

Power Rule:

$$\frac{d}{dx}[x^n] = nx^{n-1}$$

Constant Multiple Rule:

$$\frac{d}{dx}[cf(x)] = c \frac{d}{dx}[f(x)]$$

Sum & Difference:

$$\frac{d}{dx}[f(x) \pm g(x)] = f'(x) \pm g'(x)$$

Trig Functions:

$$\frac{d}{dx}[\sin x] = \cos x$$

$$\frac{d}{dx}[\cos x] = -\sin x$$

$$\frac{d}{dx}[\tan x] = \sec^2 x$$

$$\frac{d}{dx}[\cot x] = -\csc^2 x$$

Product Rule:

$$\frac{d}{dx}[f(x)g(x)] = f'(x)g(x) + f(x)g'(x)$$

Quotient Rule:

$$\frac{d}{dx}\left[\frac{f(x)}{g(x)}\right] = \frac{f'(x)g(x) - f(x)g'(x)}{g^2(x)}$$

Chain Rule:

$$\frac{d}{dx}[f(g(x))] = f'(g(x))g'(x)$$

$$f(x) = (5x) [\sin(x^2)]$$

$$\begin{aligned} f'(x) &= (5x)' [\sin(x^2)] + (5x) [\sin(x^2)]' \\ &= \left[5 \sin(x^2) + (5x) \cdot \cos(x^2) \cdot 2x \right] \\ &= 5 \sin(x^2) + 10x^2 \cos(x^2) \end{aligned}$$

$$f(x) = 5 \sin(3 \cos(2x^5))$$

$$f'(x) = 5 \left[\cos(3 \cos 2x^5) \right] \cdot \left(-3 \left[\sin(2x^5) \right] \right) \cdot 10x^4$$

$$= -150x^4 \cos(3 \cos 2x^5) \sin(2x^5)$$

$$f(x) = x(\sin x) \sqrt{x-1}$$

$$f(x) = [x(\sin x)] [(x-1)^{1/2}]$$

$$f'(x) = [x(\sin x)]' [(x-1)^{1/2}] + [x(\sin x)] [(x-1)^{1/2}]'$$

$$= [1 \cdot \sin x + x \cdot \cos x] \sqrt{x-1} + (x \sin x) \cdot \frac{1}{2} (x-1)^{-1/2} \cdot 1$$

$$f(x) = \sec^2(\sin(3x))$$

$$f^2(x) = [f(x)]^2$$

$$= [\sec(\sin(3x))]^2$$

$$f'(x) = 2\sec(\sin 3x) \cdot \sec(\sin 3x) \tan(\sin 3x) \cdot \cos 3x \cdot 3$$

$$f(x) = [5 \cos(2x)] \sqrt{x^2 + 3}$$

$$f(x) = \frac{\cot(x^3)}{5x^{2/3} - 4x^5 + 3x}$$

$$f(x) = \sqrt[3]{\tan(4 - x^2)}$$

$$f(x) = x\sqrt{x} \sec(3x^{-4})$$

$$f(x) = \frac{9\sqrt{2x-1}}{\csc 5x - 3}$$

$$f(x) = 6 \sin^2(x\sqrt{1-x^3})$$

$$f(x) = (2x^{-3}) \sec \sqrt{9x - \cos x}$$