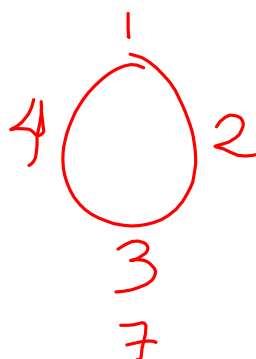


$$21 \equiv 9 \pmod{12}$$

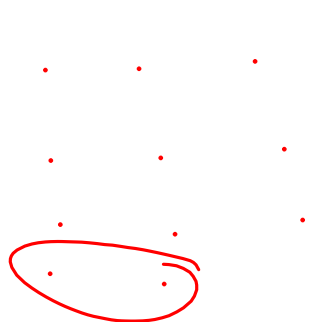


$$7 \equiv 3 \pmod{4}$$

$$26 \equiv 2 \pmod{4}$$

$$N \equiv 2 \pmod{3}$$

$$2 \equiv 5 \equiv 2 \pmod{3} \equiv 17$$



$$0 \equiv 0 \pmod{3}$$

$$1 \equiv 1 \pmod{3}$$

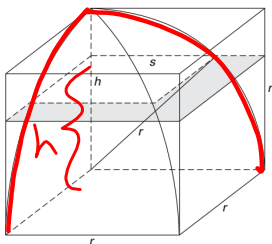
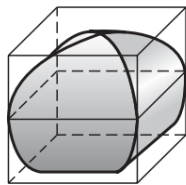
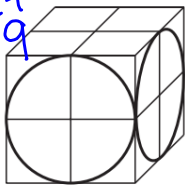
$$2 \equiv 2 \pmod{3}$$

$$3 \equiv 0 \pmod{3}$$

a group is a set w/ an operation
 (usually + or ·)
 that is closed under that operation
 & has an identity element &
 every element has an inverse in that set

$\{0, 1, 2\}$ is a group under addition mod 3
 $2^{-1} \equiv 1 \pmod{3}$ bc $2+1 = 0 \pmod{3}$

Ch 7
 #9

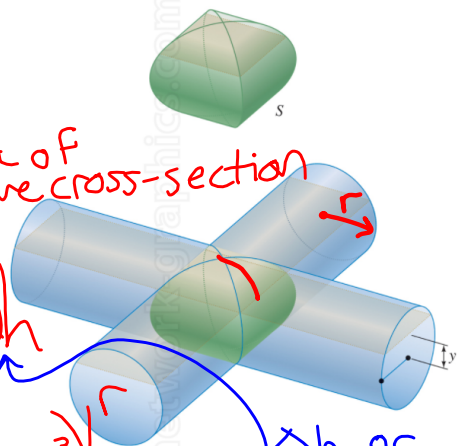


$S^2 = \text{area of square cross-section}$

$$V = 8 \int_0^r (r^2 - h^2) dh$$

$$= 8 \left(r^2 h - \frac{1}{3} h^3 \right) \Big|_0^r$$

$$= 8r^3 - \frac{8}{3} r^3 = \frac{16}{3} r^3$$



Δh or width of skinny rectangular prism

$$S^2 = r^2 - h^2$$

$$S^2 + h^2 = r^2$$

$$(x^2 + y^2 = r^2)$$

