} = \frac{\frac{25}{4} + \frac{10}{4}}{\frac{5}{2} - \frac{2}{2}} = \frac{\frac{35}{4} \cdot \frac{2}{3}}{3} = \frac{35}{6} < 6$

$f(4) = \frac{4^2 + 4}{4 - 1} = \frac{20}{3} > 6$

Yes, the IVT guarantees  
 $a \in [\frac{5}{2}, 4]$  s.t.  $f(c) = 6$

To find it set

$\frac{x^2 + x}{x - 1} = 6$

$x^2 + x = 6(x - 1)$

$x^2 + x = 6x - 6$

$x^2 - 5x + 6 = 0$

$(x - 3)(x - 2) = 0$

$\cancel{x=2}, x=3$   
 not in  $[\frac{5}{2}, 4]$