

If $(0,1)$ is countable, then \exists a 1-1 function
 $f: \mathbb{N} \rightarrow (0,1)$. (& onto)

$f(n) =$ some decimal (it's a real # in $(0,1)$)

$f(1)$

$f(2)$

\dots
 $f(n) \dots$

	1	2	3	4	5	6
1	$1/1 \rightarrow$	$2/1$	$3/1$			
2	$1/2 \leftarrow$					
3	$1/3 \rightarrow$					
4	$1/4$					
5	$1/5$					
6						

$$A \times B = \{ (a, b) \mid a \in A \text{ and } b \in B \}$$

$$\mathbb{R}^2 = \mathbb{R} \times \mathbb{R} = \{ (x, y) \mid x, y \in \mathbb{R} \}$$

3A. Union of 2 finite sets is finite
 Let A & B be finite sets with cardinality m & n respectively.
 \Rightarrow there is a 1-1 correspondence f between A & a set of
 the set $\{1, 2, \dots, m\}$. & a 1-1 correspondence g
 between B & the set $\{1, 2, \dots, n\}$

The set $A \cup B$

Let the elements of A be $\{a_1, a_2, \dots, a_m\}$ & elements
 of B be $\{b_1, b_2, \dots, b_n\}$

Define $h: \mathbb{N} \rightarrow A \cup B$ so that

$$h(1) = a_1, h(2) = a_2, \dots, h(m) = a_m$$

$$h(m+1) = b_1, h(m+2) = b_2, \dots, h(m+n) = b_n.$$

h as defined is finite. If $h(x) = h(y)$ for any x, y ,
 we are making the set smaller, but still finite

1.3
#1, 3, 7, 9

Read 1.4