

$$\frac{d}{dx} f(x) = f'(x) \quad f(x)$$

$$[g(x)]^2 = g^2(x)$$

~~$$f(x)'$$~~

$$g(x)^2 = g(x^2)$$

$$\frac{d}{dx} [\csc x] = -\csc x \cot x$$

~~$$= -\csc \cot x$$~~

$$\frac{d}{dx} [\sqrt[3]{x} \sin x] = \frac{d}{dx} [(x^{1/3})(\sin x)]$$

$$= \left(\frac{1}{3}x^{-2/3}\right)(\sin x) + (x^{1/3})(\cos x)$$

Let  $h(x) = \frac{\csc(3x)}{x^3}$ .

Find  $h'(x)$ .

Choose 1 answer:

(A)  $\frac{-\csc(3x) \cot(3x)}{3x^2}$

(B)  $\frac{-\csc(3x) \cot(3x)}{x^2}$

(C)  $\frac{-\csc(3x)(x \cot(3x) + 3)}{x^6}$

(D)  $\frac{-3 \csc(3x)(x \cot(3x) + 1)}{x^4}$

$$h'(x) = \frac{x^3 \cdot (-\csc 3x \cot 3x) \cdot 3 - (\csc 3x)(3x^2)}{(x^3)^2}$$

$$= \frac{-3x^2 \csc 3x (x \cot 3x + 1)}{x^6}$$

$$= \frac{-3 \csc 3x (x \cot 3x + 1)}{x^4}$$

$$y = -3 \tan^3(\sin(x)) = -3 [\tan(\sin x)]^3$$

Find  $\frac{dy}{dx}$ .

Choose 1 answer:

- (A)  $-9 \sin^2(x) \cos(x) \sec^2(\sin^3(x))$
- (B)  $-9 \tan^2(x) \sec^2(\sin(x)) \cos(x)$
- (C)  $-9 \sec^2(x) \sin^2(\tan(x)) \cos(\tan(x))$
- (D)  $-9 \tan^2(\sin(x)) \sec^2(\sin(x)) \cos(x)$

$$y' = -9 [\tan(\sin x)]^2 \cdot \sec^2(\sin x) \cdot \cos x$$

$$\text{Let } h(x) = x \cos^3(x). = [(x) (\cos x)^3]$$

Find  $h'(x)$ .

Choose 1 answer:

- (A)  $-3 \cos^2(x) \sin(x)$
- (B)  $\cos^2(x) (\cos(x) + 3x)$
- (C)  $\cos^3(x) - x \sin^3(x)$
- (D)  $\cos^2(x) (\cos(x) - 3x \sin(x))$

$$\begin{aligned} h'(x) &= 1 \cdot \cos^3 x + x \cdot 3 \cos^2 x \cdot (-\sin x) \\ &= \cos^2 x (\cos x - 3x \sin x) \end{aligned}$$

Let  $f(x) = \log_3(x - 4x^2)$ .

Find  $f'(x)$ .

Choose 1 answer:

A  $\frac{1 - 8x}{(x - 4x^2) \ln(3)}$

B  $\frac{1 - 8x}{(x - 4x^2) \log_3(x)}$

C  $\frac{1 - 8x}{x - 4x^2}$

D  $\frac{1}{(x - 4x^2) \ln(3)}$

$$f'(x) = \frac{1}{(x - 4x^2) \ln 3} \cdot (1 - 8x)$$

$$= \frac{1 - 8x}{(x - 4x^2) \ln 3}$$

Let  $g(x) = 3^{(5x-2)}$ .

Find  $g'(x)$ .

Choose 1 answer:

A  $5 \ln(3) \cdot 3^{(5x-2)}$

B  $\ln(3) \cdot 3^{(5x-2)}$

C  $5 \cdot 3^{(5x-2)}$

D  $(5x - 2) \cdot 3^{(5x-3)}$

$$g'(x) = 3^{5x-2} \ln 3 \cdot 5$$

~~$$= 15^{5x-2} \ln 3$$~~

If  $f(x) = \sin(e^{-x})$ , then  $f'(x) =$   $\cos(e^{-x}) \cdot e^{-x} \cdot (-1)$

- (A)  $-\cos(e^{-x})$   
(B)  $\cos(e^{-x}) + e^{-x}$   
(C)  $\cos(e^{-x}) - e^{-x}$   
(D)  $e^{-x} \cos(e^{-x})$   
(E)  $-e^{-x} \cos(e^{-x})$

For a function  $g$ , we are given that  $g(7) = -3$  and  $g'(7) = -1$ .

What's the equation of the tangent line to the graph of  $g$  at  $x = 7$ ?

Choose 1 answer:

(A)  $y - 7 = -1(x + 3)$

(B)  $y - 7 = -3(x + 1)$

(C)  $y + 1 = -3(x - 7)$

(D)  $y + 3 = -1(x - 7)$

$$y - y_1 = m(x - x_1)$$

$$y - (-3) = -1(x - 7)$$

What is the instantaneous rate of change at  $x = 2$  of the function  $f$  given by  $f(x) = \frac{x^2 - 2}{x - 1}$ ?

(A) -2

(B)  $\frac{1}{6}$ (C)  $\frac{1}{2}$ 

(D) 2

(E) 6

$$f'(x) = \frac{(x-1)(2x) - (x^2-2)(1)}{(x-1)^2}$$

$$f'(2) = \frac{1 \cdot 4 - (4-2)}{1} = \frac{4-2}{1} = 2$$

The following table lists the values of functions  $g$  and  $h$ , and of their derivatives,  $g'$  and  $h'$ , for the  $x$ -values  $-2$  and  $3$ .

$x$	$g(x)$	$h(x)$	$g'(x)$	$h'(x)$
-2	0	3	1	-5
3	5	3	1	5

Evaluate  $\frac{d}{dx} [g(h(x))]$  at  $x = -2$ .

$$= \boxed{-5}$$

$$\frac{d}{dx} [g(h(x))] =$$

$$g'(h(x)) \cdot h'(x)$$

$$= g'(h(-2)) \cdot h'(-2)$$

$$= g'(3) \cdot (-5) = 1 \cdot (-5)$$

The graph of function  $h$  is given below. It has a vertical asymptote at  $x = -5$  and a horizontal asymptote at  $y = -2$ .

Select all the  $x$ -values for which  $h$  is not differentiable.

Choose all answers that apply:

- (A)  $-5$
- (B)  $-4$
- (C)  $-2$
- (D)  $0$

