

Assignments for the week of 10/3:

- Read 2.5-2.6
- 45 minutes of Khan Academy
- Textbook assignment due Friday, 10/14:
 - 2.5 # 1-39 odd; 43, 47 - Implicit Differentiation
 - 2.6 # 15-23 odd - Related Rates
 - 2.6 # 25, 27, 35 - Related Rates (more challenging problems)

• Upcoming:

- 3.1 # 17-35 odd - Absolute Extrema on an Interval
- 3.2 # 9-21 odd - Rolle's Theorem
- 3.2 # 33-45 odd - Mean Value Theorem
- 3.3 # 17-39 odd - Increasing, Decreasing, and Relative Extrema
- 3.4 # 15-39 odd - Inflection Points and Concavity

6th per. solutions:

1.e	7.e	12.b
2.d	8.c	13.c
3.b	9.c	14.a
4.b	10.d	15.e
5.c	11.a	16.d
6.c		

8th per. solutions:

1. b

7. e

12. b

2. a

8. d

13. a

3. b

9. b

14. c

4. d

10. e

15. c

5. c

11. c

16. a

6. b

$$y^4 + 3xy + x = 2, (2, 0)$$

$$\frac{d}{dx} [\quad] = \frac{d}{dx} [2]$$

$$y' = \text{~~~~~}$$

$$y' |_{(2,0)}$$

$$\ln\left(\frac{e^{5x}+1}{e^{2x}+1}\right) = \ln(e^{5x}+1) - \ln(e^{2x}+1)$$

$$\begin{aligned}y' &= \frac{1}{e^{5x}+1} \cdot e^{5x} \cdot 5 - \frac{1}{e^{2x}+1} \cdot e^{2x} \cdot 2 \\ &= \frac{5e^{5x}}{e^{5x}+1} - \frac{2e^{2x}}{e^{2x}+1}\end{aligned}$$

$$y = \frac{3}{5} (\sec x)^2$$

$$y' = \frac{6}{5} \sec x \cdot \sec x \tan x$$

$$\begin{aligned} \frac{\Delta s}{\Delta t} &= \frac{s(t) = -16t^2 + 1372}{\left(-16(4)^2 + 1372 \right) - \left(-16(3)^2 + 1372 \right)} \\ &= \frac{-16(16) + 16(9)}{4-3} = -112 \end{aligned}$$

2.6 Related Rates

$$18. V = \frac{4}{3} \pi r^3$$

$$\frac{d}{dt} [V] = \frac{d}{dt} \left[\frac{4}{3} \pi r^3 \right]$$

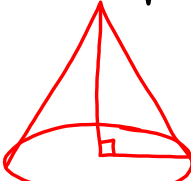
$$\frac{dV}{dt} = \frac{4}{3} \pi (\cancel{3} r^2) \cdot \frac{dr}{dt}$$

$$= 4\pi (6 \text{ in})^2 \cdot \frac{2 \text{ in}}{\text{min}}$$

$$= \boxed{288\pi \frac{\text{in}^3}{\text{min}}}$$

$$\frac{dr}{dt} = 2 \text{ in/min}$$

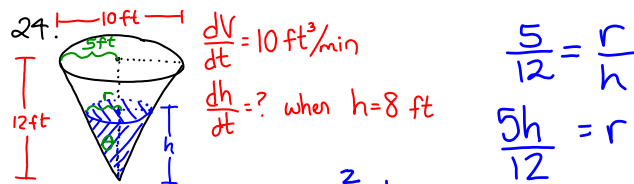
$$\frac{dV}{dt} = ? \text{ when } r = 6 \text{ in}$$

22. $V = \frac{1}{3} \pi r^2 h$ $\frac{dr}{dt} = 2 \text{ in/min}$
 $V = \frac{\pi}{3} r^2 (3r)$ $h = 3r$
 $V = \pi r^3$ $\frac{dV}{dt} = ? \text{ when } r = 6 \text{ in}$

~~$\frac{d}{dt} [V] = \frac{d}{dt} \left[\frac{1}{3} \pi r^2 h \right]$~~

~~$\frac{dV}{dt} = \frac{2\pi}{3} r \cdot \frac{dr}{dt} h + \frac{1}{3} \pi r^2 \cdot \frac{dh}{dt}$~~

$\frac{dV}{dt} = 3\pi r^2 \cdot \frac{dr}{dt}$
 $= 3\pi (6 \text{ in})^2 \cdot \frac{2 \text{ in}}{\text{min}}$
 $= 216\pi \text{ in}^3/\text{min}$



$V = \frac{1}{3} \pi r^2 h = \frac{\pi}{3} \left(\frac{5h}{12} \right)^2 \cdot h$

$V = \frac{25\pi}{3 \cdot 144} h^3$

$\frac{d}{dt} [V] = \frac{d}{dt} \left[\frac{25\pi}{3 \cdot 144} h^3 \right]$

$\frac{dV}{dt} = \frac{25\pi}{144} h^2 \cdot \frac{dh}{dt}$

$\frac{dh}{dt} = \frac{\frac{dV}{dt}}{\frac{25\pi h^2}{144}} = \frac{144 \cdot \frac{dV}{dt}}{25\pi h^2} = \frac{144 \cdot 10}{25\pi (8)^2}$

$= \frac{3 \cdot \cancel{4} \cdot 3 \cdot \cancel{4} \cdot \cancel{2} \cdot \cancel{8}}{5 \cdot \cancel{8} \cdot \pi \cdot \cancel{4} \cdot \cancel{2} \cdot \cancel{4} \cdot 2}$

$= \frac{9}{10\pi} \frac{\text{ft}}{\text{min}}$